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ENGINEERING DESIGN HANDBOOK, EXPERIMENTAL  
STATISTICS. SECTION 5

December 1969

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# ENGINEERING DESIGN HANDBOOK

## EXPERIMENTAL STATISTICS

### SECTION 5

### TABLES

HEADQUARTERS, U.S. ARMY MATERIEL COMMAND

DECEMBER 1969

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HEADQUARTERS  
UNITED STATES ARMY MATERIEL COMMAND  
WASHINGTON, D.C. 20315

17 December 1969

AMC PAMPHLET  
No. 706-114\*

ENGINEERING DESIGN HANDBOOK  
EXPERIMENTAL STATISTICS (SEC 5)

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## FOREWORD

### INTRODUCTION

This is one of a group of handbooks covering the engineering information and quantitative data needed in the design, development, construction, and test of military equipment which (as a group) constitute the Army Materiel Command Engineering Design Handbook.

### PURPOSE OF HANDBOOK

The Handbook on Experimental Statistics has been prepared as an aid to scientists and engineers engaged in Army research and development programs, and especially as a guide and ready reference for military and civilian personnel who have responsibility for the planning and interpretation of experiments and tests relating to the performance of Army equipment in the design and developmental stages of production.

### SCOPE AND USE OF HANDBOOK

This Handbook is a collection of statistical procedures and tables. It is presented in five sections, viz:

AMCP 706-110, Section 1, Basic Concepts and Analysis of Measurement Data (Chapters 1-6)

AMCP 706-111, Section 2, Analysis of Enumerative and Classificatory Data (Chapters 7-10)

AMCP 706-112, Section 3, Planning and Analysis of Comparative Experiments (Chapters 11-14)

AMCP 706-113, Section 4, Special Topics (Chapters 15-23)

AMCP 706-114, Section 5, Tables

Section 1 provides an elementary introduction to basic statistical concepts and furnishes full details on standard statistical techniques for the analysis and interpretation of measure-

ment data. Section 2 provides detailed procedures for the analysis and interpretation of enumerative and classificatory data. Section 3 has to do with the planning and analysis of comparative experiments. Section 4 is devoted to consideration and exemplification of a number of important but as yet non-standard statistical techniques, and to discussion of various other special topics. An index for the material in all four sections is placed at the end of Section 4. Section 5 contains all the mathematical tables needed for application of the procedures given in Sections 1 through 4.

An understanding of a few basic statistical concepts, as given in Chapter 1, is necessary; otherwise each of the first four sections is largely independent of the others. Each procedure, test, and technique described is illustrated by means of a worked example. A list of authoritative references is included, where appropriate, at the end of each chapter. Step-by-step instructions are given for attaining a stated goal, and the conditions under which a particular procedure is strictly valid are stated explicitly. An attempt is made to indicate the extent to which results obtained by a given procedure are valid to a good approximation when these conditions are not fully met. Alternative procedures are given for handling cases where the more standard procedures cannot be trusted to yield reliable results.

The Handbook is intended for the user with an engineering background who, although he has an occasional need for statistical techniques, does not have the time or inclination to become an expert on statistical theory and methodology.

The Handbook has been written with three types of users in mind. The first is the person who has had a course or two in statistics, and who may even have had some practical experience in applying statistical methods in the past, but who does not have statistical ideas and techniques at his fingertips. For him, the Handbook will provide a ready reference source of once familiar ideas and techniques. The second is the

person who feels, or has been advised, that some particular problem can be solved by means of fairly simple statistical techniques, and is in need of a book that will enable him to obtain the solution to his problem with a minimum of outside assistance. The Handbook should enable such a person to become familiar with the statistical ideas, and reasonably adept at the techniques, that are most fruitful in his particular line of research and development work. Finally, there is the individual who, as the head of, or as a member of a service group, has responsibility for analyzing and interpreting experimental and test data brought in by scientists and engineers engaged in Army research and development work. This individual needs a ready source of model work sheets and worked examples corresponding to the more common applications of statistics, to free him from the need of translating textbook discussions into step-by-step procedures that can be followed by individuals having little or no previous experience with statistical methods.

It is with this last need in mind that some of the procedures included in the Handbook have been explained and illustrated in detail twice: once for the case where the important question is whether the performance of a new material, product, or process exceeds an established standard; and again for the case where the important question is whether its performance is not up to the specified standards. Small but serious errors are often made in changing "greater than" procedures into "less than" procedures.

#### **AUTHORSHIP AND ACKNOWLEDGMENTS**

The Handbook on Experimental Statistics was prepared in the Statistical Engineering Laboratory, National Bureau of Standards, under a contract with the Department of Army. The project was under the general guidance of Churchill Eisenhart, Chief, Statistical Engineering Laboratory.

Most of the present text is by Mary G. Natrella, who had overall responsibility for the completion of the final version of the Handbook. The original plans for coverage, a first draft of the text, and some original tables were prepared by Paul N. Somerville. Chapter 6 is by Joseph M. Cameron; most of Chapter 1 and all of Chapters 20 and 23 are by Churchill Eisenhart; and Chapter 10 is based on a nearly-final draft by Mary L. Epling.

Other members of the staff of the Statistical Engineering Laboratory have aided in various ways through the years, and the assistance of all who helped is gratefully acknowledged. Particular mention should be made of Norman C. Severo, for assistance with Section 2, and of Shirley Young Lehman for help in the collection and computation of examples.

Editorial assistance and art preparation were provided by John I. Thompson & Company, Washington, D. C. Final preparation and arrangement for publication of the Handbook were performed by the Engineering Handbook Office, Duke University.

Appreciation is expressed for the generous cooperation of publishers and authors in granting permission for the use of their source material. References for tables and other material, taken wholly or in part, from published works, are given on the respective first pages.

Elements of the U. S. Army Materiel Command having need for handbooks may submit requisitions or official requests directly to the Publications and Reproduction Agency, Letterkenny Army Depot, Chambersburg, Pennsylvania 17201. Contractors should submit such requisitions or requests to their contracting officers.

Comments and suggestions on this handbook are welcome and should be addressed to Army Research Office-Durham, Box CM, Duke Station, Durham, North Carolina 27706.

## PREFACE

This listing is a guide to the Section and Chapter subject coverage in all Sections of the Handbook on Experimental Statistics.

*Chapter  
No.*

*Title*

### AMCP 706-110 (SECTION 1) — BASIC STATISTICAL CONCEPTS AND STANDARD TECHNIQUES FOR ANALYSIS AND INTERPRETATION OF MEASUREMENT DATA

- 1 — Some Basic Statistical Concepts and Preliminary Considerations
- 2 — Characterizing the Measured Performance of a Material, Product, or Process
- 3 — Comparing Materials or Products with Respect to Average Performance
- 4 — Comparing Materials or Products with Respect to Variability of Performance
- 5 — Characterizing Linear Relationships Between Two Variables
- 6 — Polynomial and Multivariable Relationships, Analysis by the Method of Least Squares

### AMCP 706-111 (SECTION 2) — ANALYSIS OF ENUMERATIVE AND CLASSIFICATORY DATA

- 7 — Characterizing the Qualitative Performance of a Material, Product, or Process
- 8 — Comparing Materials or Products with Respect to a Two-Fold Classification of Performance (Comparing Two Percentages)
- 9 — Comparing Materials or Products with Respect to Several Categories of Performance (Chi-Square Tests)
- 10 — Sensitivity Testing

### AMCP 706-112 (SECTION 3) — THE PLANNING AND ANALYSIS OF COMPARATIVE EXPERIMENTS

- 11 — General Considerations in Planning Experiments
- 12 — Factorial Experiments
- 13 — Randomized Blocks, Latin Squares, and Other Special-Purpose Designs
- 14 — Experiments to Determine Optimum Conditions or Levels

### AMCP 706-113 (SECTION 4) — SPECIAL TOPICS

- 15 — Some "Short-Cut" Tests for Small Samples from Normal Populations
  - 16 — Some Tests Which Are Independent of the Form of the Distribution
  - 17 — The Treatment of Outliers
  - 18 — The Place of Control Charts in Experimental Work
  - 19 — Statistical Techniques for Analyzing Extreme-Value Data
  - 20 — The Use of Transformations
  - 21 — The Relation Between Confidence Intervals and Tests of Significance
  - 22 — Notes on Statistical Computations
  - 23 — Expression of the Uncertainties of Final Results
- Index

### AMCP 706-114 (SECTION 5) — TABLES

Tables A-1 through A-37



## SECTION 5

## TABLES

This section contains all the mathematical tables referenced throughout Sections 1 through 4 of this handbook, and needed in the application of the given procedures. The tables have been informally arranged in groups as follows: Tables A-1 through A-5 are needed for the "standard" tests of significance; Tables A-6 through A-21 are further tables concerning the analysis of samples from normal distributions; Tables A-22 through A-27 are concerned with analysis of samples from binomial distributions; Tables A-30 through A-35 are for distribution-free techniques; and Tables A-36 and A-37 are sample pages of tables of random numbers and random normal deviates.

## THE GREEK ALPHABET

|           |            |         |            |            |         |
|-----------|------------|---------|------------|------------|---------|
| A         | $\alpha$   | alpha   | N          | $\nu$      | nu      |
| B         | $\beta$    | beta    | $\Xi$      | $\xi$      | xi      |
| $\Gamma$  | $\gamma$   | gamma   | O          | $\omicron$ | omicron |
| $\Delta$  | $\delta$   | delta   | $\Pi$      | $\pi$      | pi      |
| E         | $\epsilon$ | epsilon | P          | $\rho$     | rho     |
| Z         | $\zeta$    | zeta    | $\Sigma$   | $\sigma$   | sigma   |
| H         | $\eta$     | eta     | T          | $\tau$     | tau     |
| $\Theta$  | $\theta$   | theta   | $\Upsilon$ | $\upsilon$ | upsilon |
| I         | $\iota$    | iota    | $\Phi$     | $\phi$     | phi     |
| K         | $\kappa$   | kappa   | X          | $\chi$     | chi     |
| $\Lambda$ | $\lambda$  | lambda  | $\Psi$     | $\psi$     | psi     |
| M         | $\mu$      | mu      | $\Omega$   | $\omega$   | omega   |

## TABLES

TABLE A-1. CUMULATIVE NORMAL DISTRIBUTION — VALUES OF  $P$ 

Values of  $P$  corresponding to  $z_p$  for the normal curve.

$z$  is the standard normal variable. The value of  $P$  for  $-z_p$  equals one minus the value of  $P$  for  $+z_p$ ,  
e.g., the  $P$  for  $-1.62$  equals  $1 - .9474 = .0526$ .

| $z_p$ | .00   | .01   | .02   | .03   | .04   | .05   | .06   | .07   | .08   | .09   |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| .0    | .5000 | .5040 | .5080 | .5120 | .5160 | .5199 | .5239 | .5279 | .5319 | .5359 |
| .1    | .5398 | .5438 | .5478 | .5517 | .5557 | .5596 | .5636 | .5675 | .5714 | .5753 |
| .2    | .5793 | .5832 | .5871 | .5910 | .5948 | .5987 | .6026 | .6064 | .6103 | .6141 |
| .3    | .6179 | .6217 | .6255 | .6293 | .6331 | .6368 | .6406 | .6443 | .6480 | .6517 |
| .4    | .6554 | .6591 | .6628 | .6664 | .6700 | .6736 | .6772 | .6808 | .6844 | .6879 |
| .5    | .6915 | .6950 | .6985 | .7019 | .7054 | .7088 | .7123 | .7157 | .7190 | .7224 |
| .6    | .7257 | .7291 | .7324 | .7357 | .7389 | .7422 | .7454 | .7486 | .7517 | .7549 |
| .7    | .7580 | .7611 | .7642 | .7673 | .7704 | .7734 | .7764 | .7794 | .7823 | .7852 |
| .8    | .7881 | .7910 | .7939 | .7967 | .7995 | .8023 | .8051 | .8078 | .8106 | .8133 |
| .9    | .8159 | .8186 | .8212 | .8238 | .8264 | .8289 | .8315 | .8340 | .8365 | .8389 |
| 1.0   | .8413 | .8438 | .8461 | .8485 | .8508 | .8531 | .8554 | .8577 | .8599 | .8621 |
| 1.1   | .8643 | .8665 | .8686 | .8708 | .8729 | .8749 | .8770 | .8790 | .8810 | .8830 |
| 1.2   | .8849 | .8869 | .8888 | .8907 | .8925 | .8944 | .8962 | .8980 | .8997 | .9015 |
| 1.3   | .9032 | .9049 | .9066 | .9082 | .9099 | .9115 | .9131 | .9147 | .9162 | .9177 |
| 1.4   | .9192 | .9207 | .9222 | .9236 | .9251 | .9265 | .9279 | .9292 | .9306 | .9319 |
| 1.5   | .9332 | .9345 | .9357 | .9370 | .9382 | .9394 | .9406 | .9418 | .9429 | .9441 |
| 1.6   | .9452 | .9463 | .9474 | .9484 | .9495 | .9505 | .9515 | .9525 | .9535 | .9545 |
| 1.7   | .9554 | .9564 | .9573 | .9582 | .9591 | .9599 | .9608 | .9616 | .9625 | .9633 |
| 1.8   | .9641 | .9649 | .9656 | .9664 | .9671 | .9678 | .9686 | .9693 | .9699 | .9706 |
| 1.9   | .9713 | .9719 | .9726 | .9732 | .9738 | .9744 | .9750 | .9756 | .9761 | .9767 |
| 2.0   | .9772 | .9778 | .9783 | .9788 | .9793 | .9798 | .9803 | .9808 | .9812 | .9817 |
| 2.1   | .9821 | .9826 | .9830 | .9834 | .9838 | .9842 | .9846 | .9850 | .9854 | .9857 |
| 2.2   | .9861 | .9864 | .9868 | .9871 | .9875 | .9878 | .9881 | .9884 | .9887 | .9890 |
| 2.3   | .9893 | .9896 | .9898 | .9901 | .9904 | .9906 | .9909 | .9911 | .9913 | .9916 |
| 2.4   | .9918 | .9920 | .9922 | .9925 | .9927 | .9929 | .9931 | .9932 | .9934 | .9936 |
| 2.5   | .9938 | .9940 | .9941 | .9943 | .9945 | .9946 | .9948 | .9949 | .9951 | .9952 |
| 2.6   | .9953 | .9955 | .9956 | .9957 | .9959 | .9960 | .9961 | .9962 | .9963 | .9964 |
| 2.7   | .9965 | .9966 | .9967 | .9968 | .9969 | .9970 | .9971 | .9972 | .9973 | .9974 |
| 2.8   | .9974 | .9975 | .9976 | .9977 | .9977 | .9978 | .9979 | .9979 | .9980 | .9981 |
| 2.9   | .9981 | .9982 | .9982 | .9983 | .9984 | .9984 | .9985 | .9985 | .9986 | .9986 |
| 3.0   | .9987 | .9987 | .9987 | .9988 | .9988 | .9989 | .9989 | .9989 | .9990 | .9990 |
| 3.1   | .9990 | .9991 | .9991 | .9991 | .9992 | .9992 | .9992 | .9992 | .9993 | .9993 |
| 3.2   | .9993 | .9993 | .9994 | .9994 | .9994 | .9994 | .9994 | .9995 | .9995 | .9995 |
| 3.3   | .9995 | .9995 | .9995 | .9996 | .9996 | .9996 | .9996 | .9996 | .9996 | .9997 |
| 3.4   | .9997 | .9997 | .9997 | .9997 | .9997 | .9997 | .9997 | .9997 | .9997 | .9998 |

TABLE A-2. CUMULATIVE NORMAL DISTRIBUTION — VALUES OF  $z_p$



Values of  $z_p$  corresponding to  $P$  for the normal curve.

$z$  is the standard normal variable

| $P$ | .00   | .01   | .02   | .03   | .04   | .05   | .06   | .07   | .08   | .09   |
|-----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| .00 | —     | -2.33 | -2.05 | -1.88 | -1.75 | -1.64 | -1.55 | -1.48 | -1.41 | -1.34 |
| .10 | -1.28 | -1.23 | -1.18 | -1.13 | -1.08 | -1.04 | -0.99 | -0.95 | -0.92 | -0.88 |
| .20 | -0.84 | -0.81 | -0.77 | -0.74 | -0.71 | -0.67 | -0.64 | -0.61 | -0.58 | -0.55 |
| .30 | -0.52 | -0.50 | -0.47 | -0.44 | -0.41 | -0.39 | -0.36 | -0.33 | -0.31 | -0.28 |
| .40 | -0.25 | -0.23 | -0.20 | -0.18 | -0.15 | -0.13 | -0.10 | -0.08 | -0.05 | -0.03 |
| .50 | 0.00  | 0.03  | 0.05  | 0.08  | 0.10  | 0.13  | 0.15  | 0.18  | 0.20  | 0.23  |
| .60 | 0.25  | 0.28  | 0.31  | 0.33  | 0.36  | 0.39  | 0.41  | 0.44  | 0.47  | 0.50  |
| .70 | 0.52  | 0.55  | 0.58  | 0.61  | 0.64  | 0.67  | 0.71  | 0.74  | 0.77  | 0.81  |
| .80 | 0.84  | 0.88  | 0.92  | 0.95  | 0.99  | 1.04  | 1.08  | 1.13  | 1.18  | 1.23  |
| .90 | 1.28  | 1.34  | 1.41  | 1.48  | 1.55  | 1.64  | 1.75  | 1.88  | 2.05  | 2.33  |

Special Values

| $P$   | .001   | .005   | .010   | .025   | .050   | .100   |
|-------|--------|--------|--------|--------|--------|--------|
| $z_p$ | -3.090 | -2.576 | -2.326 | -1.960 | -1.645 | -1.282 |

| $P$   | .999  | .995  | .990  | .975  | .950  | .900  |
|-------|-------|-------|-------|-------|-------|-------|
| $z_p$ | 3.090 | 2.576 | 2.326 | 1.960 | 1.645 | 1.282 |

## TABLES

TABLE A-3. PERCENTILES OF THE  $\chi^2$  DISTRIBUTIONValues of  $\chi^2_p$  corresponding to  $P$ 

| df  | $\chi^2_{.995}$ | $\chi^2_{.99}$ | $\chi^2_{.975}$ | $\chi^2_{.95}$ | $\chi^2_{.90}$ | $\chi^2_{.80}$ | $\chi^2_{.70}$ | $\chi^2_{.60}$ | $\chi^2_{.50}$ | $\chi^2_{.40}$ |
|-----|-----------------|----------------|-----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
| 1   | .000039         | .00016         | .00098          | .0039          | .0158          | 2.71           | 3.84           | 5.02           | 6.63           | 7.88           |
| 2   | .0100           | .0201          | .0506           | .1026          | .2107          | 4.61           | 5.99           | 7.38           | 9.21           | 10.60          |
| 3   | .0717           | .115           | .216            | .352           | .584           | 6.25           | 7.81           | 9.35           | 11.34          | 12.84          |
| 4   | .207            | .297           | .484            | .711           | 1.064          | 7.78           | 9.49           | 11.14          | 13.28          | 14.86          |
| 5   | .412            | .554           | .831            | 1.15           | 1.61           | 9.24           | 11.07          | 12.83          | 15.09          | 16.75          |
| 6   | .676            | .872           | 1.24            | 1.64           | 2.20           | 10.64          | 12.59          | 14.45          | 16.81          | 18.55          |
| 7   | .989            | 1.24           | 1.69            | 2.17           | 2.83           | 12.02          | 14.07          | 16.01          | 18.48          | 20.28          |
| 8   | 1.34            | 1.65           | 2.18            | 2.73           | 3.49           | 13.36          | 15.51          | 17.53          | 20.09          | 21.96          |
| 9   | 1.73            | 2.09           | 2.70            | 3.33           | 4.17           | 14.68          | 16.92          | 19.02          | 21.67          | 23.59          |
| 10  | 2.16            | 2.56           | 3.25            | 3.94           | 4.87           | 15.99          | 18.31          | 20.48          | 23.21          | 25.19          |
| 11  | 2.60            | 3.05           | 3.82            | 4.57           | 5.58           | 17.28          | 19.68          | 21.92          | 24.73          | 26.76          |
| 12  | 3.07            | 3.57           | 4.40            | 5.23           | 6.30           | 18.55          | 21.03          | 23.34          | 26.22          | 28.30          |
| 13  | 3.57            | 4.11           | 5.01            | 5.89           | 7.04           | 19.81          | 22.36          | 24.74          | 27.69          | 29.82          |
| 14  | 4.07            | 4.66           | 5.63            | 6.57           | 7.79           | 21.06          | 23.68          | 26.12          | 29.14          | 31.32          |
| 15  | 4.60            | 5.23           | 6.26            | 7.26           | 8.55           | 22.31          | 25.00          | 27.49          | 30.58          | 32.80          |
| 16  | 5.14            | 5.81           | 6.91            | 7.96           | 9.31           | 23.54          | 26.30          | 28.85          | 32.00          | 34.27          |
| 18  | 6.26            | 7.01           | 8.23            | 9.39           | 10.86          | 25.99          | 28.87          | 31.53          | 34.81          | 37.16          |
| 20  | 7.43            | 8.26           | 9.59            | 10.85          | 12.44          | 28.41          | 31.41          | 34.17          | 37.57          | 40.00          |
| 24  | 9.89            | 10.86          | 12.40           | 13.85          | 15.66          | 33.20          | 36.42          | 39.36          | 42.98          | 45.56          |
| 30  | 13.79           | 14.95          | 16.79           | 18.49          | 20.60          | 40.26          | 43.77          | 46.98          | 50.89          | 53.67          |
| 40  | 20.71           | 22.16          | 24.43           | 26.51          | 29.05          | 51.81          | 55.76          | 59.34          | 63.69          | 66.77          |
| 60  | 35.53           | 37.48          | 40.48           | 43.19          | 46.46          | 74.40          | 79.08          | 83.30          | 88.38          | 91.95          |
| 120 | 83.85           | 86.92          | 91.58           | 95.70          | 100.62         | 140.23         | 146.57         | 152.21         | 158.95         | 163.64         |

For large degrees of freedom,

$$\chi^2_p = \frac{1}{2}(z_p + \sqrt{2\nu - 1})^2 \text{ approximately,}$$

where  $\nu$  = degrees of freedom and  $z_p$  is given in Table A-2.

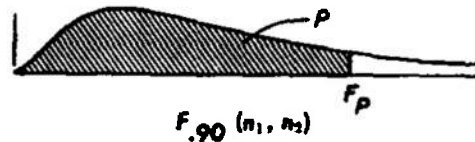
## TABLES

TABLE A-4. PERCENTILES OF THE  $t$  DISTRIBUTION

| df       | $t_{.99}$ | $t_{.95}$ | $t_{.90}$ | $t_{.80}$ | $t_{.70}$ | $t_{.50}$ | $t_{.25}$ | $t_{.10}$ | $t_{.05}$ |
|----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| 1        | .325      | .727      | 1.376     | 3.078     | 6.314     | 12.706    | 31.821    | 63.657    |           |
| 2        | .289      | .617      | 1.061     | 1.886     | 2.920     | 4.303     | 6.965     | 9.925     |           |
| 3        | .277      | .584      | .978      | 1.638     | 2.353     | 3.182     | 4.541     | 5.841     |           |
| 4        | .271      | .569      | .941      | 1.533     | 2.132     | 2.776     | 3.747     | 4.604     |           |
| 5        | .267      | .559      | .920      | 1.476     | 2.015     | 2.571     | 3.365     | 4.032     |           |
| 6        | .265      | .553      | .906      | 1.440     | 1.943     | 2.447     | 3.143     | 3.707     |           |
| 7        | .263      | .549      | .896      | 1.415     | 1.895     | 2.365     | 2.998     | 3.499     |           |
| 8        | .262      | .546      | .889      | 1.397     | 1.860     | 2.306     | 2.896     | 3.355     |           |
| 9        | .261      | .543      | .883      | 1.383     | 1.833     | 2.262     | 2.821     | 3.250     |           |
| 10       | .260      | .542      | .879      | 1.372     | 1.812     | 2.228     | 2.764     | 3.169     |           |
| 11       | .260      | .540      | .876      | 1.363     | 1.796     | 2.201     | 2.718     | 3.106     |           |
| 12       | .259      | .539      | .873      | 1.356     | 1.782     | 2.179     | 2.681     | 3.055     |           |
| 13       | .259      | .538      | .870      | 1.350     | 1.771     | 2.160     | 2.650     | 3.012     |           |
| 14       | .258      | .537      | .868      | 1.345     | 1.761     | 2.145     | 2.624     | 2.977     |           |
| 15       | .258      | .536      | .866      | 1.341     | 1.753     | 2.131     | 2.602     | 2.947     |           |
| 16       | .258      | .535      | .865      | 1.337     | 1.746     | 2.120     | 2.583     | 2.921     |           |
| 17       | .257      | .534      | .863      | 1.333     | 1.740     | 2.110     | 2.567     | 2.898     |           |
| 18       | .257      | .534      | .862      | 1.330     | 1.734     | 2.101     | 2.552     | 2.878     |           |
| 19       | .257      | .533      | .861      | 1.328     | 1.729     | 2.093     | 2.539     | 2.861     |           |
| 20       | .257      | .533      | .860      | 1.325     | 1.725     | 2.086     | 2.528     | 2.845     |           |
| 21       | .257      | .532      | .859      | 1.323     | 1.721     | 2.080     | 2.518     | 2.831     |           |
| 22       | .256      | .532      | .858      | 1.321     | 1.717     | 2.074     | 2.508     | 2.819     |           |
| 23       | .256      | .532      | .858      | 1.319     | 1.714     | 2.069     | 2.500     | 2.807     |           |
| 24       | .256      | .531      | .857      | 1.318     | 1.711     | 2.064     | 2.492     | 2.797     |           |
| 25       | .256      | .531      | .856      | 1.316     | 1.708     | 2.060     | 2.485     | 2.787     |           |
| 26       | .256      | .531      | .856      | 1.315     | 1.706     | 2.056     | 2.479     | 2.779     |           |
| 27       | .256      | .531      | .855      | 1.314     | 1.703     | 2.052     | 2.473     | 2.771     |           |
| 28       | .256      | .530      | .855      | 1.313     | 1.701     | 2.048     | 2.467     | 2.763     |           |
| 29       | .256      | .530      | .854      | 1.311     | 1.699     | 2.045     | 2.462     | 2.756     |           |
| 30       | .256      | .530      | .854      | 1.310     | 1.697     | 2.042     | 2.457     | 2.750     |           |
| 40       | .255      | .529      | .851      | 1.303     | 1.684     | 2.021     | 2.423     | 2.704     |           |
| 60       | .254      | .527      | .848      | 1.296     | 1.671     | 2.000     | 2.390     | 2.660     |           |
| 120      | .254      | .526      | .845      | 1.289     | 1.658     | 1.980     | 2.358     | 2.617     |           |
| $\infty$ | .253      | .524      | .842      | 1.282     | 1.645     | 1.960     | 2.326     | 2.576     |           |

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TABLE A-5. PERCENTILES OF THE F DISTRIBUTION

 $n_1$  = degrees of freedom for numerator

| $n_2 \backslash n_1$ | 1     | 2     | 3     | 4     | 5     | 6     | 7     | 8     | 9     | 10    | 12    | 15    | 20    | 24    | 30    | 40    | 60    | 120   | $\infty$ |
|----------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| 1                    | 39.86 | 49.50 | 53.59 | 55.83 | 57.24 | 58.20 | 58.91 | 59.44 | 59.86 | 60.19 | 60.71 | 61.22 | 61.74 | 62.00 | 62.26 | 62.53 | 62.79 | 63.06 | 63.33    |
| 2                    | 8.53  | 9.00  | 9.16  | 9.24  | 9.29  | 9.33  | 9.35  | 9.37  | 9.38  | 9.39  | 9.41  | 9.42  | 9.44  | 9.45  | 9.46  | 9.47  | 9.47  | 9.48  | 9.49     |
| 3                    | 5.54  | 5.46  | 5.39  | 5.34  | 5.31  | 5.28  | 5.27  | 5.25  | 5.24  | 5.23  | 5.22  | 5.20  | 5.18  | 5.18  | 5.17  | 5.16  | 5.15  | 5.14  | 5.13     |
| 4                    | 4.54  | 4.32  | 4.19  | 4.11  | 4.05  | 4.01  | 3.98  | 3.95  | 3.94  | 3.92  | 3.90  | 3.87  | 3.84  | 3.83  | 3.82  | 3.80  | 3.79  | 3.78  | 3.76     |
| 5                    | 4.06  | 3.78  | 3.62  | 3.52  | 3.45  | 3.40  | 3.37  | 3.34  | 3.32  | 3.30  | 3.27  | 3.24  | 3.21  | 3.19  | 3.17  | 3.16  | 3.14  | 3.12  | 3.10     |
| 6                    | 3.78  | 3.46  | 3.29  | 3.18  | 3.11  | 3.05  | 3.01  | 2.98  | 2.96  | 2.94  | 2.90  | 2.87  | 2.84  | 2.82  | 2.80  | 2.78  | 2.76  | 2.74  | 2.72     |
| 7                    | 3.59  | 3.26  | 3.07  | 2.96  | 2.88  | 2.83  | 2.78  | 2.75  | 2.72  | 2.70  | 2.67  | 2.63  | 2.59  | 2.58  | 2.56  | 2.54  | 2.51  | 2.49  | 2.47     |
| 8                    | 3.46  | 3.11  | 2.92  | 2.81  | 2.73  | 2.67  | 2.62  | 2.59  | 2.56  | 2.50  | 2.50  | 2.46  | 2.42  | 2.40  | 2.38  | 2.36  | 2.34  | 2.32  | 2.29     |
| 9                    | 3.36  | 3.01  | 2.81  | 2.69  | 2.61  | 2.55  | 2.51  | 2.47  | 2.44  | 2.42  | 2.38  | 2.34  | 2.30  | 2.28  | 2.25  | 2.23  | 2.21  | 2.18  | 2.16     |
| 10                   | 3.29  | 2.92  | 2.73  | 2.61  | 2.52  | 2.46  | 2.41  | 2.38  | 2.35  | 2.32  | 2.28  | 2.24  | 2.20  | 2.18  | 2.16  | 2.13  | 2.11  | 2.08  | 2.06     |
| 11                   | 3.23  | 2.86  | 2.66  | 2.54  | 2.45  | 2.39  | 2.34  | 2.30  | 2.27  | 2.25  | 2.21  | 2.17  | 2.12  | 2.10  | 2.08  | 2.05  | 2.03  | 2.00  | 1.97     |
| 12                   | 3.18  | 2.81  | 2.61  | 2.48  | 2.39  | 2.33  | 2.28  | 2.24  | 2.21  | 2.19  | 2.15  | 2.10  | 2.06  | 2.04  | 2.01  | 1.99  | 1.96  | 1.93  | 1.90     |
| 13                   | 3.14  | 2.76  | 2.56  | 2.43  | 2.35  | 2.28  | 2.23  | 2.20  | 2.16  | 2.14  | 2.10  | 2.05  | 2.01  | 1.98  | 1.96  | 1.93  | 1.90  | 1.88  | 1.85     |
| 14                   | 3.10  | 2.73  | 2.52  | 2.39  | 2.31  | 2.24  | 2.19  | 2.15  | 2.12  | 2.10  | 2.05  | 2.01  | 1.96  | 1.94  | 1.91  | 1.89  | 1.86  | 1.83  | 1.80     |
| 15                   | 3.07  | 2.70  | 2.49  | 2.36  | 2.27  | 2.21  | 2.16  | 2.12  | 2.09  | 2.06  | 2.02  | 1.97  | 1.92  | 1.90  | 1.87  | 1.85  | 1.82  | 1.79  | 1.76     |
| 16                   | 3.05  | 2.67  | 2.46  | 2.33  | 2.24  | 2.18  | 2.13  | 2.09  | 2.06  | 2.03  | 1.99  | 1.94  | 1.89  | 1.87  | 1.84  | 1.81  | 1.78  | 1.75  | 1.72     |
| 17                   | 3.03  | 2.64  | 2.44  | 2.31  | 2.22  | 2.15  | 2.10  | 2.06  | 2.03  | 2.00  | 1.96  | 1.91  | 1.86  | 1.84  | 1.81  | 1.78  | 1.75  | 1.72  | 1.69     |
| 18                   | 3.01  | 2.62  | 2.42  | 2.29  | 2.20  | 2.13  | 2.08  | 2.04  | 2.00  | 1.98  | 1.93  | 1.89  | 1.84  | 1.81  | 1.78  | 1.75  | 1.72  | 1.69  | 1.66     |
| 19                   | 2.99  | 2.61  | 2.40  | 2.27  | 2.18  | 2.11  | 2.06  | 2.02  | 1.98  | 1.96  | 1.91  | 1.86  | 1.81  | 1.79  | 1.76  | 1.73  | 1.70  | 1.67  | 1.63     |
| 20                   | 2.97  | 2.59  | 2.38  | 2.25  | 2.16  | 2.09  | 2.04  | 2.00  | 1.96  | 1.94  | 1.89  | 1.84  | 1.79  | 1.77  | 1.74  | 1.71  | 1.68  | 1.64  | 1.61     |
| 21                   | 2.96  | 2.57  | 2.36  | 2.23  | 2.14  | 2.08  | 2.02  | 1.98  | 1.95  | 1.92  | 1.87  | 1.83  | 1.78  | 1.75  | 1.72  | 1.69  | 1.66  | 1.62  | 1.59     |
| 22                   | 2.95  | 2.56  | 2.35  | 2.22  | 2.13  | 2.06  | 2.01  | 1.97  | 1.93  | 1.90  | 1.86  | 1.81  | 1.76  | 1.73  | 1.70  | 1.67  | 1.64  | 1.60  | 1.57     |
| 23                   | 2.94  | 2.55  | 2.34  | 2.21  | 2.11  | 2.05  | 1.99  | 1.95  | 1.92  | 1.89  | 1.84  | 1.80  | 1.74  | 1.72  | 1.69  | 1.66  | 1.62  | 1.59  | 1.55     |
| 24                   | 2.93  | 2.54  | 2.33  | 2.19  | 2.10  | 2.04  | 1.98  | 1.94  | 1.91  | 1.88  | 1.83  | 1.78  | 1.73  | 1.70  | 1.67  | 1.64  | 1.61  | 1.57  | 1.53     |
| 25                   | 2.92  | 2.53  | 2.32  | 2.18  | 2.09  | 2.02  | 1.97  | 1.93  | 1.89  | 1.87  | 1.82  | 1.77  | 1.72  | 1.69  | 1.66  | 1.63  | 1.59  | 1.56  | 1.52     |
| 26                   | 2.91  | 2.52  | 2.31  | 2.17  | 2.08  | 2.01  | 1.96  | 1.92  | 1.88  | 1.86  | 1.81  | 1.76  | 1.71  | 1.68  | 1.65  | 1.61  | 1.58  | 1.54  | 1.50     |
| 27                   | 2.90  | 2.51  | 2.30  | 2.17  | 2.07  | 2.00  | 1.95  | 1.91  | 1.87  | 1.85  | 1.80  | 1.75  | 1.70  | 1.67  | 1.64  | 1.60  | 1.57  | 1.53  | 1.49     |
| 28                   | 2.89  | 2.50  | 2.29  | 2.16  | 2.06  | 2.00  | 1.94  | 1.90  | 1.87  | 1.84  | 1.79  | 1.74  | 1.69  | 1.66  | 1.63  | 1.59  | 1.56  | 1.52  | 1.48     |
| 29                   | 2.89  | 2.50  | 2.28  | 2.15  | 2.06  | 1.99  | 1.93  | 1.89  | 1.86  | 1.83  | 1.78  | 1.73  | 1.68  | 1.65  | 1.62  | 1.58  | 1.55  | 1.51  | 1.47     |
| 30                   | 2.88  | 2.49  | 2.28  | 2.14  | 2.05  | 1.98  | 1.93  | 1.88  | 1.85  | 1.82  | 1.77  | 1.72  | 1.67  | 1.64  | 1.61  | 1.57  | 1.54  | 1.50  | 1.46     |
| 40                   | 2.84  | 2.44  | 2.23  | 2.09  | 2.00  | 1.93  | 1.87  | 1.83  | 1.79  | 1.76  | 1.71  | 1.66  | 1.61  | 1.57  | 1.54  | 1.51  | 1.47  | 1.42  | 1.38     |
| 60                   | 2.79  | 2.39  | 2.18  | 2.04  | 1.95  | 1.87  | 1.82  | 1.77  | 1.74  | 1.71  | 1.66  | 1.60  | 1.54  | 1.51  | 1.48  | 1.44  | 1.40  | 1.35  | 1.29     |
| 120                  | 2.75  | 2.35  | 2.13  | 1.99  | 1.90  | 1.82  | 1.77  | 1.72  | 1.68  | 1.65  | 1.60  | 1.55  | 1.48  | 1.45  | 1.41  | 1.37  | 1.32  | 1.26  | 1.19     |
| $\infty$             | 2.71  | 2.30  | 2.08  | 1.94  | 1.85  | 1.77  | 1.72  | 1.67  | 1.63  | 1.60  | 1.55  | 1.49  | 1.42  | 1.38  | 1.34  | 1.30  | 1.24  | 1.17  | 1.00     |

 $n_2$  = degrees of freedom for denominator

TABLE A-5 (Continued). PERCENTILES OF THE F DISTRIBUTION

 $F_{.95}(n_1, n_2)$  $n_1$  = degrees of freedom for numerator

| $n_2 \backslash n_1$ | 1     | 2     | 3     | 4     | 5     | 6     | 7     | 8     | 9     | 10    | 12    | 15    | 20    | 24    | 30    | 40    | 60    | 120   | $\infty$ |
|----------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| 1                    | 161.4 | 199.5 | 215.7 | 224.6 | 230.2 | 234.0 | 236.8 | 238.9 | 240.5 | 241.9 | 243.9 | 245.9 | 248.0 | 249.1 | 250.1 | 251.1 | 252.2 | 253.3 | 254.3    |
| 2                    | 18.51 | 19.00 | 19.16 | 19.25 | 19.30 | 19.33 | 19.35 | 19.37 | 19.38 | 19.40 | 19.41 | 19.43 | 19.45 | 19.45 | 19.46 | 19.47 | 19.48 | 19.49 | 19.50    |
| 3                    | 10.13 | 9.55  | 9.28  | 9.12  | 9.01  | 8.94  | 8.89  | 8.85  | 8.81  | 8.79  | 8.74  | 8.70  | 8.66  | 8.64  | 8.62  | 8.59  | 8.57  | 8.55  | 8.53     |
| 4                    | 7.71  | 6.94  | 6.59  | 6.39  | 6.26  | 6.16  | 6.09  | 6.04  | 6.00  | 5.96  | 5.91  | 5.86  | 5.80  | 5.77  | 5.75  | 5.72  | 5.69  | 5.66  | 5.63     |
| 5                    | 6.61  | 5.79  | 5.41  | 5.19  | 5.05  | 4.95  | 4.88  | 4.82  | 4.77  | 4.74  | 4.68  | 4.62  | 4.56  | 4.53  | 4.50  | 4.46  | 4.43  | 4.40  | 4.36     |
| 6                    | 5.99  | 5.14  | 4.76  | 4.53  | 4.39  | 4.28  | 4.21  | 4.15  | 4.10  | 4.06  | 4.00  | 3.94  | 3.87  | 3.84  | 3.81  | 3.77  | 3.74  | 3.70  | 3.67     |
| 7                    | 5.59  | 4.74  | 4.35  | 4.12  | 3.97  | 3.87  | 3.79  | 3.73  | 3.68  | 3.64  | 3.57  | 3.51  | 3.44  | 3.41  | 3.38  | 3.34  | 3.30  | 3.27  | 3.23     |
| 8                    | 5.32  | 4.46  | 4.07  | 3.84  | 3.69  | 3.58  | 3.50  | 3.44  | 3.39  | 3.35  | 3.28  | 3.22  | 3.15  | 3.12  | 3.08  | 3.04  | 3.01  | 2.97  | 2.93     |
| 9                    | 5.12  | 4.26  | 3.86  | 3.63  | 3.48  | 3.37  | 3.29  | 3.23  | 3.18  | 3.14  | 3.07  | 3.01  | 2.94  | 2.90  | 2.86  | 2.83  | 2.79  | 2.75  | 2.71     |
| 10                   | 4.96  | 4.10  | 3.71  | 3.48  | 3.33  | 3.22  | 3.14  | 3.07  | 3.02  | 2.98  | 2.91  | 2.85  | 2.77  | 2.74  | 2.70  | 2.66  | 2.62  | 2.58  | 2.54     |
| 11                   | 4.84  | 3.98  | 3.59  | 3.36  | 3.20  | 3.09  | 3.01  | 2.95  | 2.90  | 2.85  | 2.79  | 2.72  | 2.65  | 2.61  | 2.57  | 2.53  | 2.49  | 2.45  | 2.40     |
| 12                   | 4.75  | 3.89  | 3.49  | 3.26  | 3.11  | 3.00  | 2.91  | 2.85  | 2.80  | 2.75  | 2.69  | 2.62  | 2.54  | 2.51  | 2.47  | 2.43  | 2.38  | 2.34  | 2.30     |
| 13                   | 4.67  | 3.81  | 3.41  | 3.18  | 3.03  | 2.92  | 2.83  | 2.77  | 2.71  | 2.67  | 2.60  | 2.53  | 2.46  | 2.42  | 2.38  | 2.34  | 2.30  | 2.25  | 2.21     |
| 14                   | 4.60  | 3.74  | 3.34  | 3.11  | 2.96  | 2.85  | 2.76  | 2.70  | 2.65  | 2.60  | 2.53  | 2.46  | 2.39  | 2.35  | 2.31  | 2.27  | 2.22  | 2.18  | 2.13     |
| 15                   | 4.54  | 3.68  | 3.29  | 3.06  | 2.90  | 2.79  | 2.71  | 2.64  | 2.59  | 2.54  | 2.48  | 2.40  | 2.33  | 2.29  | 2.25  | 2.20  | 2.16  | 2.11  | 2.07     |
| 16                   | 4.49  | 3.63  | 3.24  | 3.01  | 2.85  | 2.74  | 2.66  | 2.59  | 2.54  | 2.49  | 2.42  | 2.35  | 2.28  | 2.24  | 2.19  | 2.15  | 2.11  | 2.06  | 2.01     |
| 17                   | 4.45  | 3.59  | 3.20  | 2.96  | 2.81  | 2.70  | 2.61  | 2.55  | 2.49  | 2.45  | 2.38  | 2.31  | 2.23  | 2.19  | 2.15  | 2.10  | 2.06  | 2.01  | 1.96     |
| 18                   | 4.41  | 3.55  | 3.16  | 2.93  | 2.77  | 2.66  | 2.58  | 2.51  | 2.46  | 2.41  | 2.34  | 2.27  | 2.19  | 2.15  | 2.11  | 2.06  | 2.02  | 1.97  | 1.92     |
| 19                   | 4.38  | 3.52  | 3.13  | 2.90  | 2.74  | 2.63  | 2.54  | 2.48  | 2.42  | 2.38  | 2.31  | 2.23  | 2.16  | 2.11  | 2.07  | 2.03  | 1.98  | 1.93  | 1.88     |
| 20                   | 4.35  | 3.49  | 3.10  | 2.87  | 2.71  | 2.60  | 2.51  | 2.45  | 2.39  | 2.35  | 2.28  | 2.20  | 2.12  | 2.08  | 2.04  | 1.99  | 1.95  | 1.90  | 1.84     |
| 21                   | 4.32  | 3.47  | 3.07  | 2.84  | 2.68  | 2.57  | 2.49  | 2.42  | 2.37  | 2.32  | 2.25  | 2.18  | 2.10  | 2.05  | 2.01  | 1.96  | 1.92  | 1.87  | 1.81     |
| 22                   | 4.30  | 3.44  | 3.05  | 2.82  | 2.66  | 2.55  | 2.46  | 2.40  | 2.34  | 2.30  | 2.23  | 2.15  | 2.07  | 2.03  | 1.98  | 1.94  | 1.89  | 1.84  | 1.78     |
| 23                   | 4.28  | 3.42  | 3.03  | 2.80  | 2.64  | 2.53  | 2.44  | 2.37  | 2.32  | 2.27  | 2.20  | 2.13  | 2.05  | 2.01  | 1.96  | 1.91  | 1.86  | 1.81  | 1.76     |
| 24                   | 4.26  | 3.40  | 3.01  | 2.78  | 2.62  | 2.51  | 2.42  | 2.36  | 2.30  | 2.25  | 2.18  | 2.11  | 2.03  | 1.98  | 1.94  | 1.89  | 1.84  | 1.79  | 1.73     |
| 25                   | 4.24  | 3.39  | 2.99  | 2.76  | 2.60  | 2.49  | 2.40  | 2.34  | 2.28  | 2.24  | 2.16  | 2.09  | 2.01  | 1.96  | 1.92  | 1.87  | 1.82  | 1.77  | 1.71     |
| 26                   | 4.23  | 3.37  | 2.98  | 2.74  | 2.59  | 2.47  | 2.39  | 2.32  | 2.27  | 2.22  | 2.15  | 2.07  | 1.99  | 1.95  | 1.90  | 1.85  | 1.80  | 1.75  | 1.69     |
| 27                   | 4.21  | 3.35  | 2.96  | 2.73  | 2.57  | 2.46  | 2.37  | 2.31  | 2.25  | 2.20  | 2.13  | 2.06  | 1.97  | 1.93  | 1.88  | 1.84  | 1.79  | 1.75  | 1.67     |
| 28                   | 4.20  | 3.34  | 2.95  | 2.71  | 2.56  | 2.45  | 2.36  | 2.29  | 2.24  | 2.19  | 2.12  | 2.04  | 1.96  | 1.91  | 1.87  | 1.82  | 1.77  | 1.71  | 1.65     |
| 29                   | 4.18  | 3.33  | 2.93  | 2.70  | 2.55  | 2.43  | 2.35  | 2.28  | 2.22  | 2.18  | 2.10  | 2.03  | 1.94  | 1.90  | 1.85  | 1.81  | 1.75  | 1.70  | 1.64     |
| 30                   | 4.17  | 3.32  | 2.92  | 2.69  | 2.53  | 2.42  | 2.33  | 2.27  | 2.21  | 2.16  | 2.09  | 2.01  | 1.93  | 1.89  | 1.84  | 1.79  | 1.74  | 1.68  | 1.62     |
| 40                   | 4.08  | 3.23  | 2.84  | 2.61  | 2.45  | 2.34  | 2.25  | 2.18  | 2.12  | 2.08  | 2.00  | 1.92  | 1.84  | 1.79  | 1.74  | 1.69  | 1.64  | 1.58  | 1.51     |
| 60                   | 4.00  | 3.15  | 2.76  | 2.53  | 2.37  | 2.25  | 2.17  | 2.10  | 2.04  | 1.99  | 1.92  | 1.84  | 1.75  | 1.70  | 1.65  | 1.59  | 1.53  | 1.47  | 1.39     |
| 120                  | 3.92  | 3.07  | 2.68  | 2.45  | 2.29  | 2.17  | 2.09  | 2.02  | 1.96  | 1.91  | 1.83  | 1.75  | 1.66  | 1.61  | 1.55  | 1.50  | 1.43  | 1.35  | 1.25     |
| $\infty$             | 3.84  | 3.00  | 2.60  | 2.37  | 2.21  | 2.10  | 2.01  | 1.94  | 1.88  | 1.83  | 1.75  | 1.67  | 1.57  | 1.52  | 1.46  | 1.39  | 1.32  | 1.22  | 1.00     |

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TABLES

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TABLE A-5 (Continued). PERCENTILES OF THE F DISTRIBUTION

 $F_{.975}(n_1, n_2)$  $n_1$  = degrees of freedom for numerator

| $n_2$    | 1     | 2     | 3     | 4     | 5     | 6     | 7     | 8     | 9     | 10    | 12    | 15    | 20    | 24    | 30    | 40    | 60    | 120   | $\infty$ |
|----------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| 1        | 6.78  | 799.5 | 864.2 | 899.6 | 921.8 | 937.1 | 948.2 | 956.7 | 963.3 | 968.6 | 976.7 | 984.9 | 993.1 | 997.2 | 1001  | 1006  | 1010  | 1014  | 1018     |
| 2        | 38.51 | 39.00 | 39.17 | 39.25 | 39.30 | 39.33 | 39.36 | 39.37 | 39.39 | 39.40 | 39.41 | 39.43 | 39.45 | 39.46 | 39.46 | 39.47 | 39.48 | 39.49 | 39.50    |
| 3        | 17.44 | 16.04 | 15.44 | 15.10 | 14.88 | 14.73 | 14.62 | 14.54 | 14.47 | 14.42 | 14.34 | 14.25 | 14.17 | 14.12 | 14.08 | 14.04 | 13.99 | 13.95 | 13.90    |
| 4        | 12.22 | 10.65 | 9.98  | 9.60  | 9.36  | 9.20  | 9.07  | 8.98  | 8.90  | 8.84  | 8.75  | 8.66  | 8.56  | 8.51  | 8.46  | 8.41  | 8.36  | 8.31  | 8.26     |
| 5        | 10.01 | 8.43  | 7.76  | 7.39  | 7.15  | 6.98  | 6.85  | 6.76  | 6.68  | 6.62  | 6.52  | 6.43  | 6.33  | 6.28  | 6.23  | 6.18  | 6.12  | 6.07  | 6.02     |
| 6        | 8.81  | 7.26  | 6.60  | 6.23  | 5.99  | 5.82  | 5.70  | 5.60  | 5.52  | 5.46  | 5.37  | 5.27  | 5.17  | 5.12  | 5.07  | 5.01  | 4.96  | 4.90  | 4.85     |
| 7        | 8.07  | 6.54  | 5.89  | 5.52  | 5.29  | 5.12  | 4.99  | 4.90  | 4.82  | 4.76  | 4.67  | 4.57  | 4.47  | 4.42  | 4.36  | 4.31  | 4.25  | 4.20  | 4.14     |
| 8        | 7.57  | 6.06  | 5.42  | 5.05  | 4.82  | 4.65  | 4.53  | 4.43  | 4.36  | 4.30  | 4.20  | 4.10  | 4.00  | 3.95  | 3.89  | 3.84  | 3.78  | 3.73  | 3.67     |
| 9        | 7.21  | 5.71  | 5.08  | 4.72  | 4.48  | 4.32  | 4.20  | 4.10  | 4.03  | 3.96  | 3.87  | 3.77  | 3.67  | 3.61  | 3.56  | 3.51  | 3.45  | 3.39  | 3.33     |
| 10       | 6.94  | 5.46  | 4.83  | 4.47  | 4.24  | 4.07  | 3.95  | 3.85  | 3.78  | 3.72  | 3.62  | 3.52  | 3.42  | 3.37  | 3.31  | 3.26  | 3.20  | 3.14  | 3.08     |
| 11       | 6.72  | 5.26  | 4.63  | 4.28  | 4.04  | 3.88  | 3.76  | 3.66  | 3.59  | 3.53  | 3.43  | 3.33  | 3.23  | 3.17  | 3.12  | 3.06  | 3.00  | 2.94  | 2.88     |
| 12       | 6.55  | 5.10  | 4.47  | 4.12  | 3.89  | 3.73  | 3.61  | 3.51  | 3.44  | 3.37  | 3.28  | 3.18  | 3.07  | 3.02  | 2.96  | 2.91  | 2.85  | 2.79  | 2.72     |
| 13       | 6.41  | 4.97  | 4.35  | 4.00  | 3.77  | 3.60  | 3.48  | 3.39  | 3.31  | 3.25  | 3.15  | 3.05  | 2.95  | 2.89  | 2.84  | 2.78  | 2.72  | 2.66  | 2.60     |
| 14       | 6.30  | 4.86  | 4.24  | 3.89  | 3.66  | 3.50  | 3.38  | 3.29  | 3.21  | 3.15  | 3.05  | 2.95  | 2.84  | 2.79  | 2.73  | 2.67  | 2.61  | 2.55  | 2.49     |
| 15       | 6.20  | 4.77  | 4.15  | 3.80  | 3.58  | 3.41  | 3.29  | 3.20  | 3.12  | 3.06  | 2.96  | 2.86  | 2.76  | 2.70  | 2.64  | 2.59  | 2.52  | 2.46  | 2.40     |
| 16       | 6.12  | 4.69  | 4.08  | 3.73  | 3.50  | 3.34  | 3.22  | 3.12  | 3.05  | 2.99  | 2.89  | 2.79  | 2.68  | 2.63  | 2.57  | 2.51  | 2.45  | 2.38  | 2.32     |
| 17       | 6.04  | 4.62  | 4.01  | 3.66  | 3.44  | 3.28  | 3.16  | 3.06  | 2.98  | 2.92  | 2.82  | 2.72  | 2.62  | 2.56  | 2.50  | 2.44  | 2.38  | 2.32  | 2.25     |
| 18       | 5.98  | 4.56  | 3.95  | 3.61  | 3.38  | 3.22  | 3.10  | 3.01  | 2.93  | 2.87  | 2.77  | 2.67  | 2.56  | 2.50  | 2.44  | 2.38  | 2.32  | 2.26  | 2.19     |
| 19       | 5.92  | 4.51  | 3.90  | 3.56  | 3.33  | 3.17  | 3.05  | 2.96  | 2.88  | 2.82  | 2.72  | 2.62  | 2.51  | 2.45  | 2.39  | 2.33  | 2.27  | 2.20  | 2.13     |
| 20       | 5.87  | 4.46  | 3.86  | 3.51  | 3.29  | 3.13  | 3.01  | 2.91  | 2.84  | 2.77  | 2.68  | 2.57  | 2.46  | 2.41  | 2.35  | 2.29  | 2.22  | 2.16  | 2.09     |
| 21       | 5.83  | 4.42  | 3.82  | 3.48  | 3.25  | 3.09  | 2.97  | 2.87  | 2.80  | 2.73  | 2.64  | 2.53  | 2.42  | 2.37  | 2.31  | 2.25  | 2.18  | 2.11  | 2.04     |
| 22       | 5.79  | 4.38  | 3.78  | 3.44  | 3.22  | 3.05  | 2.93  | 2.84  | 2.76  | 2.70  | 2.60  | 2.50  | 2.39  | 2.33  | 2.27  | 2.21  | 2.14  | 2.08  | 2.00     |
| 23       | 5.75  | 4.35  | 3.75  | 3.41  | 3.18  | 3.02  | 2.90  | 2.81  | 2.73  | 2.67  | 2.57  | 2.47  | 2.36  | 2.30  | 2.24  | 2.18  | 2.11  | 2.04  | 1.97     |
| 24       | 5.72  | 4.32  | 3.72  | 3.38  | 3.15  | 2.99  | 2.87  | 2.78  | 2.70  | 2.64  | 2.54  | 2.44  | 2.33  | 2.27  | 2.21  | 2.15  | 2.08  | 2.01  | 1.94     |
| 25       | 5.69  | 4.29  | 3.69  | 3.35  | 3.13  | 2.97  | 2.85  | 2.75  | 2.68  | 2.61  | 2.51  | 2.41  | 2.30  | 2.24  | 2.18  | 2.12  | 2.05  | 1.98  | 1.91     |
| 26       | 5.66  | 4.27  | 3.67  | 3.33  | 3.10  | 2.94  | 2.82  | 2.73  | 2.65  | 2.59  | 2.49  | 2.39  | 2.28  | 2.22  | 2.16  | 2.09  | 2.03  | 1.95  | 1.88     |
| 27       | 5.63  | 4.24  | 3.65  | 3.31  | 3.08  | 2.92  | 2.80  | 2.71  | 2.63  | 2.57  | 2.47  | 2.36  | 2.25  | 2.19  | 2.13  | 2.07  | 2.00  | 1.93  | 1.85     |
| 28       | 5.61  | 4.22  | 3.63  | 3.29  | 3.06  | 2.90  | 2.78  | 2.69  | 2.61  | 2.55  | 2.45  | 2.34  | 2.23  | 2.17  | 2.11  | 2.05  | 1.98  | 1.91  | 1.83     |
| 29       | 5.59  | 4.20  | 3.61  | 3.27  | 3.04  | 2.88  | 2.76  | 2.67  | 2.59  | 2.53  | 2.43  | 2.32  | 2.21  | 2.15  | 2.09  | 2.03  | 1.96  | 1.89  | 1.81     |
| 30       | 5.57  | 4.18  | 3.59  | 3.25  | 3.03  | 2.87  | 2.75  | 2.65  | 2.57  | 2.51  | 2.41  | 2.31  | 2.20  | 2.14  | 2.07  | 2.01  | 1.94  | 1.87  | 1.79     |
| 40       | 5.42  | 4.05  | 3.46  | 3.13  | 2.90  | 2.74  | 2.62  | 2.53  | 2.45  | 2.39  | 2.29  | 2.18  | 2.07  | 2.01  | 1.94  | 1.88  | 1.80  | 1.72  | 1.64     |
| 60       | 5.29  | 3.93  | 3.34  | 3.01  | 2.79  | 2.63  | 2.51  | 2.41  | 2.33  | 2.27  | 2.17  | 2.06  | 1.94  | 1.88  | 1.82  | 1.74  | 1.67  | 1.58  | 1.48     |
| 120      | 5.15  | 3.80  | 3.23  | 2.89  | 2.67  | 2.52  | 2.39  | 2.30  | 2.22  | 2.16  | 2.05  | 1.94  | 1.82  | 1.76  | 1.69  | 1.61  | 1.53  | 1.43  | 1.31     |
| $\infty$ | 5.02  | 3.69  | 3.12  | 2.79  | 2.57  | 2.41  | 2.29  | 2.19  | 2.11  | 2.05  | 1.94  | 1.83  | 1.71  | 1.64  | 1.57  | 1.48  | 1.39  | 1.27  | 1.00     |

 $n_2$  = degrees of freedom for denominator



$n_1$  = degrees of freedom for denominator

| $n_1 \backslash n_2$ | 1     | 2     | 3     | 4     | 5     | 6     | 7     | 8     | 9     | 10    | 12    | 15    | 20    | 24    | 30    | 40    | 60    | 120   | $\infty$ |
|----------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| 1                    | 16.26 | 13.27 | 12.06 | 11.39 | 10.97 | 10.67 | 10.46 | 10.29 | 10.16 | 10.05 | 9.89  | 9.72  | 9.55  | 9.47  | 9.38  | 9.29  | 9.21  | 9.13  | 9.05     |
| 2                    | 18.00 | 14.85 | 13.82 | 13.00 | 12.50 | 12.19 | 11.94 | 11.73 | 11.55 | 11.40 | 11.22 | 11.05 | 10.88 | 10.71 | 10.54 | 10.37 | 10.21 | 10.05 | 9.89     |
| 3                    | 19.16 | 15.52 | 14.39 | 13.56 | 13.05 | 12.73 | 12.47 | 12.25 | 12.06 | 11.90 | 11.72 | 11.55 | 11.38 | 11.21 | 11.04 | 10.87 | 10.71 | 10.54 | 10.37    |
| 4                    | 20.00 | 16.00 | 14.87 | 14.03 | 13.51 | 13.19 | 12.92 | 12.69 | 12.49 | 12.32 | 12.14 | 11.97 | 11.80 | 11.63 | 11.46 | 11.29 | 11.12 | 10.95 | 10.78    |
| 5                    | 20.70 | 16.46 | 15.33 | 14.48 | 13.95 | 13.63 | 13.36 | 13.12 | 12.91 | 12.73 | 12.55 | 12.37 | 12.20 | 12.02 | 11.85 | 11.67 | 11.50 | 11.32 | 11.15    |
| 6                    | 21.20 | 16.82 | 15.68 | 14.82 | 14.29 | 13.96 | 13.68 | 13.43 | 13.21 | 13.02 | 12.83 | 12.65 | 12.47 | 12.29 | 12.11 | 11.93 | 11.75 | 11.57 | 11.39    |
| 7                    | 21.56 | 17.04 | 15.89 | 15.02 | 14.48 | 14.15 | 13.86 | 13.60 | 13.37 | 13.17 | 12.98 | 12.79 | 12.60 | 12.41 | 12.22 | 12.03 | 11.85 | 11.66 | 11.47    |
| 8                    | 21.83 | 17.21 | 16.05 | 15.17 | 14.62 | 14.28 | 13.98 | 13.71 | 13.47 | 13.25 | 13.04 | 12.84 | 12.64 | 12.44 | 12.24 | 12.04 | 11.84 | 11.65 | 11.45    |
| 9                    | 22.04 | 17.36 | 16.19 | 15.30 | 14.74 | 14.39 | 14.08 | 13.79 | 13.54 | 13.31 | 13.09 | 12.88 | 12.67 | 12.46 | 12.25 | 12.04 | 11.83 | 11.63 | 11.42    |
| 10                   | 22.21 | 17.49 | 16.31 | 15.41 | 14.84 | 14.48 | 14.16 | 13.86 | 13.60 | 13.36 | 13.13 | 12.91 | 12.69 | 12.47 | 12.25 | 12.03 | 11.81 | 11.59 | 11.37    |
| 12                   | 22.47 | 17.65 | 16.46 | 15.55 | 14.97 | 14.60 | 14.27 | 13.95 | 13.67 | 13.42 | 13.17 | 12.94 | 12.71 | 12.48 | 12.25 | 12.02 | 11.79 | 11.56 | 11.32    |
| 15                   | 22.73 | 17.81 | 16.61 | 15.69 | 15.10 | 14.72 | 14.38 | 14.04 | 13.75 | 13.49 | 13.23 | 13.00 | 12.78 | 12.55 | 12.32 | 12.09 | 11.86 | 11.63 | 11.39    |
| 20                   | 23.00 | 18.00 | 16.78 | 15.85 | 15.25 | 14.86 | 14.51 | 14.15 | 13.85 | 13.58 | 13.31 | 13.04 | 12.79 | 12.56 | 12.33 | 12.10 | 11.87 | 11.64 | 11.40    |
| 24                   | 23.18 | 18.14 | 16.92 | 15.98 | 15.37 | 14.97 | 14.61 | 14.24 | 13.93 | 13.65 | 13.37 | 13.08 | 12.79 | 12.50 | 12.21 | 11.92 | 11.63 | 11.34 | 11.05    |
| 30                   | 23.33 | 18.27 | 17.05 | 16.10 | 15.48 | 15.07 | 14.70 | 14.32 | 14.00 | 13.71 | 13.42 | 13.12 | 12.82 | 12.52 | 12.22 | 11.92 | 11.62 | 11.31 | 11.00    |
| 40                   | 23.47 | 18.38 | 17.15 | 16.19 | 15.56 | 15.14 | 14.75 | 14.36 | 14.03 | 13.74 | 13.44 | 13.14 | 12.84 | 12.54 | 12.24 | 11.94 | 11.64 | 11.33 | 11.02    |
| 60                   | 23.61 | 18.49 | 17.25 | 16.28 | 15.64 | 15.21 | 14.81 | 14.41 | 14.00 | 13.68 | 13.36 | 13.04 | 12.72 | 12.40 | 12.07 | 11.75 | 11.42 | 11.09 | 10.75    |
| 120                  | 23.75 | 18.59 | 17.34 | 16.36 | 15.71 | 15.27 | 14.86 | 14.45 | 14.03 | 13.70 | 13.37 | 13.04 | 12.71 | 12.38 | 12.04 | 11.71 | 11.37 | 11.03 | 10.68    |
| $\infty$             | 23.86 | 18.68 | 17.42 | 16.43 | 15.77 | 15.32 | 14.90 | 14.48 | 14.05 | 13.72 | 13.38 | 13.04 | 12.70 | 12.36 | 12.01 | 11.67 | 11.32 | 10.97 | 10.61    |

$F_{.99}(n_1, n_2)$   
 $n_1$  = degrees of freedom for numerator

 $n_2$  = degrees of freedom for numerator $F_{.99}(n_1, n_2)$ 

TABLE A-5 (Continued). PERCENTILES OF THE F DISTRIBUTION

## TABLES

## TABLES

TABLE A-6. FACTORS FOR TWO-SIDED TOLERANCE LIMITS FOR NORMAL DISTRIBUTIONS

Factors  $K$  such that the probability is  $\gamma$  that at least a proportion  $P$  of the distribution will be included between  $\bar{X} \pm Ks$ , where  $\bar{X}$  and  $s$  are estimates of the mean and the standard deviation computed from a sample size of  $n$ .

| P<br>n | $\gamma = 0.75$ |       |       |       |        | $\gamma = 0.90$ |        |        |        |        |
|--------|-----------------|-------|-------|-------|--------|-----------------|--------|--------|--------|--------|
|        | 0.75            | 0.90  | 0.95  | 0.99  | 0.999  | 0.75            | 0.90   | 0.95   | 0.99   | 0.999  |
| 2      | 4.498           | 6.301 | 7.414 | 9.531 | 11.920 | 11.407          | 15.978 | 18.800 | 24.167 | 30.227 |
| 3      | 2.501           | 3.538 | 4.187 | 5.431 | 6.844  | 4.132           | 5.847  | 6.919  | 8.974  | 11.309 |
| 4      | 2.035           | 2.892 | 3.431 | 4.471 | 5.657  | 2.932           | 4.166  | 4.943  | 6.440  | 8.149  |
| 5      | 1.825           | 2.599 | 3.088 | 4.033 | 5.117  | 2.454           | 3.494  | 4.152  | 5.423  | 6.879  |
| 6      | 1.704           | 2.429 | 2.889 | 3.779 | 4.802  | 2.196           | 3.131  | 3.723  | 4.870  | 6.188  |
| 7      | 1.624           | 2.318 | 2.757 | 3.611 | 4.593  | 2.034           | 2.902  | 3.452  | 4.521  | 5.750  |
| 8      | 1.568           | 2.238 | 2.663 | 3.491 | 4.444  | 1.921           | 2.743  | 3.264  | 4.278  | 5.446  |
| 9      | 1.525           | 2.178 | 2.593 | 3.400 | 4.330  | 1.839           | 2.626  | 3.125  | 4.098  | 5.220  |
| 10     | 1.492           | 2.131 | 2.537 | 3.328 | 4.241  | 1.775           | 2.535  | 3.018  | 3.959  | 5.046  |
| 11     | 1.465           | 2.093 | 2.493 | 3.271 | 4.169  | 1.724           | 2.463  | 2.933  | 3.849  | 4.906  |
| 12     | 1.443           | 2.062 | 2.456 | 3.223 | 4.110  | 1.683           | 2.404  | 2.863  | 3.758  | 4.792  |
| 13     | 1.425           | 2.036 | 2.424 | 3.183 | 4.059  | 1.648           | 2.355  | 2.805  | 3.682  | 4.697  |
| 14     | 1.409           | 2.013 | 2.398 | 3.148 | 4.016  | 1.619           | 2.314  | 2.756  | 3.618  | 4.615  |
| 15     | 1.395           | 1.994 | 2.375 | 3.118 | 3.979  | 1.594           | 2.278  | 2.713  | 3.562  | 4.545  |
| 16     | 1.383           | 1.977 | 2.355 | 3.092 | 3.946  | 1.572           | 2.246  | 2.676  | 3.514  | 4.484  |
| 17     | 1.372           | 1.962 | 2.337 | 3.069 | 3.917  | 1.552           | 2.219  | 2.643  | 3.471  | 4.430  |
| 18     | 1.363           | 1.948 | 2.321 | 3.048 | 3.891  | 1.535           | 2.194  | 2.614  | 3.433  | 4.382  |
| 19     | 1.355           | 1.936 | 2.307 | 3.030 | 3.867  | 1.520           | 2.172  | 2.588  | 3.399  | 4.339  |
| 20     | 1.347           | 1.925 | 2.294 | 3.013 | 3.846  | 1.506           | 2.152  | 2.564  | 3.368  | 4.300  |
| 21     | 1.340           | 1.915 | 2.282 | 2.998 | 3.827  | 1.493           | 2.135  | 2.543  | 3.340  | 4.264  |
| 22     | 1.334           | 1.906 | 2.271 | 2.984 | 3.809  | 1.482           | 2.118  | 2.524  | 3.315  | 4.232  |
| 23     | 1.328           | 1.898 | 2.261 | 2.971 | 3.793  | 1.471           | 2.103  | 2.506  | 3.292  | 4.203  |
| 24     | 1.322           | 1.891 | 2.252 | 2.959 | 3.778  | 1.462           | 2.089  | 2.489  | 3.270  | 4.176  |
| 25     | 1.317           | 1.883 | 2.244 | 2.948 | 3.764  | 1.453           | 2.077  | 2.474  | 3.251  | 4.151  |
| 26     | 1.313           | 1.877 | 2.236 | 2.938 | 3.751  | 1.444           | 2.065  | 2.460  | 3.232  | 4.127  |
| 27     | 1.309           | 1.871 | 2.229 | 2.929 | 3.740  | 1.437           | 2.054  | 2.447  | 3.215  | 4.106  |

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## TABLES

TABLE A-6 (Continued). FACTORS FOR TWO-SIDED TOLERANCE LIMITS FOR NORMAL DISTRIBUTIONS

| P<br>n | $\gamma = 0.95$ |        |        |        |        | $\gamma = 0.99$ |         |         |         |         |
|--------|-----------------|--------|--------|--------|--------|-----------------|---------|---------|---------|---------|
|        | 0.75            | 0.90   | 0.95   | 0.99   | 0.999  | 0.75            | 0.90    | 0.95    | 0.99    | 0.999   |
| 2      | 22.858          | 32.019 | 37.674 | 48.430 | 60.573 | 114.363         | 160.193 | 188.491 | 242.300 | 303.054 |
| 3      | 5.922           | 8.380  | 9.916  | 12.861 | 16.208 | 13.378          | 18.930  | 22.401  | 29.055  | 36.616  |
| 4      | 3.779           | 5.369  | 6.370  | 8.299  | 10.502 | 6.614           | 9.398   | 11.150  | 14.527  | 18.383  |
| 5      | 3.002           | 4.275  | 5.079  | 6.634  | 8.415  | 4.643           | 6.612   | 7.855   | 10.260  | 13.015  |
| 6      | 2.604           | 3.712  | 4.414  | 5.775  | 7.337  | 3.743           | 5.337   | 6.345   | 8.301   | 10.548  |
| 7      | 2.361           | 3.369  | 4.007  | 5.248  | 6.676  | 3.233           | 4.613   | 5.488   | 7.187   | 9.142   |
| 8      | 2.197           | 3.136  | 3.732  | 4.891  | 6.226  | 2.905           | 4.147   | 4.936   | 6.468   | 8.234   |
| 9      | 2.078           | 2.967  | 3.532  | 4.631  | 5.899  | 2.677           | 3.822   | 4.550   | 5.966   | 7.600   |
| 10     | 1.987           | 2.839  | 3.379  | 4.433  | 5.649  | 2.508           | 3.582   | 4.265   | 5.594   | 7.129   |
| 11     | 1.916           | 2.737  | 3.259  | 4.277  | 5.452  | 2.378           | 3.397   | 4.045   | 5.308   | 6.766   |
| 12     | 1.858           | 2.655  | 3.162  | 4.150  | 5.291  | 2.274           | 3.250   | 3.870   | 5.079   | 6.477   |
| 13     | 1.810           | 2.587  | 3.081  | 4.044  | 5.158  | 2.190           | 3.130   | 3.727   | 4.893   | 6.240   |
| 14     | 1.770           | 2.529  | 3.012  | 3.955  | 5.045  | 2.120           | 3.029   | 3.608   | 4.737   | 6.043   |
| 15     | 1.735           | 2.480  | 2.954  | 3.878  | 4.949  | 2.060           | 2.945   | 3.507   | 4.605   | 5.876   |
| 16     | 1.705           | 2.437  | 2.903  | 3.812  | 4.865  | 2.009           | 2.872   | 3.421   | 4.492   | 5.732   |
| 17     | 1.679           | 2.400  | 2.858  | 3.754  | 4.791  | 1.965           | 2.808   | 3.345   | 4.393   | 5.607   |
| 18     | 1.655           | 2.366  | 2.819  | 3.702  | 4.725  | 1.926           | 2.753   | 3.279   | 4.307   | 5.497   |
| 19     | 1.635           | 2.337  | 2.784  | 3.656  | 4.667  | 1.891           | 2.703   | 3.221   | 4.230   | 5.399   |
| 20     | 1.616           | 2.310  | 2.752  | 3.615  | 4.614  | 1.860           | 2.659   | 3.168   | 4.161   | 5.312   |
| 21     | 1.599           | 2.286  | 2.723  | 3.577  | 4.567  | 1.833           | 2.620   | 3.121   | 4.100   | 5.234   |
| 22     | 1.584           | 2.264  | 2.697  | 3.543  | 4.523  | 1.808           | 2.584   | 3.078   | 4.044   | 5.163   |
| 23     | 1.570           | 2.244  | 2.673  | 3.512  | 4.484  | 1.785           | 2.551   | 3.040   | 3.993   | 5.098   |
| 24     | 1.557           | 2.225  | 2.651  | 3.483  | 4.447  | 1.764           | 2.522   | 3.004   | 3.947   | 5.039   |
| 25     | 1.545           | 2.208  | 2.631  | 3.457  | 4.413  | 1.745           | 2.494   | 2.972   | 3.904   | 4.985   |
| 26     | 1.534           | 2.193  | 2.612  | 3.432  | 4.382  | 1.727           | 2.469   | 2.941   | 3.865   | 4.935   |
| 27     | 1.523           | 2.178  | 2.595  | 3.409  | 4.353  | 1.711           | 2.446   | 2.914   | 3.828   | 4.888   |

## TABLES

TABLE A-6 (Continued). FACTORS FOR TWO-SIDED TOLERANCE LIMITS FOR NORMAL DISTRIBUTIONS

| P<br>n   | $\gamma = 0.75$ |       |       |       |       | $\gamma = 0.90$ |       |       |       |       |
|----------|-----------------|-------|-------|-------|-------|-----------------|-------|-------|-------|-------|
|          | 0.75            | 0.90  | 0.95  | 0.99  | 0.999 | 0.75            | 0.90  | 0.95  | 0.99  | 0.999 |
| 30       | 1.297           | 1.855 | 2.210 | 2.904 | 3.708 | 1.417           | 2.025 | 2.413 | 3.170 | 4.049 |
| 35       | 1.283           | 1.834 | 2.185 | 2.871 | 3.667 | 1.390           | 1.988 | 2.368 | 3.112 | 3.974 |
| 40       | 1.271           | 1.818 | 2.166 | 2.846 | 3.635 | 1.370           | 1.959 | 2.334 | 3.066 | 3.917 |
| 45       | 1.262           | 1.805 | 2.150 | 2.826 | 3.609 | 1.354           | 1.935 | 2.306 | 3.030 | 3.871 |
| 50       | 1.255           | 1.794 | 2.138 | 2.809 | 3.588 | 1.340           | 1.916 | 2.284 | 3.001 | 3.833 |
| 55       | 1.249           | 1.785 | 2.127 | 2.795 | 3.571 | 1.329           | 1.901 | 2.265 | 2.976 | 3.801 |
| 60       | 1.243           | 1.778 | 2.118 | 2.784 | 3.556 | 1.320           | 1.887 | 2.248 | 2.955 | 3.774 |
| 65       | 1.239           | 1.771 | 2.110 | 2.773 | 3.543 | 1.312           | 1.875 | 2.235 | 2.937 | 3.751 |
| 70       | 1.235           | 1.765 | 2.104 | 2.764 | 3.531 | 1.304           | 1.865 | 2.222 | 2.920 | 3.730 |
| 75       | 1.231           | 1.760 | 2.098 | 2.757 | 3.521 | 1.298           | 1.856 | 2.211 | 2.906 | 3.712 |
| 80       | 1.228           | 1.756 | 2.092 | 2.749 | 3.512 | 1.292           | 1.848 | 2.202 | 2.894 | 3.696 |
| 85       | 1.225           | 1.752 | 2.087 | 2.743 | 3.504 | 1.287           | 1.841 | 2.193 | 2.882 | 3.682 |
| 90       | 1.223           | 1.748 | 2.083 | 2.737 | 3.497 | 1.283           | 1.834 | 2.185 | 2.872 | 3.669 |
| 95       | 1.220           | 1.745 | 2.079 | 2.732 | 3.490 | 1.278           | 1.828 | 2.178 | 2.863 | 3.657 |
| 100      | 1.218           | 1.742 | 2.075 | 2.727 | 3.484 | 1.275           | 1.822 | 2.172 | 2.854 | 3.646 |
| 110      | 1.214           | 1.736 | 2.069 | 2.719 | 3.473 | 1.268           | 1.813 | 2.160 | 2.839 | 3.626 |
| 120      | 1.211           | 1.732 | 2.063 | 2.712 | 3.464 | 1.262           | 1.804 | 2.150 | 2.826 | 3.610 |
| 130      | 1.208           | 1.728 | 2.059 | 2.705 | 3.456 | 1.257           | 1.797 | 2.141 | 2.814 | 3.595 |
| 140      | 1.206           | 1.724 | 2.054 | 2.700 | 3.449 | 1.252           | 1.791 | 2.134 | 2.804 | 3.582 |
| 150      | 1.204           | 1.721 | 2.051 | 2.695 | 3.443 | 1.248           | 1.785 | 2.127 | 2.795 | 3.571 |
| 160      | 1.202           | 1.718 | 2.047 | 2.691 | 3.437 | 1.245           | 1.780 | 2.121 | 2.787 | 3.561 |
| 170      | 1.200           | 1.716 | 2.044 | 2.687 | 3.432 | 1.242           | 1.775 | 2.116 | 2.780 | 3.552 |
| 180      | 1.198           | 1.713 | 2.042 | 2.683 | 3.427 | 1.239           | 1.771 | 2.111 | 2.774 | 3.543 |
| 190      | 1.197           | 1.711 | 2.039 | 2.680 | 3.423 | 1.236           | 1.767 | 2.106 | 2.768 | 3.536 |
| 200      | 1.195           | 1.709 | 2.037 | 2.677 | 3.419 | 1.234           | 1.764 | 2.102 | 2.762 | 3.529 |
| 250      | 1.190           | 1.702 | 2.028 | 2.665 | 3.404 | 1.224           | 1.750 | 2.085 | 2.740 | 3.501 |
| 300      | 1.186           | 1.696 | 2.021 | 2.656 | 3.393 | 1.217           | 1.740 | 2.073 | 2.725 | 3.481 |
| 400      | 1.181           | 1.688 | 2.012 | 2.644 | 3.378 | 1.207           | 1.726 | 2.057 | 2.703 | 3.453 |
| 500      | 1.177           | 1.683 | 2.006 | 2.636 | 3.368 | 1.201           | 1.717 | 2.046 | 2.689 | 3.434 |
| 600      | 1.175           | 1.680 | 2.002 | 2.631 | 3.360 | 1.196           | 1.710 | 2.038 | 2.678 | 3.421 |
| 700      | 1.173           | 1.677 | 1.998 | 2.626 | 3.355 | 1.192           | 1.705 | 2.032 | 2.670 | 3.411 |
| 800      | 1.171           | 1.675 | 1.996 | 2.623 | 3.350 | 1.189           | 1.701 | 2.027 | 2.663 | 3.402 |
| 900      | 1.170           | 1.673 | 1.993 | 2.620 | 3.347 | 1.187           | 1.697 | 2.023 | 2.658 | 3.396 |
| 1000     | 1.169           | 1.671 | 1.992 | 2.617 | 3.344 | 1.185           | 1.695 | 2.019 | 2.654 | 3.390 |
| $\infty$ | 1.150           | 1.645 | 1.960 | 2.576 | 3.291 | 1.150           | 1.645 | 1.960 | 2.576 | 3.291 |

## TABLES

TABLE A-6 (Continued). FACTORS FOR TWO-SIDED TOLERANCE LIMITS FOR NORMAL DISTRIBUTIONS

| $\frac{P}{n}$ | $\gamma = 0.95$ |       |       |       |       | $\gamma = 0.99$ |       |       |       |       |
|---------------|-----------------|-------|-------|-------|-------|-----------------|-------|-------|-------|-------|
|               | 0.75            | 0.90  | 0.95  | 0.99  | 0.999 | 0.75            | 0.90  | 0.95  | 0.99  | 0.999 |
| 30            | 1.497           | 2.140 | 2.549 | 3.350 | 4.278 | 1.668           | 2.385 | 2.841 | 3.733 | 4.768 |
| 35            | 1.462           | 2.090 | 2.490 | 3.272 | 4.179 | 1.613           | 2.306 | 2.748 | 3.611 | 4.611 |
| 40            | 1.435           | 2.052 | 2.445 | 3.213 | 4.104 | 1.571           | 2.247 | 2.677 | 3.518 | 4.493 |
| 45            | 1.414           | 2.021 | 2.408 | 3.165 | 4.042 | 1.539           | 2.200 | 2.621 | 3.444 | 4.399 |
| 50            | 1.396           | 1.996 | 2.379 | 3.126 | 3.993 | 1.512           | 2.162 | 2.576 | 3.385 | 4.323 |
| 55            | 1.382           | 1.976 | 2.354 | 3.094 | 3.951 | 1.490           | 2.130 | 2.538 | 3.335 | 4.260 |
| 60            | 1.369           | 1.958 | 2.333 | 3.066 | 3.916 | 1.471           | 2.103 | 2.506 | 3.293 | 4.206 |
| 65            | 1.359           | 1.943 | 2.315 | 3.042 | 3.886 | 1.455           | 2.080 | 2.478 | 3.257 | 4.160 |
| 70            | 1.349           | 1.929 | 2.299 | 3.021 | 3.859 | 1.440           | 2.060 | 2.454 | 3.225 | 4.120 |
| 75            | 1.341           | 1.917 | 2.285 | 3.002 | 3.835 | 1.428           | 2.042 | 2.433 | 3.197 | 4.084 |
| 80            | 1.334           | 1.907 | 2.272 | 2.986 | 3.814 | 1.417           | 2.026 | 2.414 | 3.173 | 4.053 |
| 85            | 1.327           | 1.897 | 2.261 | 2.971 | 3.795 | 1.407           | 2.012 | 2.397 | 3.150 | 4.024 |
| 90            | 1.321           | 1.889 | 2.251 | 2.958 | 3.778 | 1.398           | 1.999 | 2.382 | 3.130 | 3.999 |
| 95            | 1.315           | 1.881 | 2.241 | 2.945 | 3.763 | 1.390           | 1.987 | 2.368 | 3.112 | 3.976 |
| 100           | 1.311           | 1.874 | 2.233 | 2.934 | 3.748 | 1.383           | 1.977 | 2.355 | 3.096 | 3.954 |
| 110           | 1.302           | 1.861 | 2.218 | 2.915 | 3.723 | 1.369           | 1.958 | 2.333 | 3.066 | 3.917 |
| 120           | 1.294           | 1.850 | 2.205 | 2.898 | 3.702 | 1.358           | 1.942 | 2.314 | 3.041 | 3.885 |
| 130           | 1.288           | 1.841 | 2.194 | 2.883 | 3.683 | 1.349           | 1.928 | 2.298 | 3.019 | 3.857 |
| 140           | 1.282           | 1.833 | 2.184 | 2.870 | 3.666 | 1.340           | 1.916 | 2.283 | 3.000 | 3.833 |
| 150           | 1.277           | 1.825 | 2.175 | 2.859 | 3.652 | 1.332           | 1.905 | 2.270 | 2.983 | 3.811 |
| 160           | 1.272           | 1.819 | 2.167 | 2.848 | 3.638 | 1.326           | 1.896 | 2.259 | 2.968 | 3.792 |
| 170           | 1.268           | 1.813 | 2.160 | 2.839 | 3.627 | 1.320           | 1.887 | 2.248 | 2.955 | 3.774 |
| 180           | 1.264           | 1.808 | 2.154 | 2.831 | 3.616 | 1.314           | 1.879 | 2.239 | 2.942 | 3.759 |
| 190           | 1.261           | 1.803 | 2.148 | 2.823 | 3.606 | 1.309           | 1.872 | 2.230 | 2.931 | 3.744 |
| 200           | 1.258           | 1.798 | 2.143 | 2.816 | 3.597 | 1.304           | 1.865 | 2.222 | 2.921 | 3.731 |
| 250           | 1.245           | 1.780 | 2.121 | 2.788 | 3.561 | 1.286           | 1.839 | 2.191 | 2.880 | 3.678 |
| 300           | 1.236           | 1.767 | 2.106 | 2.767 | 3.535 | 1.273           | 1.820 | 2.169 | 2.850 | 3.641 |
| 400           | 1.223           | 1.749 | 2.084 | 2.739 | 3.499 | 1.255           | 1.794 | 2.138 | 2.809 | 3.589 |
| 500           | 1.215           | 1.737 | 2.070 | 2.721 | 3.475 | 1.243           | 1.777 | 2.117 | 2.783 | 3.555 |
| 600           | 1.209           | 1.729 | 2.060 | 2.707 | 3.458 | 1.234           | 1.764 | 2.102 | 2.763 | 3.530 |
| 700           | 1.204           | 1.722 | 2.052 | 2.697 | 3.445 | 1.227           | 1.755 | 2.091 | 2.748 | 3.511 |
| 800           | 1.201           | 1.717 | 2.046 | 2.688 | 3.434 | 1.222           | 1.747 | 2.082 | 2.736 | 3.495 |
| 900           | 1.198           | 1.712 | 2.040 | 2.682 | 3.426 | 1.218           | 1.741 | 2.075 | 2.726 | 3.483 |
| 1000          | 1.195           | 1.709 | 2.036 | 2.676 | 3.418 | 1.214           | 1.736 | 2.068 | 2.718 | 3.472 |
| $\infty$      | 1.150           | 1.645 | 1.960 | 2.576 | 3.291 | 1.150           | 1.645 | 1.960 | 2.576 | 3.291 |

## TABLES

TABLE A-7. FACTORS FOR ONE-SIDED TOLERANCE LIMITS FOR NORMAL DISTRIBUTIONS

Factors  $K$  such that the probability is  $\gamma$  that at least a proportion  $P$  of the distribution will be less than  $\bar{X} + Ks$  (or greater than  $\bar{X} - Ks$ ), where  $\bar{X}$  and  $s$  are estimates of the mean and the standard deviation computed from a sample size of  $n$ .

| n \ P | $\gamma = 0.75$ |       |       |       |       | $\gamma = 0.90$ |       |       |       |       |
|-------|-----------------|-------|-------|-------|-------|-----------------|-------|-------|-------|-------|
|       | 0.75            | 0.90  | 0.95  | 0.99  | 0.999 | 0.75            | 0.90  | 0.95  | 0.99  | 0.999 |
| 3     | 1.464           | 2.501 | 3.152 | 4.396 | 5.805 | 2.602           | 4.258 | 5.310 | 7.340 | 9.651 |
| 4     | 1.256           | 2.134 | 2.680 | 3.726 | 4.910 | 1.972           | 3.187 | 3.957 | 5.437 | 7.128 |
| 5     | 1.152           | 1.961 | 2.463 | 3.421 | 4.507 | 1.698           | 2.742 | 3.400 | 4.666 | 6.112 |
| 6     | 1.087           | 1.860 | 2.336 | 3.243 | 4.273 | 1.540           | 2.494 | 3.091 | 4.242 | 5.556 |
| 7     | 1.043           | 1.791 | 2.250 | 3.126 | 4.118 | 1.435           | 2.333 | 2.894 | 3.972 | 5.201 |
| 8     | 1.010           | 1.740 | 2.190 | 3.042 | 4.008 | 1.360           | 2.219 | 2.755 | 3.783 | 4.955 |
| 9     | 0.984           | 1.702 | 2.141 | 2.977 | 3.924 | 1.302           | 2.133 | 2.649 | 3.641 | 4.772 |
| 10    | 0.964           | 1.671 | 2.103 | 2.927 | 3.858 | 1.257           | 2.065 | 2.568 | 3.532 | 4.629 |
| 11    | 0.947           | 1.646 | 2.073 | 2.885 | 3.804 | 1.219           | 2.012 | 2.503 | 3.444 | 4.515 |
| 12    | 0.933           | 1.624 | 2.048 | 2.851 | 3.760 | 1.188           | 1.966 | 2.448 | 3.371 | 4.420 |
| 13    | 0.919           | 1.606 | 2.026 | 2.822 | 3.722 | 1.162           | 1.928 | 2.403 | 3.310 | 4.341 |
| 14    | 0.909           | 1.591 | 2.007 | 2.796 | 3.690 | 1.139           | 1.895 | 2.363 | 3.257 | 4.274 |
| 15    | 0.899           | 1.577 | 1.991 | 2.776 | 3.661 | 1.119           | 1.866 | 2.329 | 3.212 | 4.215 |
| 16    | 0.891           | 1.566 | 1.977 | 2.756 | 3.637 | 1.101           | 1.842 | 2.299 | 3.172 | 4.164 |
| 17    | 0.883           | 1.554 | 1.964 | 2.739 | 3.615 | 1.085           | 1.820 | 2.272 | 3.136 | 4.118 |
| 18    | 0.876           | 1.544 | 1.951 | 2.723 | 3.595 | 1.071           | 1.800 | 2.249 | 3.106 | 4.078 |
| 19    | 0.870           | 1.536 | 1.942 | 2.710 | 3.577 | 1.058           | 1.781 | 2.228 | 3.078 | 4.041 |
| 20    | 0.865           | 1.528 | 1.933 | 2.697 | 3.561 | 1.046           | 1.765 | 2.208 | 3.052 | 4.009 |
| 21    | 0.859           | 1.520 | 1.923 | 2.686 | 3.545 | 1.035           | 1.750 | 2.190 | 3.028 | 3.979 |
| 22    | 0.854           | 1.514 | 1.916 | 2.675 | 3.532 | 1.025           | 1.736 | 2.174 | 3.007 | 3.952 |
| 23    | 0.849           | 1.508 | 1.907 | 2.665 | 3.520 | 1.016           | 1.724 | 2.159 | 2.987 | 3.927 |
| 24    | 0.845           | 1.502 | 1.901 | 2.656 | 3.509 | 1.007           | 1.712 | 2.145 | 2.969 | 3.904 |
| 25    | 0.842           | 1.496 | 1.895 | 2.647 | 3.497 | 0.999           | 1.702 | 2.132 | 2.952 | 3.882 |
| 30    | 0.825           | 1.475 | 1.869 | 2.613 | 3.454 | 0.966           | 1.657 | 2.080 | 2.884 | 3.794 |
| 35    | 0.812           | 1.458 | 1.849 | 2.588 | 3.421 | 0.942           | 1.623 | 2.041 | 2.833 | 3.730 |
| 40    | 0.803           | 1.445 | 1.834 | 2.568 | 3.395 | 0.923           | 1.598 | 2.010 | 2.793 | 3.679 |
| 45    | 0.795           | 1.435 | 1.821 | 2.552 | 3.375 | 0.908           | 1.577 | 1.986 | 2.762 | 3.638 |
| 50    | 0.788           | 1.426 | 1.811 | 2.538 | 3.358 | 0.894           | 1.560 | 1.965 | 2.735 | 3.604 |

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## TABLES

TABLE A-7 (Continued). FACTORS FOR ONE-SIDED TOLERANCE LIMITS FOR NORMAL DISTRIBUTIONS

| P<br>n | $\gamma = 0.95$ |       |       |        |        | $\gamma = 0.99$ |       |       |       |       |
|--------|-----------------|-------|-------|--------|--------|-----------------|-------|-------|-------|-------|
|        | 0.75            | 0.90  | 0.95  | 0.99   | 0.999  | 0.75            | 0.90  | 0.95  | 0.99  | 0.999 |
| 3      | 3.804           | 6.158 | 7.655 | 10.552 | 13.857 | —               | —     | —     | —     | —     |
| 4      | 2.619           | 4.163 | 5.145 | 7.042  | 9.215  | —               | —     | —     | —     | —     |
| 5      | 2.149           | 3.407 | 4.202 | 5.741  | 7.501  | —               | —     | —     | —     | —     |
| 6      | 1.895           | 3.006 | 3.707 | 5.062  | 6.612  | 2.849           | 4.408 | 5.409 | 7.334 | 9.540 |
| 7      | 1.732           | 2.755 | 3.399 | 4.641  | 6.061  | 2.490           | 3.856 | 4.730 | 6.411 | 8.348 |
| 8      | 1.617           | 2.582 | 3.188 | 4.353  | 5.686  | 2.252           | 3.496 | 4.287 | 5.811 | 7.566 |
| 9      | 1.532           | 2.454 | 3.031 | 4.143  | 5.414  | 2.085           | 3.242 | 3.971 | 5.389 | 7.014 |
| 10     | 1.465           | 2.355 | 2.911 | 3.981  | 5.203  | 1.954           | 3.048 | 3.739 | 5.075 | 6.603 |
| 11     | 1.411           | 2.275 | 2.815 | 3.852  | 5.036  | 1.854           | 2.897 | 3.557 | 4.828 | 6.284 |
| 12     | 1.366           | 2.210 | 2.736 | 3.747  | 4.900  | 1.771           | 2.773 | 3.410 | 4.633 | 6.032 |
| 13     | 1.329           | 2.155 | 2.670 | 3.659  | 4.787  | 1.702           | 2.677 | 3.290 | 4.472 | 5.826 |
| 14     | 1.296           | 2.108 | 2.614 | 3.585  | 4.690  | 1.645           | 2.592 | 3.189 | 4.336 | 5.651 |
| 15     | 1.268           | 2.068 | 2.566 | 3.520  | 4.607  | 1.596           | 2.521 | 3.102 | 4.224 | 5.507 |
| 16     | 1.242           | 2.032 | 2.523 | 3.463  | 4.534  | 1.553           | 2.458 | 3.028 | 4.124 | 5.374 |
| 17     | 1.220           | 2.001 | 2.486 | 3.415  | 4.471  | 1.514           | 2.405 | 2.962 | 4.038 | 5.268 |
| 18     | 1.200           | 1.974 | 2.453 | 3.370  | 4.415  | 1.481           | 2.357 | 2.906 | 3.961 | 5.167 |
| 19     | 1.183           | 1.949 | 2.423 | 3.331  | 4.364  | 1.450           | 2.315 | 2.855 | 3.893 | 5.078 |
| 20     | 1.167           | 1.926 | 2.396 | 3.295  | 4.319  | 1.424           | 2.275 | 2.807 | 3.832 | 5.003 |
| 21     | 1.152           | 1.905 | 2.371 | 3.262  | 4.276  | 1.397           | 2.241 | 2.768 | 3.776 | 4.932 |
| 22     | 1.138           | 1.887 | 2.350 | 3.233  | 4.238  | 1.376           | 2.208 | 2.729 | 3.727 | 4.866 |
| 23     | 1.126           | 1.869 | 2.329 | 3.206  | 4.204  | 1.355           | 2.179 | 2.693 | 3.680 | 4.806 |
| 24     | 1.114           | 1.853 | 2.309 | 3.181  | 4.171  | 1.336           | 2.154 | 2.663 | 3.638 | 4.755 |
| 25     | 1.103           | 1.838 | 2.292 | 3.158  | 4.143  | 1.319           | 2.129 | 2.632 | 3.601 | 4.706 |
| 30     | 1.059           | 1.778 | 2.220 | 3.064  | 4.022  | 1.249           | 2.029 | 2.516 | 3.446 | 4.508 |
| 35     | 1.025           | 1.732 | 2.166 | 2.994  | 3.934  | 1.195           | 1.957 | 2.431 | 3.334 | 4.364 |
| 40     | 0.999           | 1.697 | 2.126 | 2.941  | 3.866  | 1.154           | 1.902 | 2.365 | 3.250 | 4.255 |
| 45     | 0.978           | 1.669 | 2.092 | 2.897  | 3.811  | 1.122           | 1.857 | 2.313 | 3.181 | 4.168 |
| 50     | 0.961           | 1.646 | 2.065 | 2.863  | 3.766  | 1.096           | 1.821 | 2.296 | 3.124 | 4.096 |

## TABLES

**TABLE A-8. SAMPLE SIZES REQUIRED TO DETECT PRESCRIBED DIFFERENCES BETWEEN AVERAGES WHEN THE SIGN OF THE DIFFERENCE IS NOT IMPORTANT**

The table entry is the sample size ( $n$ ) required to detect, with probability  $1 - \beta$ , that the average  $m$  of a new product differs from the standard  $m_0$  (or that two product averages  $m_A$  and  $m_B$  differ). The standardized difference is  $d$ , where

$$d = \frac{|m - m_0|}{\sigma} \quad (\text{or } d = \frac{|m_A - m_B|}{\sqrt{\sigma_A^2 + \sigma_B^2}} \text{ if we are comparing two products}).$$

The standard deviations are assumed to be known, and  $n$  is determined by the formula:

$$n = \frac{(z_{1-\alpha/2} + z_{1-\beta})^2}{d^2}$$

$$\alpha = .01$$

| $d \backslash 1-\beta$ | .50 | .60 | .70 | .80  | .90  | .95  | .99  |
|------------------------|-----|-----|-----|------|------|------|------|
| .1                     | 664 | 801 | 962 | 1168 | 1488 | 1782 | 2404 |
| .2                     | 166 | 201 | 241 | 292  | 372  | 446  | 601  |
| .4                     | 42  | 51  | 61  | 73   | 93   | 112  | 151  |
| .6                     | 19  | 23  | 27  | 33   | 42   | 50   | 67   |
| .8                     | 11  | 13  | 16  | 19   | 24   | 28   | 38   |
| 1.0                    | 7   | 9   | 10  | 12   | 15   | 18   | 25   |
| 1.2                    | 5   | 6   | 7   | 9    | 11   | 13   | 17   |
| 1.4                    | 4   | 5   | 5   | 6    | 8    | 10   | 13   |
| 1.6                    | 3   | 4   | 4   | 5    | 6    | 7    | 10   |
| 1.8                    | 3   | 3   | 3   | 4    | 5    | 6    | 8    |
| 2.0                    | 2   | 3   | 3   | 3    | 4    | 5    | 7    |
| 3.0                    | 1   | 1   | 2   | 2    | 2    | 2    | 3    |

If we must estimate  $\sigma$  from our sample and use Student's  $t$ , then we should add 4 to the tabulated values to obtain the approximate required sample size. (If we are comparing two product averages, add 2 to the tabulated values, to obtain the required size of each sample. For this case, we must have  $\sigma_A = \sigma_B$ ).

$$\alpha = .05$$

| $d \backslash 1-\beta$ | .50 | .60 | .70 | .80 | .90  | .95  | .99  |
|------------------------|-----|-----|-----|-----|------|------|------|
| .1                     | 385 | 490 | 618 | 785 | 1051 | 1300 | 1838 |
| .2                     | 97  | 123 | 155 | 197 | 263  | 325  | 460  |
| .4                     | 25  | 31  | 39  | 50  | 66   | 82   | 115  |
| .6                     | 11  | 14  | 18  | 22  | 30   | 37   | 52   |
| .8                     | 7   | 8   | 10  | 13  | 17   | 21   | 29   |
| 1.0                    | 4   | 5   | 7   | 8   | 11   | 13   | 19   |
| 1.2                    | 3   | 4   | 5   | 6   | 8    | 10   | 13   |
| 1.4                    | 2   | 3   | 4   | 5   | 6    | 7    | 10   |
| 1.6                    | 2   | 2   | 3   | 4   | 5    | 6    | 8    |
| 1.8                    | 2   | 2   | 2   | 3   | 4    | 5    | 6    |
| 2.0                    | 1   | 2   | 2   | 2   | 3    | 4    | 5    |
| 3.0                    | 1   | 1   | 1   | 1   | 2    | 2    | 3    |

If we must estimate  $\sigma$  from our sample and use Student's  $t$ , then we should add 2 to the tabulated values to obtain the approximate required sample size. (If we are comparing two product averages, add 1 to the tabulated values to obtain the required size of each sample. For this case, we must have  $\sigma_A = \sigma_B$ ).



## TABLES

**TABLE A-9. SAMPLE SIZES REQUIRED TO DETECT PRESCRIBED DIFFERENCES BETWEEN AVERAGES WHEN THE SIGN OF THE DIFFERENCE IS IMPORTANT**

The table entry is the sample size ( $n$ ) required to detect with probability  $1 - \beta$  that:

(a) the average  $m$  of a new product exceeds that of a standard  $m_0$

(b) the average  $m$  of a new product is less than that of a standard  $m_0$

(c) the average of a specified product  $m_A$  exceeds the average of another specified product  $m_B$ .

The standardized difference is  $d$ , where:

$$(a) \quad d = \frac{m - m_0}{\sigma}$$

$$(b) \quad d = \frac{m_0 - m}{\sigma}$$

$$(c) \quad d = \frac{m_A - m_B}{\sqrt{\sigma_A^2 + \sigma_B^2}}$$

The standard deviations are assumed to be known, and  $n$  is calculated from the following formula:

$$n = \frac{(z_{1-\alpha} + z_{1-\beta})^2}{d^2}$$

$$\alpha = .01$$

| $d \backslash 1-\beta$ | .50 | .60 | .70 | .80  | .90  | .95  | .99  |
|------------------------|-----|-----|-----|------|------|------|------|
| .1                     | 542 | 666 | 813 | 1004 | 1302 | 1578 | 2165 |
| .2                     | 136 | 167 | 204 | 251  | 326  | 395  | 542  |
| .4                     | 34  | 42  | 51  | 63   | 82   | 99   | 136  |
| .6                     | 16  | 19  | 23  | 28   | 37   | 44   | 61   |
| .8                     | 9   | 11  | 13  | 16   | 21   | 25   | 34   |
| 1.0                    | 6   | 7   | 9   | 11   | 14   | 16   | 22   |
| 1.2                    | 4   | 5   | 6   | 7    | 10   | 11   | 16   |
| 1.4                    | 3   | 4   | 5   | 6    | 7    | 9    | 12   |
| 1.6                    | 3   | 3   | 4   | 4    | 6    | 7    | 9    |
| 1.8                    | 2   | 3   | 3   | 4    | 5    | 5    | 7    |
| 2.0                    | 2   | 2   | 3   | 3    | 4    | 4    | 6    |
| 3.0                    | 1   | 1   | 1   | 2    | 2    | 2    | 3    |

If we must estimate  $\sigma$  from our sample, and use Student's  $t$ , add 3 to the tabulated values to obtain the approximate required sample size. (If we are comparing two product averages, add 2 to the tabulated values to obtain the required size of each sample. For this case, we must have  $\sigma_A = \sigma_B$ ).

$$\alpha = .05$$

| $d \backslash 1-\beta$ | .50 | .60 | .70 | .80 | .90 | .95  | .99  |
|------------------------|-----|-----|-----|-----|-----|------|------|
| .1                     | 271 | 361 | 471 | 619 | 857 | 1083 | 1578 |
| .2                     | 68  | 91  | 118 | 155 | 215 | 271  | 395  |
| .4                     | 17  | 23  | 30  | 39  | 54  | 68   | 99   |
| .6                     | 8   | 11  | 14  | 18  | 24  | 31   | 44   |
| .8                     | 5   | 6   | 8   | 10  | 14  | 17   | 25   |
| 1.0                    | 3   | 4   | 5   | 7   | 9   | 11   | 16   |
| 1.2                    | 2   | 3   | 4   | 5   | 6   | 8    | 11   |
| 1.4                    | 2   | 2   | 3   | 4   | 5   | 6    | 9    |
| 1.6                    | 2   | 2   | 2   | 3   | 4   | 5    | 7    |
| 1.8                    | 1   | 2   | 2   | 2   | 3   | 4    | 5    |
| 2.0                    | 1   | 1   | 2   | 2   | 3   | 3    | 4    |
| 3.0                    | 1   | 1   | 1   | 1   | 1   | 2    | 2    |

If we must estimate  $\sigma$  from our sample, and use Student's  $t$ , add 2 to the tabulated values to obtain the approximate required sample size. (If we are comparing two product averages, add 1 to the tabulated values to obtain the required size of each sample. For this case, we must have  $\sigma_A = \sigma_B$ ).

## TABLES

TABLE A-10. PERCENTILES OF THE STUDENTIZED RANGE,  $q$ 

$q = w/s$  where  $w$  is the range of  $t$  observations, and  $\nu$  is the number of degrees of freedom associated with the standard deviation  $s$ .

$q_{.90}$

| $\nu \backslash t$ | 2    | 3     | 4     | 5     | 6     | 7     | 8     | 9     | 10    |
|--------------------|------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1                  | 8.93 | 13.44 | 16.36 | 18.49 | 20.15 | 21.51 | 22.64 | 23.62 | 24.48 |
| 2                  | 4.13 | 5.73  | 6.77  | 7.54  | 8.14  | 8.63  | 9.05  | 9.41  | 9.72  |
| 3                  | 3.33 | 4.47  | 5.20  | 5.74  | 6.16  | 6.51  | 6.81  | 7.06  | 7.29  |
| 4                  | 3.01 | 3.98  | 4.59  | 5.03  | 5.39  | 5.68  | 5.93  | 6.14  | 6.33  |
| 5                  | 2.85 | 3.72  | 4.26  | 4.66  | 4.98  | 5.24  | 5.46  | 5.65  | 5.82  |
| 6                  | 2.75 | 3.56  | 4.07  | 4.44  | 4.73  | 4.97  | 5.17  | 5.34  | 5.50  |
| 7                  | 2.68 | 3.45  | 3.93  | 4.28  | 4.55  | 4.78  | 4.97  | 5.14  | 5.28  |
| 8                  | 2.63 | 3.37  | 3.83  | 4.17  | 4.43  | 4.65  | 4.83  | 4.99  | 5.13  |
| 9                  | 2.59 | 3.32  | 3.76  | 4.08  | 4.34  | 4.54  | 4.72  | 4.87  | 5.01  |
| 10                 | 2.56 | 3.27  | 3.70  | 4.02  | 4.26  | 4.47  | 4.64  | 4.78  | 4.91  |
| 11                 | 2.54 | 3.23  | 3.66  | 3.96  | 4.20  | 4.40  | 4.57  | 4.71  | 4.84  |
| 12                 | 2.52 | 3.20  | 3.62  | 3.92  | 4.16  | 4.35  | 4.51  | 4.65  | 4.78  |
| 13                 | 2.50 | 3.18  | 3.59  | 3.88  | 4.12  | 4.30  | 4.46  | 4.60  | 4.72  |
| 14                 | 2.49 | 3.16  | 3.56  | 3.85  | 4.08  | 4.27  | 4.42  | 4.56  | 4.68  |
| 15                 | 2.48 | 3.14  | 3.54  | 3.83  | 4.05  | 4.23  | 4.39  | 4.52  | 4.64  |
| 16                 | 2.47 | 3.12  | 3.52  | 3.80  | 4.03  | 4.21  | 4.36  | 4.49  | 4.61  |
| 17                 | 2.46 | 3.11  | 3.50  | 3.78  | 4.00  | 4.18  | 4.33  | 4.46  | 4.58  |
| 18                 | 2.45 | 3.10  | 3.49  | 3.77  | 3.98  | 4.16  | 4.31  | 4.44  | 4.55  |
| 19                 | 2.45 | 3.09  | 3.47  | 3.75  | 3.97  | 4.14  | 4.29  | 4.42  | 4.53  |
| 20                 | 2.44 | 3.08  | 3.46  | 3.74  | 3.95  | 4.12  | 4.27  | 4.40  | 4.51  |
| 24                 | 2.42 | 3.05  | 3.42  | 3.69  | 3.90  | 4.07  | 4.21  | 4.34  | 4.44  |
| 30                 | 2.40 | 3.02  | 3.39  | 3.65  | 3.85  | 4.02  | 4.16  | 4.28  | 4.38  |
| 40                 | 2.38 | 2.99  | 3.35  | 3.60  | 3.80  | 3.96  | 4.10  | 4.21  | 4.32  |
| 60                 | 2.36 | 2.96  | 3.31  | 3.56  | 3.75  | 3.91  | 4.04  | 4.16  | 4.25  |
| 120                | 2.34 | 2.93  | 3.28  | 3.52  | 3.71  | 3.86  | 3.99  | 4.10  | 4.19  |
| $\infty$           | 2.33 | 2.90  | 3.24  | 3.48  | 3.66  | 3.81  | 3.93  | 4.04  | 4.13  |

Adapted by permission from *Biometrika*, Vol. 46, Dec. 1959, from article entitled "Tables of the Upper 10 % Points of the Studentized Range (Accompanied by Revised Tables of 5 % and 1 % Points)," by James Fackhaus.

## TABLES

TABLE A-10 (Continued). PERCENTILES OF THE STUDENTIZED RANGE,  $q$  $q_{.90}$ 

| $\nu \backslash t$ | 11    | 12    | 13    | 14    | 15    | 16    | 17    | 18    | 19    | 20    |
|--------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1                  | 25.24 | 25.92 | 26.54 | 27.10 | 27.62 | 28.10 | 28.54 | 28.96 | 29.35 | 29.71 |
| 2                  | 10.01 | 10.26 | 10.49 | 10.70 | 10.89 | 11.07 | 11.24 | 11.39 | 11.54 | 11.68 |
| 3                  | 7.49  | 7.67  | 7.83  | 7.98  | 8.12  | 8.25  | 8.37  | 8.48  | 8.58  | 8.68  |
| 4                  | 6.49  | 6.65  | 6.78  | 6.91  | 7.02  | 7.13  | 7.23  | 7.33  | 7.41  | 7.50  |
| 5                  | 5.97  | 6.10  | 6.22  | 6.34  | 6.44  | 6.54  | 6.63  | 6.71  | 6.79  | 6.86  |
| 6                  | 5.64  | 5.76  | 5.87  | 5.98  | 6.07  | 6.16  | 6.25  | 6.32  | 6.40  | 6.47  |
| 7                  | 5.41  | 5.53  | 5.64  | 5.74  | 5.83  | 5.91  | 5.99  | 6.06  | 6.13  | 6.19  |
| 8                  | 5.25  | 5.36  | 5.46  | 5.56  | 5.64  | 5.72  | 5.80  | 5.87  | 5.93  | 6.00  |
| 9                  | 5.13  | 5.23  | 5.33  | 5.42  | 5.51  | 5.58  | 5.66  | 5.72  | 5.79  | 5.85  |
| 10                 | 5.03  | 5.13  | 5.23  | 5.32  | 5.40  | 5.47  | 5.54  | 5.61  | 5.67  | 5.73  |
| 11                 | 4.95  | 5.05  | 5.15  | 5.23  | 5.31  | 5.38  | 5.45  | 5.51  | 5.57  | 5.63  |
| 12                 | 4.89  | 4.99  | 5.08  | 5.16  | 5.24  | 5.31  | 5.37  | 5.44  | 5.49  | 5.55  |
| 13                 | 4.83  | 4.93  | 5.02  | 5.10  | 5.18  | 5.25  | 5.31  | 5.37  | 5.43  | 5.48  |
| 14                 | 4.79  | 4.88  | 4.97  | 5.05  | 5.12  | 5.19  | 5.26  | 5.32  | 5.37  | 5.43  |
| 15                 | 4.75  | 4.84  | 4.93  | 5.01  | 5.08  | 5.15  | 5.21  | 5.27  | 5.32  | 5.38  |
| 16                 | 4.71  | 4.81  | 4.89  | 4.97  | 5.04  | 5.11  | 5.17  | 5.23  | 5.28  | 5.33  |
| 17                 | 4.68  | 4.77  | 4.86  | 4.93  | 5.01  | 5.07  | 5.13  | 5.19  | 5.24  | 5.30  |
| 18                 | 4.65  | 4.75  | 4.83  | 4.90  | 4.98  | 5.04  | 5.10  | 5.16  | 5.21  | 5.26  |
| 19                 | 4.63  | 4.72  | 4.80  | 4.88  | 4.95  | 5.01  | 5.07  | 5.13  | 5.18  | 5.23  |
| 20                 | 4.61  | 4.70  | 4.78  | 4.85  | 4.92  | 4.99  | 5.05  | 5.10  | 5.16  | 5.20  |
| 24                 | 4.54  | 4.63  | 4.71  | 4.78  | 4.85  | 4.91  | 4.97  | 5.02  | 5.07  | 5.12  |
| 30                 | 4.47  | 4.56  | 4.64  | 4.71  | 4.77  | 4.83  | 4.89  | 4.94  | 4.99  | 5.03  |
| 40                 | 4.41  | 4.49  | 4.56  | 4.63  | 4.69  | 4.75  | 4.81  | 4.86  | 4.90  | 4.95  |
| 60                 | 4.34  | 4.42  | 4.49  | 4.56  | 4.62  | 4.67  | 4.73  | 4.78  | 4.82  | 4.86  |
| 120                | 4.28  | 4.35  | 4.42  | 4.48  | 4.54  | 4.60  | 4.65  | 4.69  | 4.74  | 4.78  |
| $\infty$           | 4.21  | 4.28  | 4.35  | 4.41  | 4.47  | 4.52  | 4.57  | 4.61  | 4.65  | 4.69  |

## TABLES

TABLE A-10 (Continued). PERCENTILES OF THE STUDENTIZED RANGE,  $q$  $q_{.95}$ 

| $\nu \backslash t$ | 2     | 3     | 4     | 5     | 6     | 7     | 8     | 9     | 10    |
|--------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1                  | 17.97 | 26.98 | 32.82 | 37.08 | 40.41 | 43.12 | 45.40 | 47.36 | 49.07 |
| 2                  | 6.08  | 8.33  | 9.80  | 10.88 | 11.74 | 12.44 | 13.03 | 13.54 | 13.99 |
| 3                  | 4.50  | 5.91  | 6.82  | 7.50  | 8.04  | 8.48  | 8.85  | 9.18  | 9.46  |
| 4                  | 3.93  | 5.04  | 5.76  | 6.29  | 6.71  | 7.05  | 7.35  | 7.60  | 7.83  |
| 5                  | 3.64  | 4.60  | 5.22  | 5.67  | 6.03  | 6.33  | 6.58  | 6.80  | 6.99  |
| 6                  | 3.46  | 4.34  | 4.90  | 5.30  | 5.63  | 5.90  | 6.12  | 6.32  | 6.49  |
| 7                  | 3.34  | 4.16  | 4.68  | 5.06  | 5.36  | 5.61  | 5.82  | 6.00  | 6.16  |
| 8                  | 3.26  | 4.04  | 4.53  | 4.89  | 5.17  | 5.40  | 5.60  | 5.77  | 5.92  |
| 9                  | 3.20  | 3.95  | 4.41  | 4.76  | 5.02  | 5.24  | 5.43  | 5.59  | 5.74  |
| 10                 | 3.15  | 3.88  | 4.33  | 4.65  | 4.91  | 5.12  | 5.30  | 5.46  | 5.60  |
| 11                 | 3.11  | 3.82  | 4.26  | 4.57  | 4.82  | 5.03  | 5.20  | 5.35  | 5.49  |
| 12                 | 3.08  | 3.77  | 4.20  | 4.51  | 4.75  | 4.95  | 5.12  | 5.27  | 5.39  |
| 13                 | 3.06  | 3.73  | 4.15  | 4.45  | 4.69  | 4.88  | 5.05  | 5.19  | 5.32  |
| 14                 | 3.03  | 3.70  | 4.11  | 4.41  | 4.64  | 4.83  | 4.99  | 5.13  | 5.25  |
| 15                 | 3.01  | 3.67  | 4.08  | 4.37  | 4.59  | 4.78  | 4.94  | 5.08  | 5.20  |
| 16                 | 3.00  | 3.65  | 4.05  | 4.33  | 4.56  | 4.74  | 4.90  | 5.03  | 5.15  |
| 17                 | 2.98  | 3.63  | 4.02  | 4.30  | 4.52  | 4.70  | 4.86  | 4.99  | 5.11  |
| 18                 | 2.97  | 3.61  | 4.00  | 4.28  | 4.49  | 4.67  | 4.82  | 4.96  | 5.07  |
| 19                 | 2.96  | 3.59  | 3.98  | 4.25  | 4.47  | 4.65  | 4.79  | 4.92  | 5.04  |
| 20                 | 2.95  | 3.58  | 3.96  | 4.23  | 4.45  | 4.62  | 4.77  | 4.90  | 5.01  |
| 24                 | 2.92  | 3.53  | 3.90  | 4.17  | 4.37  | 4.54  | 4.68  | 4.81  | 4.92  |
| 30                 | 2.89  | 3.49  | 3.85  | 4.10  | 4.30  | 4.46  | 4.60  | 4.72  | 4.82  |
| 40                 | 2.86  | 3.44  | 3.79  | 4.04  | 4.23  | 4.39  | 4.52  | 4.63  | 4.73  |
| 60                 | 2.83  | 3.40  | 3.74  | 3.98  | 4.16  | 4.31  | 4.44  | 4.55  | 4.65  |
| 120                | 2.80  | 3.36  | 3.68  | 3.92  | 4.10  | 4.24  | 4.36  | 4.47  | 4.56  |
| $\infty$           | 2.77  | 3.31  | 3.63  | 3.86  | 4.03  | 4.17  | 4.29  | 4.39  | 4.47  |

## TABLES

TABLE A-10 (Continued). PERCENTILES OF THE STUDENTIZED RANGE,  $q$  $q_{.95}$ 

| $\nu \backslash t$ | 11    | 12    | 13    | 14    | 15    | 16    | 17    | 18    | 19    | 20    |
|--------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1                  | 50.59 | 51.96 | 53.20 | 54.33 | 55.36 | 56.32 | 57.22 | 58.04 | 58.83 | 59.56 |
| 2                  | 14.39 | 14.75 | 15.08 | 15.38 | 15.65 | 15.91 | 16.14 | 16.37 | 16.57 | 16.77 |
| 3                  | 9.72  | 9.95  | 10.15 | 10.35 | 10.52 | 10.69 | 10.84 | 10.98 | 11.11 | 11.24 |
| 4                  | 8.03  | 8.21  | 8.37  | 8.52  | 8.66  | 8.79  | 8.91  | 9.03  | 9.13  | 9.23  |
| 5                  | 7.17  | 7.32  | 7.47  | 7.60  | 7.72  | 7.83  | 7.93  | 8.03  | 8.12  | 8.21  |
| 6                  | 6.65  | 6.79  | 6.92  | 7.03  | 7.14  | 7.24  | 7.34  | 7.43  | 7.51  | 7.59  |
| 7                  | 6.30  | 6.43  | 6.55  | 6.66  | 6.76  | 6.85  | 6.94  | 7.02  | 7.10  | 7.17  |
| 8                  | 6.05  | 6.18  | 6.29  | 6.39  | 6.48  | 6.57  | 6.65  | 6.73  | 6.80  | 6.87  |
| 9                  | 5.87  | 5.98  | 6.09  | 6.19  | 6.28  | 6.36  | 6.44  | 6.51  | 6.58  | 6.64  |
| 10                 | 5.72  | 5.83  | 5.93  | 6.03  | 6.11  | 6.19  | 6.27  | 6.34  | 6.40  | 6.47  |
| 11                 | 5.61  | 5.71  | 5.81  | 5.90  | 5.98  | 6.06  | 6.13  | 6.20  | 6.27  | 6.33  |
| 12                 | 5.51  | 5.61  | 5.71  | 5.80  | 5.88  | 5.95  | 6.02  | 6.09  | 6.15  | 6.21  |
| 13                 | 5.43  | 5.53  | 5.63  | 5.71  | 5.79  | 5.86  | 5.93  | 5.99  | 6.05  | 6.11  |
| 14                 | 5.36  | 5.46  | 5.55  | 5.64  | 5.71  | 5.79  | 5.85  | 5.91  | 5.97  | 6.03  |
| 15                 | 5.31  | 5.40  | 5.49  | 5.57  | 5.65  | 5.72  | 5.78  | 5.85  | 5.90  | 5.96  |
| 16                 | 5.26  | 5.35  | 5.44  | 5.52  | 5.59  | 5.66  | 5.73  | 5.79  | 5.84  | 5.90  |
| 17                 | 5.21  | 5.31  | 5.39  | 5.47  | 5.54  | 5.61  | 5.67  | 5.73  | 5.79  | 5.84  |
| 18                 | 5.17  | 5.27  | 5.35  | 5.43  | 5.50  | 5.57  | 5.63  | 5.69  | 5.74  | 5.79  |
| 19                 | 5.14  | 5.23  | 5.31  | 5.39  | 5.46  | 5.53  | 5.59  | 5.65  | 5.70  | 5.75  |
| 20                 | 5.11  | 5.20  | 5.28  | 5.36  | 5.43  | 5.49  | 5.55  | 5.61  | 5.66  | 5.71  |
| 24                 | 5.01  | 5.10  | 5.18  | 5.25  | 5.32  | 5.38  | 5.44  | 5.49  | 5.55  | 5.59  |
| 30                 | 4.92  | 5.00  | 5.08  | 5.15  | 5.21  | 5.27  | 5.33  | 5.38  | 5.43  | 5.47  |
| 40                 | 4.82  | 4.90  | 4.98  | 5.04  | 5.11  | 5.16  | 5.22  | 5.27  | 5.31  | 5.36  |
| 60                 | 4.73  | 4.81  | 4.88  | 4.94  | 5.00  | 5.06  | 5.11  | 5.15  | 5.20  | 5.24  |
| 120                | 4.64  | 4.71  | 4.78  | 4.84  | 4.90  | 4.95  | 5.00  | 5.04  | 5.09  | 5.13  |
| $\infty$           | 4.55  | 4.62  | 4.68  | 4.74  | 4.80  | 4.85  | 4.89  | 4.93  | 4.97  | 5.01  |

## TABLES

TABLE A-10 (Continued). PERCENTILES OF THE STUDENTIZED RANGE,  $q$  $q_{.99}$ 

| $t$      | 2     | 3     | 4     | 5     | 6     | 7     | 8     | 9     | 10    |
|----------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1        | 90.03 | 135.0 | 164.3 | 185.6 | 202.2 | 215.8 | 227.2 | 237.0 | 245.6 |
| 2        | 14.04 | 19.02 | 22.29 | 24.72 | 26.63 | 28.20 | 29.53 | 30.68 | 31.69 |
| 3        | 8.26  | 10.62 | 12.17 | 13.33 | 14.24 | 15.00 | 15.64 | 16.20 | 16.69 |
| 4        | 6.51  | 8.12  | 9.17  | 9.96  | 10.58 | 11.10 | 11.55 | 11.93 | 12.27 |
| 5        | 5.70  | 6.98  | 7.80  | 8.42  | 8.91  | 9.32  | 9.67  | 9.97  | 10.24 |
| 6        | 5.24  | 6.33  | 7.03  | 7.56  | 7.97  | 8.32  | 8.61  | 8.87  | 9.10  |
| 7        | 4.95  | 5.92  | 6.54  | 7.01  | 7.37  | 7.68  | 7.94  | 8.17  | 8.37  |
| 8        | 4.75  | 5.64  | 6.20  | 6.62  | 6.96  | 7.24  | 7.47  | 7.68  | 7.86  |
| 9        | 4.60  | 5.43  | 5.96  | 6.35  | 6.66  | 6.91  | 7.13  | 7.33  | 7.49  |
| 10       | 4.48  | 5.27  | 5.77  | 6.14  | 6.43  | 6.67  | 6.87  | 7.05  | 7.21  |
| 11       | 4.39  | 5.15  | 5.62  | 5.97  | 6.25  | 6.48  | 6.67  | 6.84  | 6.99  |
| 12       | 4.32  | 5.05  | 5.50  | 5.84  | 6.10  | 6.32  | 6.51  | 6.67  | 6.81  |
| 13       | 4.26  | 4.96  | 5.40  | 5.73  | 5.98  | 6.19  | 6.37  | 6.53  | 6.67  |
| 14       | 4.21  | 4.89  | 5.32  | 5.63  | 5.88  | 6.08  | 6.26  | 6.41  | 6.54  |
| 15       | 4.17  | 4.84  | 5.25  | 5.56  | 5.80  | 5.99  | 6.16  | 6.31  | 6.44  |
| 16       | 4.13  | 4.79  | 5.19  | 5.49  | 5.72  | 5.92  | 6.08  | 6.22  | 6.35  |
| 17       | 4.10  | 4.74  | 5.14  | 5.43  | 5.66  | 5.85  | 6.01  | 6.15  | 6.27  |
| 18       | 4.07  | 4.70  | 5.09  | 5.38  | 5.60  | 5.79  | 5.94  | 6.08  | 6.20  |
| 19       | 4.05  | 4.67  | 5.05  | 5.33  | 5.55  | 5.73  | 5.89  | 6.02  | 6.14  |
| 20       | 4.02  | 4.64  | 5.02  | 5.29  | 5.51  | 5.69  | 5.84  | 5.97  | 6.09  |
| 24       | 3.96  | 4.55  | 4.91  | 5.17  | 5.37  | 5.54  | 5.69  | 5.81  | 5.92  |
| 30       | 3.89  | 4.45  | 4.80  | 5.05  | 5.24  | 5.40  | 5.54  | 5.65  | 5.76  |
| 40       | 3.82  | 4.37  | 4.70  | 4.93  | 5.11  | 5.26  | 5.39  | 5.50  | 5.60  |
| 60       | 3.76  | 4.28  | 4.59  | 4.82  | 4.99  | 5.13  | 5.25  | 5.36  | 5.45  |
| 120      | 3.70  | 4.20  | 4.50  | 4.71  | 4.87  | 5.01  | 5.12  | 5.21  | 5.30  |
| $\infty$ | 3.64  | 4.12  | 4.40  | 4.60  | 4.76  | 4.88  | 4.99  | 5.08  | 5.16  |

## TABLES

TABLE A-10 (Continued). PERCENTILES OF THE STUDENTIZED RANGE,  $q$  $q_{.99}$ 

| $\nu \backslash t$ | 11    | 12    | 13    | 14    | 15    | 16    | 17    | 18    | 19    | 20    |
|--------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1                  | 253.2 | 260.0 | 266.2 | 271.8 | 277.0 | 281.8 | 286.3 | 290.4 | 294.3 | 298.0 |
| 2                  | 32.59 | 33.40 | 34.13 | 34.81 | 35.43 | 36.00 | 36.53 | 37.03 | 37.50 | 37.95 |
| 3                  | 17.13 | 17.53 | 17.89 | 18.22 | 18.52 | 18.81 | 19.07 | 19.32 | 19.55 | 19.77 |
| 4                  | 12.57 | 12.84 | 13.09 | 13.32 | 13.53 | 13.73 | 13.91 | 14.08 | 14.24 | 14.40 |
| 5                  | 10.48 | 10.70 | 10.89 | 11.08 | 11.24 | 11.40 | 11.55 | 11.68 | 11.81 | 11.93 |
| 6                  | 9.30  | 9.48  | 9.65  | 9.81  | 9.95  | 10.08 | 10.21 | 10.32 | 10.43 | 10.54 |
| 7                  | 8.55  | 8.71  | 8.86  | 9.00  | 9.12  | 9.24  | 9.35  | 9.46  | 9.55  | 9.65  |
| 8                  | 8.03  | 8.18  | 8.31  | 8.44  | 8.55  | 8.66  | 8.76  | 8.85  | 8.94  | 9.03  |
| 9                  | 7.65  | 7.78  | 7.91  | 8.03  | 8.13  | 8.23  | 8.33  | 8.41  | 8.49  | 8.57  |
| 10                 | 7.36  | 7.49  | 7.60  | 7.71  | 7.81  | 7.91  | 7.99  | 8.08  | 8.15  | 8.23  |
| 11                 | 7.13  | 7.25  | 7.36  | 7.46  | 7.56  | 7.65  | 7.73  | 7.81  | 7.88  | 7.95  |
| 12                 | 6.94  | 7.06  | 7.17  | 7.26  | 7.36  | 7.44  | 7.52  | 7.59  | 7.66  | 7.73  |
| 13                 | 6.79  | 6.90  | 7.01  | 7.10  | 7.19  | 7.27  | 7.35  | 7.42  | 7.48  | 7.55  |
| 14                 | 6.66  | 6.77  | 6.87  | 6.96  | 7.05  | 7.13  | 7.20  | 7.27  | 7.33  | 7.39  |
| 15                 | 6.55  | 6.66  | 6.76  | 6.84  | 6.93  | 7.00  | 7.07  | 7.14  | 7.20  | 7.26  |
| 16                 | 6.46  | 6.56  | 6.66  | 6.74  | 6.82  | 6.90  | 6.97  | 7.03  | 7.09  | 7.15  |
| 17                 | 6.38  | 6.48  | 6.57  | 6.66  | 6.73  | 6.81  | 6.87  | 6.94  | 7.00  | 7.05  |
| 18                 | 6.31  | 6.41  | 6.50  | 6.58  | 6.65  | 6.73  | 6.79  | 6.85  | 6.91  | 6.97  |
| 19                 | 6.25  | 6.34  | 6.43  | 6.51  | 6.58  | 6.65  | 6.72  | 6.78  | 6.84  | 6.89  |
| 20                 | 6.19  | 6.28  | 6.37  | 6.45  | 6.52  | 6.59  | 6.65  | 6.71  | 6.77  | 6.82  |
| 24                 | 6.02  | 6.11  | 6.19  | 6.26  | 6.33  | 6.39  | 6.45  | 6.51  | 6.56  | 6.61  |
| 30                 | 5.85  | 5.93  | 6.01  | 6.08  | 6.14  | 6.20  | 6.26  | 6.31  | 6.36  | 6.41  |
| 40                 | 5.69  | 5.76  | 5.83  | 5.90  | 5.96  | 6.02  | 6.07  | 6.12  | 6.16  | 6.21  |
| 60                 | 5.53  | 5.60  | 5.67  | 5.73  | 5.78  | 5.84  | 5.89  | 5.93  | 5.97  | 6.01  |
| 120                | 5.37  | 5.44  | 5.50  | 5.56  | 5.61  | 5.66  | 5.71  | 5.75  | 5.79  | 5.83  |
| $\infty$           | 5.23  | 5.29  | 5.35  | 5.40  | 5.45  | 5.49  | 5.54  | 5.57  | 5.61  | 5.65  |

## TABLES

TABLE A-11. PERCENTILES OF  $F' = \frac{w_A}{w_B}$ 

| $n_B$ | Cum.<br>Prop. | $n_A$ |      |     |     |     |     |     |      |      |
|-------|---------------|-------|------|-----|-----|-----|-----|-----|------|------|
|       |               | 2     | 3    | 4   | 5   | 6   | 7   | 8   | 9    | 10   |
| 2     | .005          | .0078 | .096 | .21 | .30 | .38 | .44 | .49 | .54  | .57  |
|       | .01           | .0157 | .136 | .26 | .38 | .46 | .53 | .59 | .64  | .68  |
|       | .025          | .039  | .217 | .37 | .50 | .60 | .68 | .74 | .79  | .83  |
|       | .05           | .079  | .31  | .50 | .62 | .74 | .80 | .86 | .91  | .95  |
|       | .95           | 12.7  | 19.1 | 23  | 26  | 29  | 30  | 32  | 34   | 35   |
|       | .975          | 25.5  | 38.2 | 52  | 57  | 60  | 62  | 64  | 67   | 68   |
|       | .99           | 63.7  | 95   | 116 | 132 | 142 | 153 | 160 | 168  | 174  |
|       | .995          | 127   | 191  | 230 | 250 | 260 | 270 | 280 | 290  | 290  |
|       |               |       |      |     |     |     |     |     |      |      |
| 3     | .005          | .0052 | .071 | .16 | .24 | .32 | .38 | .43 | .47  | .50  |
|       | .01           | .0105 | .100 | .20 | .30 | .37 | .43 | .49 | .53  | .57  |
|       | .025          | .026  | .160 | .28 | .39 | .47 | .54 | .59 | .64  | .68  |
|       | .05           | .052  | .23  | .37 | .49 | .57 | .64 | .70 | .75  | .80  |
|       | .95           | 3.19  | 4.4  | 5.0 | 5.7 | 6.2 | 6.6 | 6.9 | 7.2  | 7.4  |
|       | .975          | 4.61  | 6.3  | 7.3 | 8.0 | 8.7 | 9.3 | 9.8 | 10.2 | 10.5 |
|       | .99           | 7.37  | 10   | 12  | 13  | 14  | 15  | 15  | 16   | 17   |
|       | .995          | 10.4  | 14   | 17  | 18  | 20  | 21  | 22  | 23   | 25   |
|       |               |       |      |     |     |     |     |     |      |      |
| 4     | .005          | .0043 | .059 | .14 | .22 | .28 | .34 | .39 | .43  | .46  |
|       | .01           | .0086 | .084 | .18 | .26 | .33 | .39 | .44 | .48  | .52  |
|       | .025          | .019  | .137 | .25 | .34 | .42 | .48 | .53 | .57  | .61  |
|       | .05           | .043  | .20  | .32 | .42 | .50 | .57 | .62 | .67  | .70  |
|       | .95           | 2.02  | 2.7  | 3.1 | 3.4 | 3.6 | 3.8 | 4.0 | 4.2  | 4.4  |
|       | .975          | 2.72  | 3.5  | 4.0 | 4.4 | 4.7 | 5.0 | 5.2 | 5.4  | 5.6  |
|       | .99           | 3.83  | 5.0  | 5.5 | 6.0 | 6.4 | 6.7 | 7.0 | 7.2  | 7.5  |
|       | .995          | 4.85  | 6.1  | 7.0 | 7.6 | 8.1 | 8.5 | 8.8 | 9.3  | 9.6  |
|       |               |       |      |     |     |     |     |     |      |      |
| 5     | .005          | .0039 | .054 | .13 | .20 | .26 | .32 | .36 | .40  | .44  |
|       | .01           | .0076 | .079 | .17 | .24 | .31 | .36 | .41 | .45  | .49  |
|       | .025          | .018  | .124 | .23 | .32 | .38 | .44 | .49 | .53  | .57  |
|       | .05           | .038  | .18  | .29 | .40 | .46 | .52 | .57 | .61  | .65  |
|       | .95           | 1.61  | 2.1  | 2.4 | 2.6 | 2.8 | 2.9 | 3.0 | 3.1  | 3.2  |
|       | .975          | 2.01  | 2.6  | 2.9 | 3.2 | 3.4 | 3.6 | 3.7 | 3.8  | 3.9  |
|       | .99           | 2.64  | 3.4  | 3.8 | 4.1 | 4.3 | 4.6 | 4.7 | 4.9  | 5.0  |
|       | .995          | 3.36  | 4.1  | 4.6 | 4.9 | 5.2 | 5.5 | 5.7 | 5.9  | 6.1  |
|       |               |       |      |     |     |     |     |     |      |      |

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## TABLES

TABLE A-11 (Continued). PERCENTILES OF  $F' = \frac{w_A}{w_B}$ 

| $n_B$ | Cum.<br>Prop. | $n_A$ |      |     |     |     |     |     |     |     |
|-------|---------------|-------|------|-----|-----|-----|-----|-----|-----|-----|
|       |               | 2     | 3    | 4   | 5   | 6   | 7   | 8   | 9   | 10  |
| 6     | .005          | .0038 | .051 | .12 | .19 | .25 | .30 | .35 | .38 | .42 |
|       | .01           | .0070 | .073 | .16 | .23 | .29 | .34 | .39 | .43 | .46 |
|       | .025          | .017  | .115 | .21 | .30 | .36 | .42 | .46 | .50 | .54 |
|       | .05           | .035  | .16  | .27 | .36 | .43 | .49 | .54 | .58 | .61 |
|       | .95           | 1.36  | 1.8  | 2.0 | 2.2 | 2.3 | 2.4 | 2.5 | 2.6 | 2.7 |
|       | .975          | 1.67  | 2.1  | 2.4 | 2.6 | 2.8 | 2.9 | 3.0 | 3.1 | 3.2 |
|       | .99           | 2.16  | 2.7  | 3.0 | 3.2 | 3.4 | 3.6 | 3.7 | 3.8 | 3.9 |
|       | .995          | 2.67  | 3.1  | 3.5 | 3.8 | 4.0 | 4.1 | 4.3 | 4.5 | 4.6 |
|       |               |       |      |     |     |     |     |     |     |     |
| 7     | .005          | .0037 | .048 | .12 | .18 | .24 | .29 | .33 | .37 | .40 |
|       | .01           | .0066 | .069 | .15 | .22 | .28 | .33 | .37 | .41 | .45 |
|       | .025          | .016  | .107 | .20 | .28 | .34 | .40 | .44 | .48 | .52 |
|       | .05           | .032  | .15  | .26 | .35 | .41 | .47 | .51 | .55 | .59 |
|       | .95           | 1.26  | 1.6  | 1.8 | 1.9 | 2.0 | 2.1 | 2.2 | 2.3 | 2.4 |
|       | .975          | 1.48  | 1.9  | 2.1 | 2.3 | 2.4 | 2.5 | 2.6 | 2.7 | 2.8 |
|       | .99           | 1.87  | 2.3  | 2.6 | 2.8 | 2.9 | 3.0 | 3.1 | 3.2 | 3.3 |
|       | .995          | 2.28  | 2.7  | 2.9 | 3.1 | 3.3 | 3.5 | 3.6 | 3.7 | 3.8 |
|       |               |       |      |     |     |     |     |     |     |     |
| 8     | .005          | .0036 | .045 | .11 | .18 | .23 | .28 | .32 | .36 | .39 |
|       | .01           | .0063 | .065 | .14 | .21 | .27 | .32 | .36 | .40 | .43 |
|       | .025          | .016  | .102 | .19 | .27 | .33 | .38 | .43 | .47 | .50 |
|       | .05           | .031  | .14  | .25 | .33 | .40 | .45 | .50 | .53 | .57 |
|       | .95           | 1.17  | 1.4  | 1.6 | 1.8 | 1.9 | 1.9 | 2.0 | 2.1 | 2.1 |
|       | .975          | 1.36  | 1.7  | 1.9 | 2.0 | 2.2 | 2.3 | 2.3 | 2.4 | 2.5 |
|       | .99           | 1.69  | 2.1  | 2.3 | 2.4 | 2.6 | 2.7 | 2.8 | 2.8 | 2.9 |
|       | .995          | 2.03  | 2.3  | 2.6 | 2.7 | 2.9 | 3.0 | 3.1 | 3.2 | 3.3 |
|       |               |       |      |     |     |     |     |     |     |     |
| 9     | .005          | .0035 | .042 | .11 | .17 | .22 | .27 | .31 | .35 | .38 |
|       | .01           | .0060 | .062 | .14 | .21 | .26 | .31 | .35 | .39 | .42 |
|       | .025          | .015  | .098 | .18 | .26 | .32 | .37 | .42 | .46 | .49 |
|       | .05           | .030  | .14  | .24 | .32 | .38 | .44 | .48 | .52 | .55 |
|       | .95           | 1.10  | 1.3  | 1.5 | 1.6 | 1.7 | 1.8 | 1.9 | 1.9 | 2.0 |
|       | .975          | 1.27  | 1.6  | 1.8 | 1.9 | 2.0 | 2.1 | 2.1 | 2.2 | 2.3 |
|       | .99           | 1.56  | 1.9  | 2.1 | 2.2 | 2.3 | 2.4 | 2.5 | 2.6 | 2.6 |
|       | .995          | 1.87  | 2.1  | 2.3 | 2.5 | 2.6 | 2.7 | 2.8 | 2.9 | 3.0 |
|       |               |       |      |     |     |     |     |     |     |     |
| 10    | .005          | .0034 | .041 | .10 | .16 | .22 | .26 | .30 | .34 | .37 |
|       | .01           | .0058 | .060 | .13 | .20 | .26 | .30 | .34 | .38 | .41 |
|       | .025          | .015  | .095 | .18 | .25 | .31 | .36 | .41 | .44 | .48 |
|       | .05           | .029  | .13  | .23 | .31 | .37 | .43 | .47 | .51 | .54 |
|       | .95           | 1.05  | 1.3  | 1.4 | 1.5 | 1.6 | 1.7 | 1.8 | 1.8 | 1.9 |
|       | .975          | 1.21  | 1.5  | 1.6 | 1.8 | 1.9 | 1.9 | 2.0 | 2.0 | 2.1 |
|       | .99           | 1.47  | 1.8  | 1.9 | 2.1 | 2.2 | 2.2 | 2.3 | 2.4 | 2.4 |
|       | .995          | 1.75  | 2.0  | 2.2 | 2.3 | 2.4 | 2.5 | 2.6 | 2.6 | 2.7 |
|       |               |       |      |     |     |     |     |     |     |     |

## TABLES

TABLE A-12. PERCENTILES FOR  $\phi = \frac{\bar{X} - m_0}{w}$ 

| Sample Size | $\phi .95$ | $\phi .975$ | $\phi .99$ | $\phi .995$ | $\phi .999$ | $\phi .9995$ |
|-------------|------------|-------------|------------|-------------|-------------|--------------|
| 2           | 3.175      | 6.353       | 15.910     | 31.828      | 159.16      | 318.31       |
| 3           | .885       | 1.304       | 2.111      | 3.008       | 6.77        | 9.58         |
| 4           | .529       | .717        | 1.023      | 1.316       | 2.29        | 2.85         |
| 5           | .388       | .507        | .685       | .843        | 1.32        | 1.58         |
| 6           | .312       | .399        | .523       | .628        | .92         | 1.07         |
| 7           | .263       | .333        | .429       | .507        | .71         | .82          |
| 8           | .230       | .288        | .366       | .429        | .59         | .67          |
| 9           | .205       | .255        | .322       | .374        | .50         | .57          |
| 10          | .186       | .230        | .288       | .333        | .44         | .50          |
| 11          | .170       | .210        | .262       | .302        | .40         | .44          |
| 12          | .158       | .194        | .241       | .277        | .36         | .40          |
| 13          | .147       | .181        | .224       | .256        | .33         | .37          |
| 14          | .138       | .170        | .209       | .239        | .31         | .34          |
| 15          | .131       | .160        | .197       | .224        | .29         | .32          |
| 16          | .124       | .151        | .186       | .212        | .27         | .30          |
| 17          | .118       | .144        | .177       | .201        | .26         | .28          |
| 18          | .113       | .137        | .168       | .191        | .24         | .26          |
| 19          | .108       | .131        | .161       | .182        | .23         | .25          |
| 20          | .104       | .126        | .154       | .175        | .22         | .24          |

Adapted with permission from *Biometrika*, Vol. 34 (1947) from article entitled "The Use of the Range in Place of the Standard Deviation in the *t* Test" by E. Lord.

TABLE A-13. PERCENTILES FOR  $\phi' = \frac{\bar{X}_A - \bar{X}_B}{\frac{1}{2}(w_A + w_B)}$ 

| $n = n_A = n_B$ | $\phi' .95$ | $\phi' .975$ | $\phi' .99$ | $\phi' .995$ | $\phi' .999$ | $\phi' .9995$ |
|-----------------|-------------|--------------|-------------|--------------|--------------|---------------|
| 2               | 2.322       | 3.427        | 5.553       | 7.916        | 17.81        | 25.23         |
| 3               | .974        | 1.272        | 1.715       | 2.093        | 3.27         | 4.18          |
| 4               | .644        | .813         | 1.047       | 1.237        | 1.74         | 1.99          |
| 5               | .493        | .613         | .772        | .896         | 1.21         | 1.35          |
| 6               | .405        | .499         | .621        | .714         | .94          | 1.03          |
| 7               | .347        | .426         | .525        | .600         | .77          | .85           |
| 8               | .306        | .373         | .459        | .521         | .67          | .73           |
| 9               | .275        | .334         | .409        | .464         | .59          | .64           |
| 10              | .250        | .304         | .371        | .419         | .53          | .58           |
| 11              | .233        | .280         | .340        | .384         | .48          | .52           |
| 12              | .214        | .260         | .315        | .355         | .44          | .48           |
| 13              | .201        | .243         | .294        | .331         | .41          | .45           |
| 14              | .189        | .228         | .276        | .311         | .39          | .42           |
| 15              | .179        | .216         | .261        | .293         | .36          | .39           |
| 16              | .170        | .205         | .247        | .278         | .34          | .37           |
| 17              | .162        | .195         | .236        | .264         | .33          | .35           |
| 18              | .155        | .187         | .225        | .252         | .31          | .34           |
| 19              | .149        | .179         | .216        | .242         | .30          | .32           |
| 20              | .143        | .172         | .207        | .232         | .29          | .31           |

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## TABLES

TABLE A-14. CRITERIA FOR REJECTION OF OUTLYING OBSERVATIONS

| Statistic | Number of Observations, $n$ | Upper Percentiles |      |      |      |      |      |      |
|-----------|-----------------------------|-------------------|------|------|------|------|------|------|
|           |                             | .70               | .80  | .90  | .95  | .98  | .99  | .995 |
| $r_{10}$  | 3                           | .684              | .781 | .886 | .941 | .976 | .988 | .994 |
|           | 4                           | .471              | .560 | .679 | .765 | .846 | .889 | .926 |
|           | 5                           | .373              | .451 | .557 | .642 | .729 | .780 | .821 |
|           | 6                           | .318              | .386 | .482 | .560 | .644 | .698 | .740 |
|           | 7                           | .281              | .344 | .434 | .507 | .586 | .637 | .680 |
| $r_{11}$  | 8                           | .318              | .385 | .479 | .554 | .631 | .683 | .725 |
|           | 9                           | .288              | .352 | .441 | .512 | .587 | .635 | .677 |
|           | 10                          | .265              | .325 | .409 | .477 | .551 | .597 | .639 |
| $r_{12}$  | 11                          | .391              | .442 | .517 | .576 | .638 | .679 | .713 |
|           | 12                          | .370              | .419 | .490 | .546 | .605 | .642 | .675 |
|           | 13                          | .351              | .399 | .467 | .521 | .578 | .615 | .649 |
| $r_{25}$  | 14                          | .370              | .421 | .492 | .546 | .602 | .641 | .674 |
|           | 15                          | .353              | .402 | .472 | .525 | .579 | .616 | .647 |
|           | 16                          | .338              | .386 | .454 | .507 | .559 | .595 | .624 |
|           | 17                          | .325              | .373 | .438 | .490 | .542 | .577 | .605 |
|           | 18                          | .314              | .361 | .424 | .475 | .527 | .561 | .589 |
|           | 19                          | .304              | .350 | .412 | .462 | .514 | .547 | .575 |
|           | 20                          | .295              | .340 | .401 | .450 | .502 | .535 | .562 |
|           | 21                          | .287              | .331 | .391 | .440 | .491 | .524 | .551 |
|           | 22                          | .280              | .323 | .382 | .430 | .481 | .514 | .541 |
|           | 23                          | .274              | .316 | .374 | .421 | .472 | .505 | .532 |
|           | 24                          | .268              | .310 | .367 | .413 | .464 | .497 | .524 |
|           | 25                          | .262              | .304 | .360 | .406 | .457 | .489 | .516 |

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TABLE A-15. CRITICAL VALUES OF  $L$  FOR LINK-WALLACE TEST

$\alpha = .05$

 $t$  = number of groups = number of ranges

| $n \backslash t$ | 2    | 3    | 4    | 5    | 6    | 7    | 8   | 9   | 10  |
|------------------|------|------|------|------|------|------|-----|-----|-----|
| 2                | 3.43 | 2.37 | 1.78 | 1.40 | 1.16 | 1.00 | .87 | .78 | .70 |
| 3                | 1.91 | 1.44 | 1.13 | .94  | .80  | .70  | .62 | .56 | .51 |
| 4                | 1.63 | 1.25 | 1.01 | .84  | .72  | .63  | .57 | .51 | .47 |
| 5                | 1.53 | 1.19 | .96  | .81  | .70  | .61  | .55 | .50 | .45 |
| 6                | 1.50 | 1.18 | .95  | .80  | .69  | .61  | .55 | .49 | .45 |
| 7                | 1.49 | 1.17 | .95  | .80  | .69  | .61  | .55 | .50 | .45 |
| 8                | 1.49 | 1.17 | .96  | .81  | .70  | .62  | .55 | .50 | .46 |
| 9                | 1.50 | 1.18 | .97  | .82  | .71  | .62  | .56 | .51 | .47 |
| 10               | 1.52 | 1.20 | .98  | .83  | .72  | .63  | .57 | .52 | .47 |
| 11               | 1.54 | 1.21 | .99  | .84  | .73  | .64  | .58 | .52 | .48 |
| 12               | 1.56 | 1.23 | 1.00 | .85  | .74  | .65  | .59 | .53 | .49 |
| 13               | 1.58 | 1.25 | 1.02 | .86  | .75  | .66  | .59 | .54 | .49 |
| 14               | 1.60 | 1.26 | 1.03 | .87  | .76  | .67  | .60 | .55 | .50 |
| 15               | 1.62 | 1.28 | 1.05 | .89  | .77  | .68  | .61 | .56 | .51 |
| 16               | 1.64 | 1.30 | 1.06 | .90  | .78  | .69  | .62 | .56 | .52 |
| 17               | 1.66 | 1.31 | 1.08 | .91  | .79  | .70  | .63 | .57 | .52 |
| 18               | 1.68 | 1.33 | 1.09 | .92  | .80  | .71  | .64 | .58 | .53 |
| 19               | 1.70 | 1.34 | 1.10 | .93  | .81  | .72  | .65 | .59 | .54 |
| 20               | 1.72 | 1.36 | 1.11 | .95  | .82  | .73  | .65 | .59 | .54 |

| $n \backslash t$ | 11  | 12  | 13  | 14  | 15  | 16  | 17  | 18  | 19  | 20  |
|------------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 2                | .66 | .63 | .58 | .50 | .47 | .44 | .42 | .40 | .38 | .36 |
| 3                | .47 | .43 | .40 | .38 | .36 | .33 | .32 | .30 | .29 | .27 |
| 4                | .43 | .40 | .37 | .35 | .33 | .31 | .29 | .28 | .27 | .25 |
| 5                | .42 | .39 | .36 | .34 | .32 | .30 | .29 | .27 | .26 | .25 |
| 6                | .42 | .39 | .36 | .34 | .32 | .30 | .29 | .27 | .26 | .25 |
| 7                | .42 | .39 | .36 | .34 | .32 | .30 | .29 | .28 | .26 | .25 |
| 8                | .42 | .39 | .37 | .35 | .33 | .31 | .29 | .28 | .27 | .25 |
| 9                | .43 | .40 | .37 | .35 | .33 | .31 | .30 | .28 | .27 | .26 |
| 10               | .44 | .41 | .38 | .35 | .34 | .32 | .30 | .29 | .27 | .26 |
| 11               | .44 | .41 | .38 | .36 | .34 | .32 | .31 | .29 | .28 | .27 |
| 12               | .45 | .42 | .39 | .37 | .35 | .33 | .31 | .30 | .28 | .27 |
| 13               | .46 | .42 | .40 | .37 | .35 | .33 | .32 | .30 | .29 | .27 |
| 14               | .46 | .43 | .40 | .38 | .36 | .34 | .32 | .31 | .29 | .28 |
| 15               | .47 | .44 | .41 | .38 | .36 | .34 | .33 | .31 | .30 | .28 |
| 16               | .48 | .44 | .41 | .39 | .37 | .35 | .33 | .31 | .30 | .29 |
| 17               | .48 | .45 | .42 | .39 | .37 | .35 | .33 | .32 | .30 | .29 |
| 18               | .49 | .46 | .43 | .40 | .38 | .36 | .34 | .32 | .31 | .30 |
| 19               | .50 | .46 | .43 | .40 | .38 | .36 | .34 | .33 | .31 | .30 |
| 20               | .50 | .47 | .44 | .41 | .39 | .37 | .35 | .33 | .32 | .30 |

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## TABLES

TABLE A-15 (Continued). CRITICAL VALUES OF  $L$  FOR LINK-WALLACE TEST

$\alpha = .01$

 $t$  = number of groups = number of ranges

| $n \backslash t$ | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | 10  |
|------------------|------|------|------|------|------|------|------|------|-----|
| 2                | 7.92 | 4.42 | 2.96 | 2.06 | 1.69 | 1.39 | 1.20 | 1.03 | .91 |
| 3                | 3.14 | 2.14 | 1.57 | 1.25 | 1.04 | .89  | .78  | .69  | .62 |
| 4                | 2.47 | 1.74 | 1.33 | 1.08 | .91  | .78  | .69  | .62  | .56 |
| 5                | 2.24 | 1.60 | 1.24 | 1.02 | .86  | .75  | .66  | .59  | .54 |
| 6                | 2.14 | 1.55 | 1.21 | .99  | .85  | .74  | .65  | .59  | .53 |
| 7                | 2.10 | 1.53 | 1.21 | .99  | .84  | .74  | .65  | .59  | .53 |
| 8                | 2.08 | 1.52 | 1.21 | .99  | .85  | .74  | .66  | .59  | .54 |
| 9                | 2.09 | 1.53 | 1.22 | 1.00 | .85  | .75  | .66  | .60  | .54 |
| 10               | 2.10 | 1.55 | 1.23 | 1.01 | .86  | .75  | .67  | .61  | .55 |
| 11               | 2.11 | 1.56 | 1.24 | 1.02 | .88  | .77  | .68  | .61  | .56 |
| 12               | 2.13 | 1.58 | 1.25 | 1.03 | .89  | .78  | .69  | .62  | .57 |
| 13               | 2.15 | 1.60 | 1.27 | 1.05 | .90  | .79  | .70  | .63  | .58 |
| 14               | 2.18 | 1.62 | 1.28 | 1.06 | .91  | .80  | .71  | .64  | .58 |
| 15               | 2.20 | 1.64 | 1.30 | 1.08 | .92  | .81  | .72  | .65  | .59 |
| 16               | 2.22 | 1.65 | 1.31 | 1.09 | .93  | .82  | .73  | .66  | .60 |
| 17               | 2.24 | 1.67 | 1.33 | 1.11 | .95  | .83  | .74  | .67  | .61 |
| 18               | 2.27 | 1.69 | 1.34 | 1.12 | .96  | .84  | .75  | .68  | .62 |
| 19               | 2.30 | 1.71 | 1.36 | 1.14 | .97  | .85  | .76  | .68  | .62 |
| 20               | 2.32 | 1.73 | 1.38 | 1.15 | .98  | .86  | .77  | .69  | .63 |

| $n \backslash t$ | 11  | 12  | 13  | 14  | 15  | 16  | 17  | 18  | 19  | 20  |
|------------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 2                | .82 | .75 | .68 | .63 | .59 | .55 | .51 | .48 | .46 | .43 |
| 3                | .57 | .52 | .48 | .45 | .42 | .39 | .37 | .35 | .34 | .32 |
| 4                | .51 | .47 | .44 | .41 | .38 | .36 | .34 | .32 | .31 | .29 |
| 5                | .49 | .46 | .42 | .40 | .37 | .35 | .33 | .31 | .30 | .29 |
| 6                | .49 | .45 | .42 | .39 | .37 | .35 | .33 | .31 | .30 | .28 |
| 7                | .49 | .45 | .42 | .40 | .37 | .35 | .33 | .32 | .30 | .29 |
| 8                | .50 | .46 | .43 | .40 | .37 | .35 | .33 | .32 | .30 | .29 |
| 9                | .50 | .46 | .43 | .40 | .38 | .36 | .34 | .32 | .31 | .29 |
| 10               | .51 | .47 | .44 | .41 | .38 | .36 | .34 | .33 | .31 | .30 |
| 11               | .51 | .48 | .44 | .42 | .39 | .37 | .35 | .33 | .32 | .30 |
| 12               | .52 | .48 | .45 | .42 | .40 | .37 | .35 | .34 | .32 | .31 |
| 13               | .53 | .49 | .46 | .43 | .40 | .38 | .36 | .34 | .33 | .31 |
| 14               | .54 | .50 | .46 | .43 | .41 | .39 | .37 | .35 | .33 | .32 |
| 15               | .54 | .50 | .47 | .44 | .41 | .39 | .37 | .35 | .34 | .32 |
| 16               | .55 | .51 | .48 | .45 | .42 | .40 | .38 | .36 | .34 | .32 |
| 17               | .56 | .52 | .48 | .45 | .43 | .40 | .38 | .36 | .34 | .33 |
| 18               | .57 | .53 | .49 | .46 | .43 | .41 | .39 | .37 | .35 | .33 |
| 19               | .57 | .53 | .50 | .46 | .44 | .41 | .39 | .37 | .35 | .34 |
| 20               | .58 | .54 | .50 | .47 | .44 | .42 | .40 | .38 | .36 | .34 |

## TABLES

TABLE A-16. PERCENTAGE POINTS OF THE EXTREME STUDENTIZED DEVIATE FROM SAMPLE MEAN,

$$t_n = (X_n - \bar{X})/s, \text{ (or) } t_1 = (\bar{X} - X_1)/s,$$

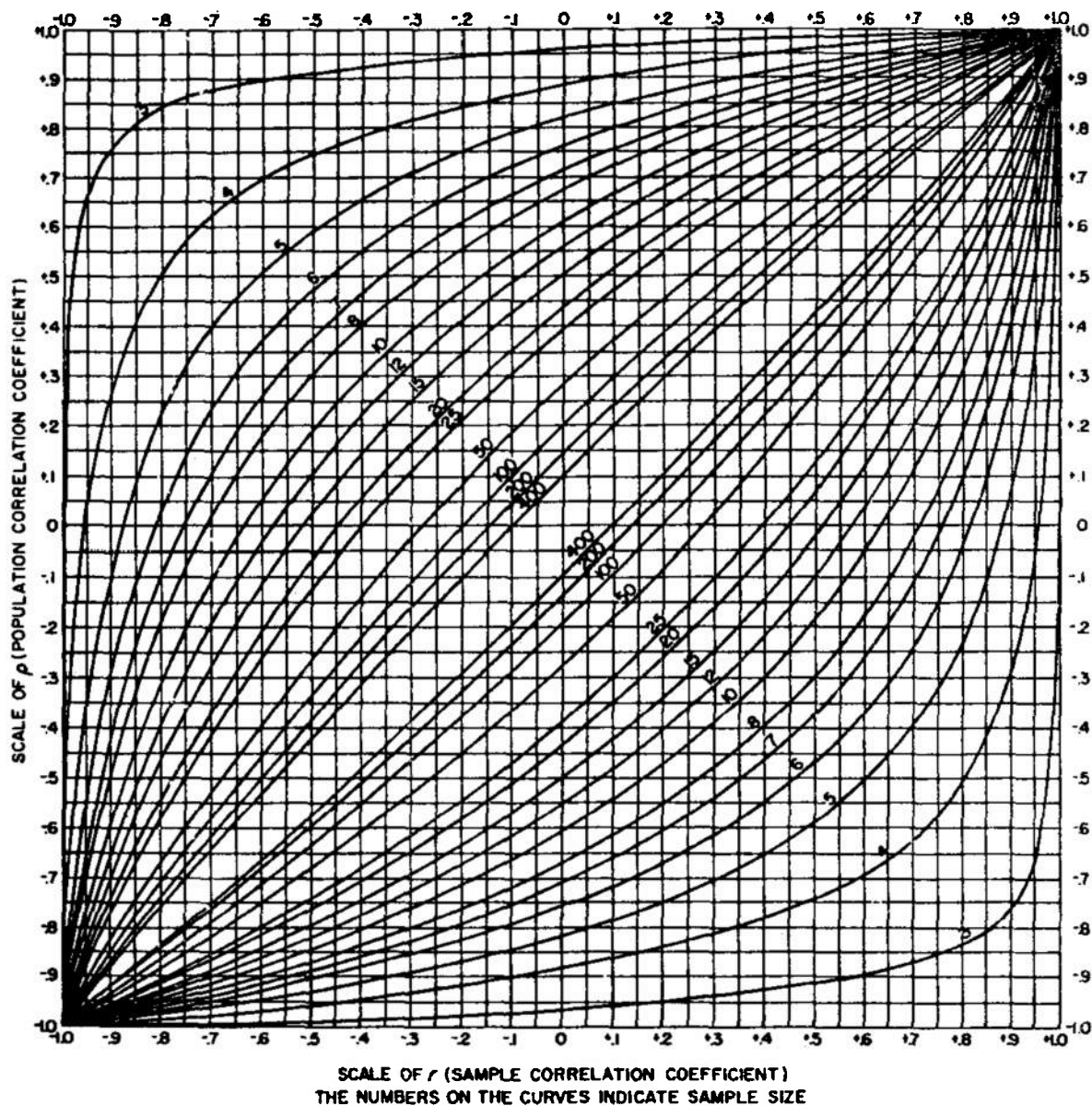
This table is to be used with  $s$ , an *external* estimate of  $\sigma$ , based on  $\nu$  degrees of freedom, not with the  $s$  computed from the sample in hand.

| $\nu$    | $\alpha = .05$ |      |      |      |      |      |      |      | $\alpha = .01$ |      |      |      |      |      |      |      |
|----------|----------------|------|------|------|------|------|------|------|----------------|------|------|------|------|------|------|------|
|          | 3              | 4    | 5    | 6    | 7    | 8    | 9    | 12   | 3              | 4    | 5    | 6    | 7    | 8    | 9    | 12   |
| 10       | 2.01           | 2.27 | 2.46 | 2.60 | 2.72 | 2.81 | 2.89 | 3.08 | 2.78           | 3.10 | 3.32 | 3.48 | 3.62 | 3.73 | 3.82 | 4.04 |
| 11       | 1.98           | 2.24 | 2.42 | 2.56 | 2.67 | 2.76 | 2.84 | 3.03 | 2.72           | 3.02 | 3.24 | 3.39 | 3.52 | 3.63 | 3.72 | 3.93 |
| 12       | 1.96           | 2.21 | 2.39 | 2.52 | 2.63 | 2.72 | 2.80 | 2.98 | 2.67           | 2.96 | 3.17 | 3.32 | 3.45 | 3.55 | 3.64 | 3.84 |
| 13       | 1.94           | 2.19 | 2.36 | 2.50 | 2.60 | 2.69 | 2.76 | 2.94 | 2.63           | 2.92 | 3.12 | 3.27 | 3.38 | 3.48 | 3.57 | 3.76 |
| 14       | 1.93           | 2.17 | 2.34 | 2.47 | 2.57 | 2.66 | 2.74 | 2.91 | 2.60           | 2.88 | 3.07 | 3.22 | 3.33 | 3.43 | 3.51 | 3.70 |
| 15       | 1.91           | 2.15 | 2.32 | 2.45 | 2.55 | 2.64 | 2.71 | 2.88 | 2.57           | 2.84 | 3.03 | 3.17 | 3.29 | 3.38 | 3.46 | 3.65 |
| 16       | 1.90           | 2.14 | 2.31 | 2.43 | 2.53 | 2.62 | 2.69 | 2.86 | 2.54           | 2.81 | 3.00 | 3.14 | 3.25 | 3.34 | 3.42 | 3.60 |
| 17       | 1.89           | 2.13 | 2.29 | 2.42 | 2.52 | 2.60 | 2.67 | 2.84 | 2.52           | 2.79 | 2.97 | 3.11 | 3.22 | 3.31 | 3.38 | 3.56 |
| 18       | 1.88           | 2.11 | 2.28 | 2.40 | 2.50 | 2.58 | 2.65 | 2.82 | 2.50           | 2.77 | 2.95 | 3.08 | 3.19 | 3.28 | 3.35 | 3.53 |
| 19       | 1.87           | 2.11 | 2.27 | 2.39 | 2.49 | 2.57 | 2.64 | 2.80 | 2.49           | 2.75 | 2.93 | 3.06 | 3.16 | 3.25 | 3.33 | 3.50 |
| 20       | 1.87           | 2.10 | 2.26 | 2.38 | 2.47 | 2.56 | 2.63 | 2.78 | 2.47           | 2.73 | 2.91 | 3.04 | 3.14 | 3.23 | 3.30 | 3.47 |
| 24       | 1.84           | 2.07 | 2.23 | 2.34 | 2.44 | 2.52 | 2.58 | 2.74 | 2.42           | 2.68 | 2.84 | 2.97 | 3.07 | 3.16 | 3.23 | 3.38 |
| 30       | 1.82           | 2.04 | 2.20 | 2.31 | 2.40 | 2.48 | 2.54 | 2.69 | 2.38           | 2.62 | 2.79 | 2.91 | 3.01 | 3.08 | 3.15 | 3.30 |
| 40       | 1.80           | 2.02 | 2.17 | 2.28 | 2.37 | 2.44 | 2.50 | 2.65 | 2.34           | 2.57 | 2.73 | 2.85 | 2.94 | 3.02 | 3.08 | 3.22 |
| 60       | 1.78           | 1.99 | 2.14 | 2.25 | 2.33 | 2.41 | 2.47 | 2.61 | 2.29           | 2.52 | 2.68 | 2.79 | 2.88 | 2.95 | 3.01 | 3.15 |
| 120      | 1.76           | 1.96 | 2.11 | 2.22 | 2.30 | 2.37 | 2.43 | 2.57 | 2.25           | 2.48 | 2.62 | 2.73 | 2.82 | 2.89 | 2.95 | 3.08 |
| $\infty$ | 1.74           | 1.94 | 2.08 | 2.18 | 2.27 | 2.33 | 2.39 | 2.52 | 2.22           | 2.43 | 2.57 | 2.68 | 2.76 | 2.83 | 2.88 | 3.01 |

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## TABLES

TABLE A-17. CONFIDENCE BELTS FOR THE CORRELATION COEFFICIENT  
(CONFIDENCE COEFFICIENT .95)



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TABLE A-18. WEIGHTING COEFFICIENTS FOR PROBIT ANALYSIS

| $\gamma$ | 0.0   | 0.1   | 0.2   | 0.3   | 0.4   | 0.5   | 0.6   | 0.7   | 0.8   | 0.9   |
|----------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1        | 0.001 | 0.001 | 0.001 | 0.002 | 0.002 | 0.003 | 0.005 | 0.006 | 0.008 | 0.011 |
| 2        | 0.015 | 0.019 | 0.025 | 0.031 | 0.040 | 0.050 | 0.062 | 0.076 | 0.092 | 0.110 |
| 3        | 0.131 | 0.154 | 0.180 | 0.208 | 0.238 | 0.269 | 0.302 | 0.336 | 0.370 | 0.405 |
| 4        | 0.439 | 0.471 | 0.503 | 0.532 | 0.558 | 0.581 | 0.601 | 0.616 | 0.627 | 0.634 |
| 5        | 0.637 | 0.634 | 0.627 | 0.616 | 0.601 | 0.581 | 0.558 | 0.532 | 0.503 | 0.471 |
| 6        | 0.439 | 0.405 | 0.370 | 0.336 | 0.302 | 0.269 | 0.238 | 0.208 | 0.180 | 0.154 |
| 7        | 0.131 | 0.110 | 0.092 | 0.076 | 0.062 | 0.050 | 0.040 | 0.031 | 0.025 | 0.019 |
| 8        | 0.015 | 0.011 | 0.008 | 0.006 | 0.005 | 0.003 | 0.002 | 0.002 | 0.001 | 0.001 |

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## TABLES

TABLE A-19. MAXIMUM AND MINIMUM WORKING PROBITS AND RANGE

| Expected Probit Y | Minimum Working Probit $y_0$ | Range 1/Z | Maximum Working Probit $y_{100}$ | Expected Probit Y |
|-------------------|------------------------------|-----------|----------------------------------|-------------------|
| 1.1               | 0.8579                       | 5034      | 9.1421                           | 8.9               |
| 1.2               | 0.9522                       | 3425      | 9.0478                           | 8.8               |
| 1.3               | 1.0462                       | 2354      | 8.9538                           | 8.7               |
| 1.4               | 1.1400                       | 1634      | 8.8600                           | 8.6               |
| 1.5               | 1.2334                       | 1146      | 8.7666                           | 8.5               |
| 1.6               | 1.3266                       | 811.5     | 8.6734                           | 8.4               |
| 1.7               | 1.4194                       | 580.5     | 8.5806                           | 8.3               |
| 1.8               | 1.5118                       | 419.4     | 8.4882                           | 8.2               |
| 1.9               | 1.6038                       | 306.1     | 8.3962                           | 8.1               |
| 2.0               | 1.6954                       | 225.6     | 8.3046                           | 8.0               |
| 2.1               | 1.7866                       | 168.00    | 8.2134                           | 7.9               |
| 2.2               | 1.8772                       | 126.34    | 8.1228                           | 7.8               |
| 2.3               | 1.9673                       | 95.96     | 8.0327                           | 7.7               |
| 2.4               | 2.0568                       | 73.62     | 7.9432                           | 7.6               |
| 2.5               | 2.1457                       | 57.05     | 7.8543                           | 7.5               |
| 2.6               | 2.2339                       | 44.654    | 7.7661                           | 7.4               |
| 2.7               | 2.3214                       | 35.302    | 7.6786                           | 7.3               |
| 2.8               | 2.4081                       | 28.189    | 7.5919                           | 7.2               |
| 2.9               | 2.4938                       | 22.736    | 7.5062                           | 7.1               |
| 3.0               | 2.5786                       | 18.522    | 7.4214                           | 7.0               |
| 3.1               | 2.6624                       | 15.240    | 7.3376                           | 6.9               |
| 3.2               | 2.7449                       | 12.666    | 7.2551                           | 6.8               |
| 3.3               | 2.8261                       | 10.633    | 7.1739                           | 6.7               |
| 3.4               | 2.9060                       | 9.015     | 7.0940                           | 6.6               |
| 3.5               | 2.9842                       | 7.721     | 7.0158                           | 6.5               |
| 3.6               | 3.0606                       | 6.6788    | 6.9394                           | 6.4               |
| 3.7               | 3.1351                       | 5.8354    | 6.8649                           | 6.3               |
| 3.8               | 3.2074                       | 5.1497    | 6.7926                           | 6.2               |
| 3.9               | 3.2773                       | 4.5903    | 6.7227                           | 6.1               |
| 4.0               | 3.3443                       | 4.1327    | 6.6557                           | 6.0               |
| 4.1               | 3.4083                       | 3.7582    | 6.5917                           | 5.9               |
| 4.2               | 3.4687                       | 3.4519    | 6.5313                           | 5.8               |
| 4.3               | 3.5251                       | 3.2025    | 6.4749                           | 5.7               |
| 4.4               | 3.5770                       | 3.0010    | 6.4230                           | 5.6               |
| 4.5               | 3.6236                       | 2.8404    | 6.3764                           | 5.5               |
| 4.6               | 3.6643                       | 2.7154    | 6.3357                           | 5.4               |
| 4.7               | 3.6982                       | 2.6220    | 6.3018                           | 5.3               |
| 4.8               | 3.7241                       | 2.5573    | 6.2759                           | 5.2               |
| 4.9               | 3.7407                       | 2.5192    | 6.2593                           | 5.1               |
| 5.0               | 3.7467                       | 2.5066    | 6.2533                           | 5.0               |

Discrepancies between the source table and some other tables were noted in the entries for  $y_0$  corresponding to  $Y = 1.5$  and  $Y = 2.6$ . These two values were recalculated and altered from the source table in the last place.

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## TABLES

TABLE A-20. FACTORS FOR COMPUTING TWO-SIDED CONFIDENCE LIMITS FOR  $\sigma$ 

| Degrees of Freedom<br>$\nu$ | $\alpha = .05$ |       | $\alpha = .01$ |       | $\alpha = .001$ |       |
|-----------------------------|----------------|-------|----------------|-------|-----------------|-------|
|                             | $B_U$          | $B_L$ | $B_U$          | $B_L$ | $B_U$           | $B_L$ |
| 1                           | 17.79          | .3576 | 86.31          | .2969 | 844.4           | .2480 |
| 2                           | 4.859          | .4581 | 10.70          | .3879 | 33.29           | .3291 |
| 3                           | 3.183          | .5178 | 5.449          | .4453 | 11.65           | .3824 |
| 4                           | 2.567          | .5590 | 3.892          | .4865 | 6.938           | .4218 |
| 5                           | 2.248          | .5899 | 3.175          | .5182 | 5.085           | .4529 |
| 6                           | 2.052          | .6143 | 2.764          | .5437 | 4.128           | .4784 |
| 7                           | 1.918          | .6344 | 2.498          | .5650 | 3.551           | .5000 |
| 8                           | 1.820          | .6513 | 2.311          | .5830 | 3.167           | .5186 |
| 9                           | 1.746          | .6657 | 2.173          | .5987 | 2.894           | .5348 |
| 10                          | 1.686          | .6784 | 2.065          | .6125 | 2.689           | .5492 |
| 11                          | 1.638          | .6896 | 1.980          | .6248 | 2.530           | .5621 |
| 12                          | 1.598          | .6995 | 1.909          | .6358 | 2.402           | .5738 |
| 13                          | 1.564          | .7084 | 1.851          | .6458 | 2.298           | .5845 |
| 14                          | 1.534          | .7166 | 1.801          | .6549 | 2.210           | .5942 |
| 15                          | 1.509          | .7240 | 1.758          | .6632 | 2.136           | .6032 |
| 16                          | 1.486          | .7308 | 1.721          | .6710 | 2.073           | .6116 |
| 17                          | 1.466          | .7372 | 1.688          | .6781 | 2.017           | .6193 |
| 18                          | 1.448          | .7430 | 1.658          | .6848 | 1.968           | .6266 |
| 19                          | 1.432          | .7484 | 1.632          | .6909 | 1.925           | .6333 |
| 20                          | 1.417          | .7535 | 1.609          | .6968 | 1.886           | .6397 |
| 21                          | 1.404          | .7582 | 1.587          | .7022 | 1.851           | .6457 |
| 22                          | 1.391          | .7627 | 1.568          | .7074 | 1.820           | .6514 |
| 23                          | 1.380          | .7669 | 1.550          | .7122 | 1.791           | .6568 |
| 24                          | 1.370          | .7709 | 1.533          | .7169 | 1.765           | .6619 |
| 25                          | 1.360          | .7747 | 1.518          | .7212 | 1.741           | .6668 |
| 26                          | 1.351          | .7783 | 1.504          | .7253 | 1.719           | .6713 |
| 27                          | 1.343          | .7817 | 1.491          | .7293 | 1.698           | .6758 |
| 28                          | 1.335          | .7849 | 1.479          | .7331 | 1.679           | .6800 |
| 29                          | 1.327          | .7880 | 1.467          | .7367 | 1.661           | .6841 |
| 30                          | 1.321          | .7909 | 1.457          | .7401 | 1.645           | .6880 |
| 31                          | 1.314          | .7937 | 1.447          | .7434 | 1.629           | .6917 |
| 32                          | 1.308          | .7964 | 1.437          | .7467 | 1.615           | .6953 |
| 33                          | 1.302          | .7990 | 1.428          | .7497 | 1.601           | .6987 |
| 34                          | 1.296          | .8015 | 1.420          | .7526 | 1.588           | .7020 |
| 35                          | 1.291          | .8039 | 1.412          | .7554 | 1.576           | .7052 |
| 36                          | 1.286          | .8062 | 1.404          | .7582 | 1.564           | .7083 |
| 37                          | 1.281          | .8085 | 1.397          | .7608 | 1.553           | .7113 |
| 38                          | 1.277          | .8106 | 1.390          | .7633 | 1.543           | .7141 |
| 39                          | 1.272          | .8126 | 1.383          | .7658 | 1.533           | .7169 |
| 40                          | 1.268          | .8146 | 1.377          | .7681 | 1.523           | .7197 |
| 41                          | 1.264          | .8166 | 1.371          | .7705 | 1.515           | .7223 |
| 42                          | 1.260          | .8184 | 1.365          | .7727 | 1.506           | .7248 |
| 43                          | 1.257          | .8202 | 1.360          | .7748 | 1.498           | .7273 |
| 44                          | 1.253          | .8220 | 1.355          | .7769 | 1.490           | .7297 |
| 45                          | 1.249          | .8237 | 1.349          | .7789 | 1.482           | .7320 |
| 46                          | 1.246          | .8253 | 1.345          | .7809 | 1.475           | .7342 |
| 47                          | 1.243          | .8269 | 1.340          | .7828 | 1.468           | .7364 |
| 48                          | 1.240          | .8285 | 1.335          | .7847 | 1.462           | .7386 |
| 49                          | 1.237          | .8300 | 1.331          | .7864 | 1.455           | .7407 |
| 50                          | 1.234          | .8314 | 1.327          | .7882 | 1.449           | .7427 |

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## TABLES

TABLE A-20 (Continued). FACTORS FOR COMPUTING TWO-SIDED CONFIDENCE LIMITS FOR  $\sigma$ 

| Degrees of Freedom $\nu$ | $\alpha = .05$ |       | $\alpha = .01$ |       | $\alpha = .001$ |       |
|--------------------------|----------------|-------|----------------|-------|-----------------|-------|
|                          | $B_U$          | $B_L$ | $B_U$          | $B_L$ | $B_U$           | $B_L$ |
| 51                       | 1.232          | .8329 | 1.323          | .7899 | 1.443           | .7446 |
| 52                       | 1.229          | .8343 | 1.319          | .7916 | 1.437           | .7466 |
| 53                       | 1.226          | .8356 | 1.315          | .7932 | 1.432           | .7485 |
| 54                       | 1.224          | .8370 | 1.311          | .7949 | 1.426           | .7503 |
| 55                       | 1.221          | .8383 | 1.308          | .7964 | 1.421           | .7521 |
| 56                       | 1.219          | .8395 | 1.304          | .7979 | 1.416           | .7539 |
| 57                       | 1.217          | .8408 | 1.301          | .7994 | 1.411           | .7556 |
| 58                       | 1.214          | .8420 | 1.298          | .8008 | 1.406           | .7573 |
| 59                       | 1.212          | .8431 | 1.295          | .8022 | 1.402           | .7589 |
| 60                       | 1.210          | .8443 | 1.292          | .8036 | 1.397           | .7605 |
| 61                       | 1.208          | .8454 | 1.289          | .8050 | 1.393           | .7621 |
| 62                       | 1.206          | .8465 | 1.286          | .8063 | 1.389           | .7636 |
| 63                       | 1.204          | .8475 | 1.283          | .8076 | 1.385           | .7651 |
| 64                       | 1.202          | .8486 | 1.280          | .8088 | 1.381           | .7666 |
| 65                       | 1.200          | .8496 | 1.277          | .8101 | 1.377           | .7680 |
| 66                       | 1.199          | .8506 | 1.275          | .8113 | 1.374           | .7694 |
| 67                       | 1.197          | .8516 | 1.272          | .8125 | 1.370           | .7708 |
| 68                       | 1.195          | .8525 | 1.270          | .8137 | 1.366           | .7722 |
| 69                       | 1.194          | .8535 | 1.268          | .8148 | 1.363           | .7735 |
| 70                       | 1.192          | .8544 | 1.265          | .8159 | 1.360           | .7749 |
| 71                       | 1.190          | .8553 | 1.263          | .8170 | 1.356           | .7761 |
| 72                       | 1.139          | .8562 | 1.261          | .8181 | 1.353           | .7774 |
| 73                       | 1.187          | .8571 | 1.259          | .8191 | 1.350           | .7787 |
| 74                       | 1.186          | .8580 | 1.257          | .8202 | 1.347           | .7799 |
| 75                       | 1.184          | .8588 | 1.255          | .8212 | 1.344           | .7811 |
| 76                       | 1.183          | .8596 | 1.253          | .8222 | 1.341           | .7822 |
| 77                       | 1.182          | .8604 | 1.251          | .8232 | 1.338           | .7834 |
| 78                       | 1.181          | .8612 | 1.249          | .8242 | 1.336           | .7845 |
| 79                       | 1.179          | .8620 | 1.247          | .8252 | 1.333           | .7856 |
| 80                       | 1.178          | .8627 | 1.245          | .8261 | 1.330           | .7868 |
| 81                       | 1.176          | .8635 | 1.243          | .8270 | 1.328           | .7878 |
| 82                       | 1.176          | .8642 | 1.241          | .8279 | 1.325           | .7889 |
| 83                       | 1.174          | .8650 | 1.239          | .8288 | 1.323           | .7899 |
| 84                       | 1.173          | .8657 | 1.238          | .8297 | 1.320           | .7909 |
| 85                       | 1.172          | .8664 | 1.236          | .8305 | 1.318           | .7920 |
| 86                       | 1.171          | .8671 | 1.235          | .8314 | 1.316           | .7930 |
| 87                       | 1.170          | .8678 | 1.233          | .8322 | 1.313           | .7939 |
| 88                       | 1.168          | .8684 | 1.231          | .8331 | 1.311           | .7949 |
| 89                       | 1.167          | .8691 | 1.230          | .8338 | 1.309           | .7959 |
| 90                       | 1.166          | .8697 | 1.228          | .8346 | 1.307           | .7968 |
| 91                       | 1.165          | .8704 | 1.227          | .8354 | 1.305           | .7977 |
| 92                       | 1.164          | .8710 | 1.225          | .8362 | 1.303           | .7987 |
| 93                       | 1.163          | .8716 | 1.224          | .8370 | 1.301           | .7996 |
| 94                       | 1.162          | .8722 | 1.222          | .8377 | 1.298           | .8004 |
| 95                       | 1.161          | .8729 | 1.221          | .8385 | 1.297           | .8013 |
| 96                       | 1.160          | .8734 | 1.219          | .8392 | 1.295           | .8022 |
| 97                       | 1.159          | .8741 | 1.218          | .8399 | 1.293           | .8031 |
| 98                       | 1.158          | .8746 | 1.217          | .8406 | 1.291           | .8039 |
| 99                       | 1.158          | .8752 | 1.216          | .8413 | 1.289           | .8047 |
| 100                      | 1.157          | .8757 | 1.214          | .8420 | 1.288           | .8055 |

## TABLES

TABLE A-21. FACTORS FOR COMPUTING ONE-SIDED CONFIDENCE LIMITS FOR  $\sigma$ 

| Degrees of Freedom<br>$\nu$ | $A_{.05}$ | $A_{.95}$ | $A_{.025}$ | $A_{.975}$ | $A_{.01}$ | $A_{.99}$ | $A_{.005}$ | $A_{.995}$ |
|-----------------------------|-----------|-----------|------------|------------|-----------|-----------|------------|------------|
| 1                           | .5108     | 15.947    | .4461      | 31.910     | .3882     | 79.786    | .3562      | 159.576    |
| 2                           | .5778     | 4.415     | .5207      | 6.285      | .4660     | 9.975     | .4344      | 14.124     |
| 3                           | .6196     | 2.920     | .5665      | 3.729      | .5142     | 5.111     | .4834      | 6.467      |
| 4                           | .6493     | 2.372     | .5892      | 2.874      | .5489     | 3.669     | .5188      | 4.396      |
| 5                           | .6721     | 2.089     | .6242      | 2.453      | .5757     | 3.003     | .5464      | 3.485      |
| 6                           | .6903     | 1.915     | .6444      | 2.202      | .5974     | 2.623     | .5688      | 2.980      |
| 7                           | .7054     | 1.797     | .6612      | 2.035      | .6155     | 2.377     | .5875      | 2.660      |
| 8                           | .7183     | 1.711     | .6754      | 1.916      | .6310     | 2.204     | .6037      | 2.439      |
| 9                           | .7293     | 1.645     | .6878      | 1.826      | .6445     | 2.076     | .6177      | 2.278      |
| 10                          | .7391     | 1.593     | .6987      | 1.755      | .6564     | 1.977     | .6301      | 2.154      |
| 11                          | .7477     | 1.551     | .7084      | 1.698      | .6670     | 1.898     | .6412      | 2.056      |
| 12                          | .7554     | 1.515     | .7171      | 1.651      | .6765     | 1.833     | .6512      | 1.976      |
| 13                          | .7624     | 1.485     | .7250      | 1.611      | .6852     | 1.779     | .6603      | 1.909      |
| 14                          | .7688     | 1.460     | .7321      | 1.577      | .6931     | 1.733     | .6686      | 1.854      |
| 15                          | .7747     | 1.437     | .7387      | 1.548      | .7004     | 1.694     | .6762      | 1.806      |
| 20                          | .7979     | 1.358     | .7650      | 1.444      | .7297     | 1.556     | .7071      | 1.640      |
| 25                          | .8149     | 1.308     | .7843      | 1.380      | .7511     | 1.473     | .7299      | 1.542      |
| 30                          | .8279     | 1.274     | .7991      | 1.337      | .7678     | 1.416     | .7477      | 1.475      |
| 40                          | .8470     | 1.228     | .8210      | 1.279      | .7925     | 1.343     | .7740      | 1.390      |
| 50                          | .8606     | 1.199     | .8367      | 1.243      | .8103     | 1.297     | .7931      | 1.337      |
| 60                          | .8710     | 1.179     | .8487      | 1.217      | .8239     | 1.265     | .8078      | 1.299      |
| 70                          | .8793     | 1.163     | .8583      | 1.198      | .8349     | 1.241     | .8196      | 1.272      |
| 80                          | .8861     | 1.151     | .8662      | 1.183      | .8439     | 1.222     | .8293      | 1.250      |
| 90                          | .8919     | 1.141     | .8728      | 1.171      | .8515     | 1.207     | .8376      | 1.233      |
| 100                         | .8968     | 1.133     | .8785      | 1.161      | .8581     | 1.195     | .8446      | 1.219      |

For large degrees of freedom, we may use the approximate formula:

$$A_p = \sqrt{2\nu} / (z_p + \sqrt{2\nu - 1}),$$

where  $z_p$  is found in Table A-2.

## TABLES

TABLE A-22. CONFIDENCE LIMITS FOR A PROPORTION (TWO-SIDED)

For confidence limits for  $n > 30$ , see Table A-24.Upper limits are in boldface. The observed proportion in a random sample is  $r/n$ 

| r      | 90%   |       |       | 95%   |       |       | 99% |       |        | r     | 90%   |       |       | 95%  |       |       | 99%   |       |  |
|--------|-------|-------|-------|-------|-------|-------|-----|-------|--------|-------|-------|-------|-------|------|-------|-------|-------|-------|--|
| n = 1  |       |       |       |       |       |       |     |       | n = 2  |       |       |       |       |      |       |       |       |       |  |
| 0      | 0     | .900  | 0     | .950  | 0     | .990  | 0   | 0     | .684   | 0     | .779  | 0     | .900  | 0    | .900  | 0     | .900  |       |  |
| 1      | .100  | 1     | .050  | 1     | .010  | 1     | 1   | .051  | .949   | .025+ | .975- | .005+ | .995- | .100 | 1     | .005+ | .995- |       |  |
| n = 3  |       |       |       |       |       |       |     |       | n = 4  |       |       |       |       |      |       |       |       |       |  |
| 0      | 0     | .539  | 0     | .632  | 0     | .768- | 0   | 0     | .500   | 0     | .527  | 0     | .684  | 0    | .500  | 0     | .527  |       |  |
| 1      | .085- | .594  | .017  | .665- | .008  | .941  | 1   | .028  | .930   | .018  | .751  | .008  | .959  | 1    | .028  | .930  | .018  | .751  |  |
| 2      | .196  | .999+ | .185+ | .983  | .059  | .997  | 2   | .143  | .857   | .098  | .902  | .042  | .958  | 2    | .143  | .857  | .098  | .902  |  |
| 3      | .464  | 1     | .368  | 1     | .215+ | 1     | 3   | .320  | .974   | .249  | .987  | .141  | .997  | 3    | .320  | .974  | .249  | .987  |  |
| n = 5  |       |       |       |       |       |       |     |       | n = 6  |       |       |       |       |      |       |       |       |       |  |
| 0      | 0     | .379  | 0     | .500  | 0     | .602  | 0   | 0     | .345-  | 0     | .462  | 0     | .536  | 0    | 0     | .345- | 0     | .462  |  |
| 1      | .021  | .621  | .010  | .657  | .002  | .778  | 1   | .017  | .542   | .009  | .598  | .002  | .706  | 1    | .017  | .542  | .009  | .598  |  |
| 2      | .112  | .753  | .076  | .811  | .033  | .894  | 2   | .098  | .697   | .065  | .729  | .027  | .827  | 2    | .098  | .697  | .065  | .729  |  |
| 3      | .247  | .888  | .189  | .924  | .106  | .997  | 3   | .201  | .799   | .153  | .847  | .085- | .915+ | 3    | .201  | .799  | .153  | .847  |  |
| 4      | .379  | .979  | .343  | .990  | .222  | .998  | 4   | .333  | .907   | .271  | .937  | .173  | .973  | 4    | .333  | .907  | .271  | .937  |  |
| 5      | .621  | 1     | .500  | 1     | .398  | 1     | 5   | .458  | .963   | .402  | .991  | .294  | .998  | 5    | .458  | .963  | .402  | .991  |  |
| n = 7  |       |       |       |       |       |       |     |       | n = 8  |       |       |       |       |      |       |       |       |       |  |
| 0      | 0     | .319  | 0     | .377  | 0     | .500  | 0   | 0     | .258-  | 0     | .315+ | 0     | .481  | 0    | 0     | .258- | 0     | .315+ |  |
| 1      | .015- | .590  | .007  | .554  | .001  | .643  | 1   | .013  | .418   | .006  | .509  | .001  | .590  | 1    | .013  | .418  | .006  | .509  |  |
| 2      | .079  | .684  | .053  | .659  | .023  | .764  | 2   | .069  | .582   | .046  | .655- | .020  | .797  | 2    | .069  | .582  | .046  | .655- |  |
| 3      | .170  | .721  | .129  | .775- | .071  | .858  | 3   | .147  | .749+  | .111  | .711  | .061  | .892  | 3    | .147  | .749+ | .111  | .711  |  |
| 4      | .279  | .830  | .225+ | .871  | .142  | .929  | 4   | .240  | .799   | .193  | .807  | .121  | .879  | 4    | .240  | .799  | .193  | .807  |  |
| 5      | .316  | .921  | .341  | .947  | .236  | .977  | 5   | .255- | .853   | .289  | .889  | .198  | .939  | 5    | .255- | .853  | .289  | .889  |  |
| 6      | .500  | .969+ | .446  | .995  | .357  | .999  | 6   | .418  | .931   | .315+ | .954  | .293  | .980  | 6    | .418  | .931  | .315+ | .954  |  |
| 7      | .684  | 1     | .623  | 1     | .500  | 1     | 7   | .582  | .987   | .500  | .994  | .410  | .999  | 7    | .582  | .987  | .500  | .994  |  |
| n = 9  |       |       |       |       |       |       |     |       | n = 10 |       |       |       |       |      |       |       |       |       |  |
| 0      | 0     | .232  | 0     | .299  | 0     | .402  | 0   | 0     | .222   | 0     | .297  | 0     | .379  | 0    | 0     | .222  | 0     | .297  |  |
| 1      | .012  | .391  | .006  | .443  | .001  | .598  | 1   | .010  | .352   | .005+ | .397  | .001  | .512  | 1    | .010  | .352  | .005+ | .397  |  |
| 2      | .061  | .915+ | .041  | .938  | .017  | .656  | 2   | .055- | .500   | .037  | .603  | .018  | .924  | 2    | .055- | .500  | .037  | .603  |  |
| 3      | .129  | .816  | .098  | .711  | .063  | .750  | 3   | .116  | .648   | .087  | .619  | .048  | .703  | 3    | .116  | .648  | .087  | .619  |  |
| 4      | .210  | .765  | .169  | .749  | .105+ | .829  | 4   | .188  | .669   | .150  | .733  | .098  | .782  | 4    | .188  | .669  | .150  | .733  |  |
| 5      | .232  | .796  | .251  | .831  | .171  | .899- | 5   | .222  | .778   | .222  | .778  | .160  | .850  | 5    | .222  | .778  | .222  | .778  |  |
| 6      | .390  | .871  | .289  | .902  | .250  | .947  | 6   | .341  | .812   | .267  | .850  | .218  | .907  | 6    | .341  | .812  | .267  | .850  |  |
| 7      | .485- | .939  | .442  | .959  | .344  | .983  | 7   | .382  | .884   | .381  | .913  | .297  | .952  | 7    | .382  | .884  | .381  | .913  |  |
| 8      | .609  | .983  | .557  | .994  | .402  | .999  | 8   | .500  | .945+  | .397  | .963  | .376  | .984  | 8    | .500  | .945+ | .397  | .963  |  |
| 9      | .768  | 1     | .711  | 1     | .598  | 1     | 9   | .648  | .990   | .603  | .995- | .488  | .999  | 9    | .648  | .990  | .603  | .995- |  |
| n = 11 |       |       |       |       |       |       |     |       | n = 12 |       |       |       |       |      |       |       |       |       |  |
| 0      | 0     | .197  | 0     | .296  | 0     | .359  | 0   | 0     | .194   | 0     | .239  | 0     | .321  | 0    | 0     | .194  | 0     | .239  |  |
| 1      | .010  | .319+ | .005- | .399  | .001  | .500  | 1   | .009  | .294   | .004  | .346  | .001  | .445+ | 1    | .009  | .294  | .004  | .346  |  |
| 2      | .049  | .423  | .033  | .500  | .014  | .593  | 2   | .045+ | .398   | .030  | .450  | .013  | .555- | 2    | .045+ | .398  | .030  | .450  |  |
| 3      | .105- | .577  | .079  | .621  | .043  | .699  | 3   | .096  | .500   | .072  | .550  | .039  | .679  | 3    | .096  | .500  | .072  | .550  |  |
| 4      | .169  | .685- | .135+ | .667  | .084  | .738  | 4   | .154  | .592   | .123  | .694  | .078  | .698  | 4    | .154  | .592  | .123  | .694  |  |
| 5      | .197  | .999  | .200  | .796  | .134  | .806  | 5   | .184  | .799   | .181  | .709  | .121  | .765+ | 5    | .184  | .799  | .181  | .709  |  |
| 6      | .302  | .863  | .250  | .849  | .194  | .899  | 6   | .271  | .729   | .235  | .794  | .175- | .825+ | 6    | .271  | .729  | .235  | .794  |  |
| 7      | .315+ | .631  | .333  | .899- | .262  | .919  | 7   | .294  | .819   | .294  | .819  | .235- | .979  | 7    | .294  | .819  | .294  | .819  |  |
| 8      | .423  | .995+ | .369  | .921  | .340  | .997  | 8   | .398  | .846   | .346  | .877  | .302  | .924  | 8    | .398  | .846  | .346  | .877  |  |
| 9      | .577  | .991  | .500  | .967  | .407  | .999  | 9   | .500  | .904   | .450  | .928  | .321  | .961  | 9    | .500  | .904  | .450  | .928  |  |
| 10     | .685- | .990  | .631  | .999+ | .500  | .999  | 10  | .602  | .955-  | .550  | .970  | .445+ | .987  | 10   | .602  | .955- | .550  | .970  |  |
| 11     | .806  | 1     | .750  | 1     | .641  | 1     | 11  | .708  | .991   | .654  | .996  | .555- | .999  | 11   | .708  | .991  | .654  | .996  |  |
|        |       |       |       |       |       |       | 12  | .816  | 1      | .764  | 1     | .679  | 1     |      |       |       |       |       |  |

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## TABLES

TABLE A-22 (Continued). CONFIDENCE LIMITS FOR A PROPORTION (TWO-SIDED)

| r      | 90%  | 95%  | 99%  | r      | 90%  | 95%  | 99%  |
|--------|------|------|------|--------|------|------|------|
| n = 13 |      |      |      | n = 14 |      |      |      |
| 0      | 0    | .176 | 0    | 0      | .183 | 0    | .288 |
| 1      | .008 | .279 | .001 | 1      | .007 | .391 | .001 |
| 2      | .042 | .379 | .023 | 2      | .039 | .399 | .011 |
| 3      | .088 | .476 | .066 | 3      | .081 | .432 | .033 |
| 4      | .142 | .546 | .116 | 4      | .131 | .479 | .064 |
| 5      | .173 | .591 | .166 | 5      | .163 | .534 | .102 |
| 6      | .249 | .724 | .224 | 6      | .224 | .649 | .146 |
| 7      | .276 | .754 | .260 | 7      | .261 | .729 | .195 |
| 8      | .279 | .757 | .273 | 8      | .255 | .776 | .249 |
| 9      | .455 | .858 | .402 | 9      | .406 | .837 | .286 |
| 10     | .530 | .912 | .460 | 10     | .422 | .869 | .364 |
| 11     | .621 | .958 | .546 | 11     | .578 | .919 | .392 |
| 12     | .724 | .992 | .672 | 12     | .635 | .961 | .500 |
| 13     | .827 | 1    | .775 | 13     | .739 | .993 | .606 |
|        |      |      |      | 14     | .837 | 1    | .714 |
| n = 15 |      |      |      | n = 16 |      |      |      |
| 0      | 0    | .154 | 0    | 0      | .147 | 0    | .284 |
| 1      | .007 | .247 | .003 | 1      | .007 | .339 | .001 |
| 2      | .036 | .329 | .024 | 2      | .034 | .385 | .010 |
| 3      | .076 | .400 | .057 | 3      | .071 | .431 | .029 |
| 4      | .122 | .460 | .097 | 4      | .114 | .480 | .055 |
| 5      | .164 | .500 | .142 | 5      | .147 | .520 | .088 |
| 6      | .205 | .574 | .191 | 6      | .189 | .599 | .125 |
| 7      | .247 | .679 | .252 | 7      | .235 | .696 | .166 |
| 8      | .285 | .753 | .294 | 8      | .299 | .761 | .212 |
| 9      | .328 | .799 | .332 | 9      | .305 | .796 | .261 |
| 10     | .400 | .846 | .369 | 10     | .381 | .811 | .295 |
| 11     | .500 | .876 | .449 | 11     | .450 | .858 | .357 |
| 12     | .600 | .924 | .532 | 12     | .550 | .886 | .421 |
| 13     | .674 | .964 | .631 | 13     | .619 | .929 | .475 |
| 14     | .753 | .993 | .696 | 14     | .695 | .966 | .549 |
| 15     | .846 | 1    | .809 | 15     | .765 | .993 | .643 |
|        |      |      |      | 16     | .853 | 1    | .736 |
| n = 17 |      |      |      | n = 18 |      |      |      |
| 0      | 0    | .140 | 0    | 0      | .135 | 0    | .229 |
| 1      | .006 | .225 | .003 | 1      | .006 | .319 | .001 |
| 2      | .032 | .290 | .021 | 2      | .030 | .377 | .008 |
| 3      | .067 | .344 | .040 | 3      | .063 | .430 | .025 |
| 4      | .107 | .412 | .085 | 4      | .101 | .479 | .049 |
| 5      | .140 | .460 | .124 | 5      | .135 | .520 | .077 |
| 6      | .175 | .509 | .166 | 6      | .163 | .539 | .110 |
| 7      | .225 | .539 | .217 | 7      | .218 | .584 | .145 |
| 8      | .277 | .716 | .253 | 8      | .257 | .651 | .184 |
| 9      | .290 | .723 | .254 | 9      | .277 | .723 | .226 |
| 10     | .364 | .778 | .337 | 10     | .349 | .743 | .228 |
| 11     | .432 | .828 | .406 | 11     | .416 | .784 | .284 |
| 12     | .500 | .860 | .456 | 12     | .444 | .837 | .318 |
| 13     | .563 | .896 | .511 | 13     | .518 | .865 | .397 |
| 14     | .636 | .933 | .553 | 14     | .581 | .899 | .466 |
| 15     | .710 | .968 | .603 | 15     | .651 | .937 | .534 |
| 16     | .775 | .994 | .746 | 16     | .723 | .979 | .608 |
| 17     | .860 | 1    | .853 | 17     | .784 | .994 | .682 |
|        |      |      |      | 18     | .845 | 1    | .772 |
| n = 19 |      |      |      | n = 20 |      |      |      |
| 0      | 0    | .136 | 0    | 0      | .129 | 0    | .209 |
| 1      | .006 | .209 | .003 | 1      | .005 | .293 | .001 |
| 2      | .025 | .265 | .019 | 2      | .027 | .338 | .008 |
| 3      | .059 | .317 | .044 | 3      | .056 | .326 | .023 |
| 4      | .095 | .367 | .075 | 4      | .090 | .367 | .044 |
| 5      | .130 | .440 | .110 | 5      | .128 | .422 | .069 |
| 6      | .151 | .490 | .147 | 6      | .141 | .490 | .096 |
| 7      | .209 | .516 | .150 | 7      | .201 | .578 | .129 |
| 8      | .238 | .514 | .232 | 8      | .221 | .633 | .163 |
| 9      | .265 | .593 | .232 | 9      | .255 | .642 | .200 |
| 10     | .337 | .709 | .312 | 10     | .325 | .679 | .209 |
| 11     | .386 | .763 | .345 | 11     | .358 | .745 | .274 |
| 12     | .437 | .791 | .385 | 12     | .407 | .779 | .293 |
| 13     | .440 | .649 | .426 | 13     | .432 | .799 | .363 |
| 14     | .560 | .676 | .500 | 14     | .500 | .659 | .399 |
| 15     | .613 | .909 | .574 | 15     | .578 | .674 | .424 |
| 16     | .683 | .941 | .635 | 16     | .633 | .919 | .500 |
| 17     | .735 | .973 | .684 | 17     | .672 | .944 | .576 |
| 18     | .791 | .994 | .768 | 18     | .745 | .976 | .625 |
| 19     | .870 | 1    | .850 | 19     | .797 | .996 | .707 |
|        |      |      |      | 20     | .874 | 1    | .791 |

## TABLES

TABLE A-22 (Continued). CONFIDENCE LIMITS FOR A PROPORTION (TWO-SIDED)

| r      | 90%    | 95%    | 99%    | r      | 90%    | 95%    | 99%    |
|--------|--------|--------|--------|--------|--------|--------|--------|
| n = 21 |        |        |        | n = 22 |        |        |        |
| 0      | 0      | .123   | 0      | 0      | 0      | .123   | 0      |
| 1      | .005 + | .192   | .002   | 1      | .005 - | .182   | .002   |
| 2      | .026   | .246 - | .017   | 2      | .024   | .236   | .016   |
| 3      | .064   | .287   | .040   | 3      | .051   | .269   | .038   |
| 4      | .086   | .313   | .065   | 4      | .063   | .290   | .055   |
| 5      | .121   | .407   | .099   | 5      | .115 - | .393   | .094   |
| 6      | .180   | .468   | .182   | 6      | .118   | .444   | .128   |
| 7      | .191   | .542   | .187   | 7      | .181   | .500   | .132   |
| 8      | .192   | .585   | .197   | 8      | .182   | .554   | .187   |
| 9      | .245 - | .647   | .213   | 9      | .236   | .607   | .206 + |
| 10     | .306   | .683   | .276   | 10     | .289   | .660   | .260   |
| 11     | .307   | .684   | .277   | 11     | .290   | .710   | .264   |
| 12     | .353   | .785 + | .333   | 12     | .340   | .711   | .326   |
| 13     | .407   | .868   | .398   | 13     | .393   | .764   | .383   |
| 14     | .453   | .869   | .449   | 14     | .444   | .818   | .410   |
| 15     | .542   | .878   | .494   | 15     | .500   | .819   | .424   |
| 16     | .593   | .879   | .545 - | 16     | .556   | .884   | .500   |
| 17     | .647   | .914   | .602   | 17     | .607   | .928 + | .576   |
| 18     | .698   | .940   | .662   | 18     | .660   | .910   | .611   |
| 19     | .755 + | .974   | .723   | 19     | .711   | .949   | .674   |
| 20     | .808   | .990 - | .787   | 20     | .764   | .970   | .786   |
| 21     | .877   | 1      | .863   | 21     | .818   | .995 + | .795 - |
|        |        |        | 1      | 22     | .884   | 1      | .863   |
|        |        |        |        |        |        |        | 1      |
| n = 23 |        |        |        | n = 24 |        |        |        |
| 0      | 0      | .111   | 0      | 0      | 0      | .111   | 0      |
| 1      | .005 - | .174   | .002   | 1      | .004   | .165 + | .002   |
| 2      | .023   | .238   | .016   | 2      | .022   | .221   | .015 + |
| 3      | .040   | .274   | .037   | 3      | .047   | .264   | .035 - |
| 4      | .078   | .328   | .062   | 4      | .075 - | .317   | .069   |
| 5      | .110   | .361   | .090   | 5      | .106 - | .370   | .098   |
| 6      | .111   | .401   | .120   | 6      | .105 + | .422   | .115 - |
| 7      | .173   | .479   | .127   | 7      | .165 + | .440   | .122   |
| 8      | .174   | .522   | .178   | 8      | .165 + | .502   | .169   |
| 9      | .228   | .609   | .198   | 9      | .221   | .553   | .191   |
| 10     | .273   | .619   | .247   | 10     | .259   | .587   | .234   |
| 11     | .274   | .672   | .255 - | 11     | .284   | .639   | .246   |
| 12     | .325   | .730   | .317   | 12     | .317   | .683   | .308   |
| 13     | .381   | .737   | .360   | 13     | .370   | .736   | .339   |
| 14     | .481   | .772   | .361   | 14     | .413   | .741   | .347   |
| 15     | .478   | .826   | .409   | 15     | .447   | .779   | .396   |
| 16     | .521   | .827   | .457   | 16     | .448   | .835 - | .443   |
| 17     | .569   | .839   | .543   | 17     | .552   | .835 + | .500   |
| 18     | .619   | .890   | .591   | 18     | .577   | .898 - | .567   |
| 19     | .672   | .923   | .639   | 19     | .630   | .899 + | .604   |
| 20     | .726   | .981   | .683   | 20     | .683   | .925 + | .653   |
| 21     | .772   | .977   | .745 + | 21     | .736   | .983   | .692   |
| 22     | .826   | .990 + | .802   | 22     | .779   | .973   | .764   |
| 23     | .889   | 1      | .873   | 23     | .835 - | .996   | .809   |
|        |        |        | 1      | 24     | .895 - | 1      | .878   |
|        |        |        |        |        |        |        | 1      |
| n = 25 |        |        |        | n = 26 |        |        |        |
| 0      | 0      | .103   | 0      | 0      | 0      | .103   | 0      |
| 1      | .004   | .159   | .002   | 1      | .004   | .162   | .002   |
| 2      | .021   | .214   | .014   | 2      | .021   | .209   | .014   |
| 3      | .045 - | .260 - | .034   | 3      | .043   | .247   | .032   |
| 4      | .072   | .307   | .057   | 4      | .069   | .299   | .054   |
| 5      | .101   | .362   | .082   | 5      | .097   | .348   | .079   |
| 6      | .102   | .390   | .110   | 6      | .098   | .377   | .106   |
| 7      | .158   | .422   | .118   | 7      | .151   | .419   | .114   |
| 8      | .159   | .500   | .161   | 8      | .152   | .460   | .154   |
| 9      | .214   | .563   | .163 + | 9      | .209   | .540   | .180   |
| 10     | .246   | .616   | .222   | 10     | .233   | .581   | .212   |
| 11     | .255 - | .611   | .233   | 11     | .247   | .623   | .230   |
| 12     | .307   | .640   | .296   | 12     | .299   | .657   | .282   |
| 13     | .360   | .693   | .317   | 13     | .342   | .688   | .323   |
| 14     | .389   | .746 + | .356   | 14     | .343   | .701   | .325 + |
| 15     | .390   | .784   | .384   | 15     | .377   | .753   | .374   |
| 16     | .432   | .786   | .431   | 16     | .419   | .787   | .421   |
| 17     | .500   | .841   | .475 - | 17     | .460   | .791   | .458   |
| 18     | .568   | .842   | .525 + | 18     | .540   | .848   | .546   |
| 19     | .610   | .898   | .569   | 19     | .581   | .849   | .585 - |
| 20     | .638   | .899   | .616   | 20     | .623   | .902   | .579   |
| 21     | .693   | .928   | .664   | 21     | .657   | .903   | .628   |
| 22     | .745 + | .985 + | .697   | 22     | .701   | .931   | .675 - |
| 23     | .786   | .979   | .762   | 23     | .753   | .957   | .717   |
| 24     | .841   | .996   | .815 - | 24     | .791   | .979   | .770   |
| 25     | .898   | 1      | .882   | 25     | .848   | .998   | .820   |
|        |        |        | 1      | 26     | .902   | 1      | .886   |
|        |        |        |        |        |        |        | 1      |

## TABLES

TABLE A-22 (Continued). CONFIDENCE LIMITS FOR A PROPORTION (TWO-SIDED)

| r      | 90%  |      |      | 95%  |      |       | 99%  |       |        | r    | 90%  |      |      | 95%  |       |      | 99%   |  |  |
|--------|------|------|------|------|------|-------|------|-------|--------|------|------|------|------|------|-------|------|-------|--|--|
| n = 27 |      |      |      |      |      |       |      |       | n = 28 |      |      |      |      |      |       |      |       |  |  |
| 0      | 0    | .092 | 0    | .110 | 0    | .166  | 0    | .225  | 0      | 0    | .090 | 0    | .166 | 0    | .215  | 0    | .273  |  |  |
| 1      | .004 | .146 | .002 | .175 | .000 | .225  | .004 | .284  | .002   | .004 | .146 | .002 | .175 | .000 | .215  | .004 | .273  |  |  |
| 2      | .020 | .204 | .018 | .222 | .006 | .284  | .019 | .343  | .013   | .019 | .201 | .013 | .217 | .005 | .273  | .016 | .332  |  |  |
| 3      | .042 | .239 | .031 | .270 | .017 | .333  | .040 | .392  | .030   | .040 | .232 | .030 | .259 | .016 | .315  | .031 | .374  |  |  |
| 4      | .068 | .291 | .052 | .316 | .032 | .384  | .064 | .444  | .050   | .064 | .264 | .050 | .297 | .031 | .355  | .046 | .414  |  |  |
| 5      | .098 | .327 | .076 | .364 | .050 | .419  | .089 | .481  | .073   | .089 | .312 | .073 | .337 | .046 | .408  | .061 | .467  |  |  |
| 6      | .094 | .365 | .101 | .416 | .070 | .461  | .090 | .523  | .098   | .090 | .354 | .098 | .364 | .068 | .449  | .083 | .508  |  |  |
| 7      | .145 | .407 | .110 | .437 | .093 | .539  | .139 | .598  | .108   | .139 | .396 | .108 | .424 | .089 | .508  | .104 | .567  |  |  |
| 8      | .146 | .447 | .148 | .500 | .117 | .581  | .140 | .643  | .142   | .140 | .435 | .142 | .463 | .112 | .551  | .127 | .610  |  |  |
| 9      | .204 | .500 | .175 | .563 | .143 | .587  | .197 | .643  | .170   | .197 | .473 | .170 | .507 | .137 | .592  | .152 | .651  |  |  |
| 10     | .221 | .553 | .202 | .570 | .166 | .517  | .208 | .627  | .192   | .208 | .527 | .192 | .576 | .162 | .635  | .177 | .694  |  |  |
| 11     | .239 | .593 | .223 | .598 | .185 | .668  | .222 | .684  | .217   | .222 | .565 | .217 | .616 | .175 | .684  | .190 | .743  |  |  |
| 12     | .291 | .635 | .289 | .636 | .224 | .703  | .284 | .703  | .258   | .284 | .604 | .258 | .619 | .214 | .677  | .229 | .736  |  |  |
| 13     | .325 | .673 | .270 | .684 | .225 | .716  | .310 | .716  | .259   | .310 | .645 | .259 | .645 | .218 | .727  | .233 | .786  |  |  |
| 14     | .327 | .674 | .316 | .730 | .264 | .775  | .312 | .775  | .264   | .312 | .688 | .264 | .693 | .272 | .736  | .287 | .795  |  |  |
| 15     | .366 | .709 | .364 | .731 | .298 | .776  | .355 | .776  | .298   | .355 | .716 | .298 | .742 | .283 | .786  | .302 | .845  |  |  |
| 16     | .407 | .761 | .402 | .777 | .332 | .815  | .396 | .815  | .351   | .396 | .758 | .351 | .783 | .323 | .823  | .338 | .882  |  |  |
| 17     | .447 | .779 | .430 | .796 | .383 | .834  | .435 | .834  | .384   | .435 | .792 | .384 | .808 | .365 | .865  | .380 | .924  |  |  |
| 18     | .500 | .796 | .437 | .825 | .413 | .857  | .473 | .857  | .424   | .473 | .834 | .424 | .834 | .385 | .894  | .400 | .943  |  |  |
| 19     | .553 | .854 | .500 | .832 | .419 | .883  | .527 | .883  | .463   | .527 | .863 | .463 | .863 | .408 | .903  | .423 | .962  |  |  |
| 20     | .593 | .856 | .583 | .890 | .461 | .907  | .565 | .907  | .507   | .565 | .860 | .507 | .860 | .449 | .923  | .464 | .982  |  |  |
| 21     | .635 | .905 | .585 | .899 | .539 | .930  | .604 | .930  | .576   | .604 | .861 | .576 | .861 | .500 | .911  | .515 | .970  |  |  |
| 22     | .673 | .967 | .635 | .924 | .581 | .950  | .645 | .950  | .615   | .645 | .910 | .615 | .910 | .551 | .932  | .566 | .991  |  |  |
| 23     | .709 | .924 | .684 | .945 | .616 | .966  | .688 | .966  | .643   | .688 | .911 | .643 | .911 | .592 | .953  | .607 | .1000 |  |  |
| 24     | .761 | .953 | .730 | .968 | .668 | .983  | .716 | .983  | .693   | .716 | .934 | .693 | .934 | .635 | .969  | .650 | .1000 |  |  |
| 25     | .795 | .980 | .777 | .987 | .703 | .994  | .768 | .994  | .741   | .768 | .960 | .741 | .960 | .677 | .984  | .692 | .1000 |  |  |
| 26     | .854 | .996 | .825 | .995 | .775 | 1.000 | .860 | .996  | .830   | .860 | .996 | .830 | .996 | .782 | 1.000 | .797 | .1000 |  |  |
| 27     | .907 | 1    | .890 | 1    | .834 | 1     | .910 | 1     | .894   | 1    | .838 | 1    | .838 | 1    | .788  | 1    | .803  |  |  |
| n = 29 |      |      |      |      |      |       |      |       | n = 30 |      |      |      |      |      |       |      |       |  |  |
| 0      | 0    | .067 | 0    | .103 | 0    | .160  | 0    | .211  | 0      | 0    | .054 | 0    | .106 | 0    | .152  | 0    | .200  |  |  |
| 1      | .004 | .135 | .002 | .165 | .000 | .211  | .004 | .263  | .002   | .004 | .130 | .002 | .163 | .000 | .206  | .004 | .258  |  |  |
| 2      | .018 | .190 | .012 | .211 | .005 | .263  | .018 | .316  | .012   | .018 | .183 | .012 | .205 | .005 | .256  | .016 | .308  |  |  |
| 3      | .039 | .235 | .029 | .251 | .015 | .316  | .037 | .369  | .028   | .037 | .219 | .028 | .244 | .015 | .308  | .026 | .360  |  |  |
| 4      | .062 | .279 | .049 | .299 | .030 | .354  | .059 | .407  | .047   | .059 | .266 | .047 | .292 | .028 | .345  | .038 | .397  |  |  |
| 5      | .086 | .303 | .070 | .340 | .046 | .397  | .083 | .444  | .068   | .083 | .295 | .068 | .325 | .045 | .376  | .055 | .428  |  |  |
| 6      | .087 | .345 | .094 | .374 | .065 | .438  | .084 | .481  | .091   | .084 | .326 | .091 | .364 | .063 | .415  | .073 | .467  |  |  |
| 7      | .184 | .385 | .103 | .412 | .086 | .477  | .129 | .523  | .100   | .129 | .376 | .100 | .402 | .083 | .453  | .093 | .505  |  |  |
| 8      | .135 | .425 | .136 | .451 | .108 | .523  | .130 | .567  | .131   | .130 | .416 | .131 | .440 | .104 | .505  | .114 | .557  |  |  |
| 9      | .189 | .453 | .166 | .500 | .132 | .562  | .182 | .609  | .163   | .182 | .458 | .163 | .476 | .127 | .538  | .137 | .590  |  |  |
| 10     | .190 | .500 | .184 | .549 | .157 | .602  | .183 | .646  | .175   | .183 | .492 | .175 | .524 | .151 | .570  | .161 | .622  |  |  |
| 11     | .225 | .527 | .211 | .567 | .185 | .646  | .219 | .690  | .190   | .219 | .524 | .190 | .560 | .162 | .612  | .172 | .664  |  |  |
| 12     | .276 | .575 | .247 | .626 | .206 | .684  | .265 | .736  | .236   | .265 | .554 | .236 | .597 | .198 | .655  | .208 | .707  |  |  |
| 13     | .294 | .515 | .251 | .660 | .211 | .684  | .266 | .736  | .244   | .266 | .554 | .244 | .597 | .198 | .655  | .208 | .707  |  |  |
| 14     | .303 | .655 | .299 | .661 | .260 | .737  | .295 | .781  | .282   | .295 | .624 | .282 | .675 | .249 | .693  | .259 | .745  |  |  |
| 15     | .345 | .697 | .339 | .761 | .263 | .740  | .336 | .784  | .324   | .336 | .564 | .324 | .676 | .256 | .744  | .266 | .796  |  |  |
| 16     | .355 | .706 | .340 | .749 | .316 | .789  | .375 | .833  | .325   | .375 | .705 | .325 | .768 | .308 | .781  | .318 | .830  |  |  |
| 17     | .425 | .724 | .374 | .753 | .345 | .794  | .416 | .834  | .364   | .416 | .724 | .364 | .756 | .329 | .794  | .339 | .839  |  |  |
| 18     | .463 | .775 | .418 | .789 | .354 | .835  | .446 | .879  | .403   | .446 | .735 | .403 | .784 | .345 | .802  | .355 | .851  |  |  |
| 19     | .500 | .810 | .451 | .816 | .397 | .843  | .476 | .887  | .440   | .476 | .781 | .440 | .825 | .388 | .848  | .398 | .897  |  |  |
| 20     | .537 | .811 | .500 | .824 | .438 | .866  | .508 | .910  | .476   | .508 | .817 | .476 | .865 | .430 | .888  | .440 | .900  |  |  |
| 21     | .575 | .865 | .549 | .864 | .477 | .892  | .545 | .934  | .515   | .545 | .815 | .515 | .867 | .462 | .890  | .472 | .942  |  |  |
| 22     | .615 | .866 | .587 | .897 | .523 | .914  | .584 | .958  | .560   | .584 | .870 | .560 | .903 | .495 | .926  | .505 | .978  |  |  |
| 23     | .655 | .912 | .625 | .906 | .562 | .935  | .624 | .979  | .597   | .624 | .917 | .597 | .960 | .531 | .983  | .541 | .1000 |  |  |
| 24     | .697 | .914 | .660 | .920 | .608 | .954  | .664 | .998  | .636   | .664 | .915 | .636 | .969 | .570 | .992  | .580 | .1000 |  |  |
| 25     | .721 | .938 | .701 | .951 | .646 | .970  | .705 | .1000 | .675   | .705 | .917 | .675 | .982 | .612 | .995  | .622 | .1000 |  |  |
| 26     | .775 | .961 | .749 | .971 | .684 | .983  | .734 | .1000 | .708   | .734 | .941 | .708 | .993 | .655 | .997  | .665 | .1000 |  |  |
| 27     | .810 | .982 | .789 | .988 | .737 | .995  | .781 | .1000 | .756   | .781 | .963 | .756 | .993 | .690 | .999  | .700 | .1000 |  |  |
| 28     | .855 | .996 | .834 | .998 | .789 | 1.000 | .817 | .1000 | .795   | .817 | .982 | .795 | .996 | .744 | .999  | .754 | .1000 |  |  |
| 29     | .913 | 1    | .897 | 1    | .840 | 1     | .870 | .1000 | .837   | .870 | .996 | .837 | .996 | .794 | 1.000 | .804 | .1000 |  |  |
|        |      |      |      |      |      |       |      |       |        |      |      |      |      |      |       |      |       |  |  |



## TABLES

TABLE A-23. CONFIDENCE LIMITS FOR A PROPORTION (ONE-SIDED)

For confidence limits for  $n > 30$ , see Table A-24.

If the observed proportion is  $r/n$ , enter the table with  $n$  and  $r$  for an upper one-sided limit.  
 For a lower one-sided limit, enter the table with  $n$  and  $n - r$  and subtract the table entry from 1.

| $r$      | 90%    | 95%    | 99%    | $r$      | 90%    | 95%    | 99%    | $r$      | 90%    | 95%    | 99%  |
|----------|--------|--------|--------|----------|--------|--------|--------|----------|--------|--------|------|
| $n = 2$  |        |        |        | $n = 3$  |        |        |        | $n = 4$  |        |        |      |
| 0        | .684   | .776   | .900   | 0        | .536   | .632   | .785 - | 0        | .438   | .527   | .684 |
| 1        | .949   | .975 - | .995 - | 1        | .804   | .865 - | .941   | 1        | .680   | .751   | .859 |
|          |        |        |        | 2        | .965 + | .988   | .997   | 2        | .857   | .902   | .958 |
|          |        |        |        |          |        |        |        | 3        | .974   | .987   | .997 |
| $n = 5$  |        |        |        | $n = 6$  |        |        |        | $n = 7$  |        |        |      |
| 0        | .369   | .451   | .602   | 0        | .319   | .393   | .536   | 0        | .280   | .348   | .482 |
| 1        | .684   | .657   | .778   | 1        | .510   | .582   | .706   | 1        | .453   | .521   | .643 |
| 2        | .753   | .811   | .894   | 2        | .667   | .729   | .827   | 2        | .596   | .659   | .764 |
| 3        | .888   | .924   | .967   | 3        | .799   | .847   | .915 + | 3        | .721   | .775 - | .858 |
| 4        | .979   | .990   | .998   | 4        | .907   | .937   | .973   | 4        | .830   | .871   | .929 |
|          |        |        |        | 5        | .983   | .991   | .998   | 5        | .921   | .947   | .977 |
|          |        |        |        |          |        |        |        | 6        | .985 + | .993   | .999 |
| $n = 8$  |        |        |        | $n = 9$  |        |        |        | $n = 10$ |        |        |      |
| 0        | .250   | .312   | .438   | 0        | .226   | .283   | .401   | 0        | .206   | .259   | .369 |
| 1        | .406   | .471   | .590   | 1        | .368   | .429   | .544   | 1        | .337   | .394   | .504 |
| 2        | .538   | .600   | .707   | 2        | .490   | .550   | .656   | 2        | .450   | .507   | .612 |
| 3        | .655 + | .711   | .802   | 3        | .599   | .655 + | .750   | 3        | .552   | .607   | .703 |
| 4        | .760   | .807   | .879   | 4        | .699   | .749   | .829   | 4        | .646   | .696   | .782 |
| 5        | .853   | .889   | .939   | 5        | .790   | .831   | .895 - | 5        | .733   | .778   | .850 |
| 6        | .931   | .954   | .980   | 6        | .871   | .902   | .947   | 6        | .812   | .850   | .907 |
| 7        | .987   | .994   | .999   | 7        | .939   | .959   | .983   | 7        | .884   | .913   | .952 |
|          |        |        |        | 8        | .988   | .994   | .999   | 8        | .945 + | .963   | .984 |
|          |        |        |        |          |        |        |        | 9        | .990   | .995 - | .999 |
| $n = 11$ |        |        |        | $n = 12$ |        |        |        | $n = 13$ |        |        |      |
| 0        | .189   | .238   | .342   | 0        | .175 - | .221   | .319   | 0        | .162   | .206   | .298 |
| 1        | .310   | .364   | .470   | 1        | .287   | .339   | .440   | 1        | .268   | .316   | .413 |
| 2        | .415 + | .470   | .572   | 2        | .388   | .438   | .537   | 2        | .360   | .410   | .506 |
| 3        | .511   | .564   | .660   | 3        | .475 + | .527   | .622   | 3        | .444   | .495 - | .588 |
| 4        | .599   | .650   | .738   | 4        | .559   | .609   | .698   | 4        | .523   | .573   | .661 |
| 5        | .682   | .729   | .806   | 5        | .638   | .685 - | .765 + | 5        | .598   | .645 + | .727 |
| 6        | .759   | .800   | .866   | 6        | .712   | .755 - | .825 + | 6        | .669   | .713   | .787 |
| 7        | .831   | .865 - | .916   | 7        | .781   | .819   | .879   | 7        | .736   | .776   | .841 |
| 8        | .895 + | .921   | .957   | 8        | .846   | .877   | .924   | 8        | .799   | .834   | .889 |
| 9        | .951   | .967   | .986   | 9        | .904   | .928   | .961   | 9        | .858   | .887   | .931 |
| 10       | .990   | .995 + | .999   | 10       | .955 - | .970   | .987   | 10       | .912   | .934   | .964 |
|          |        |        |        | 11       | .991   | .996   | .999   | 11       | .958   | .972   | .988 |
|          |        |        |        |          |        |        |        | 12       | .992   | .996   | .999 |
| $n = 14$ |        |        |        | $n = 15$ |        |        |        | $n = 16$ |        |        |      |
| 0        | .152   | .193   | .280   | 0        | .142   | .181   | .264   | 0        | .134   | .171   | .250 |
| 1        | .261   | .297   | .389   | 1        | .236   | .279   | .368   | 1        | .222   | .264   | .349 |
| 2        | .337   | .385 + | .478   | 2        | .317   | .363   | .453   | 2        | .300   | .344   | .430 |
| 3        | .417   | .466   | .557   | 3        | .393   | .440   | .529   | 3        | .371   | .417   | .503 |
| 4        | .492   | .540   | .627   | 4        | .464   | .511   | .597   | 4        | .439   | .484   | .569 |
| 5        | .563   | .610   | .692   | 5        | .532   | .577   | .660   | 5        | .504   | .548   | .630 |

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## TABLES

TABLE A-23 (Continued). CONFIDENCE LIMITS FOR A PROPORTION (ONE-SIDED)

| r                  | 90%   | 95%   | 99%   | r                  | 90%   | 95%   | 99%   | r                  | 90%   | 95%   | 99%   |
|--------------------|-------|-------|-------|--------------------|-------|-------|-------|--------------------|-------|-------|-------|
| n = 14 (Continued) |       |       |       | n = 15 (Continued) |       |       |       | n = 16 (Continued) |       |       |       |
| 6                  | .631  | .675- | .751  | 6                  | .596  | .640  | .718  | 6                  | .565+ | .609  | .687  |
| 7                  | .695+ | .736  | .805+ | 7                  | .658  | .700  | .771  | 7                  | .625- | .667  | .739  |
| 8                  | .757  | .794  | .854  | 8                  | .718  | .756  | .821  | 8                  | .682  | .721  | .788  |
| 9                  | .815- | .847  | .898  | 9                  | .774  | .809  | .865+ | 9                  | .737  | .773  | .834  |
| 10                 | .869  | .896  | .936  | 10                 | .828  | .858  | .906  | 10                 | .790  | .822  | .875- |
| 11                 | .919  | .939  | .967  | 11                 | .878  | .903  | .941  | 11                 | .839  | .868  | .912  |
| 12                 | .961  | .974  | .989  | 12                 | .924  | .943  | .969  | 12                 | .886  | .910  | .946- |
| 13                 | .998  | .996  | .999  | 13                 | .964  | .976  | .990  | 13                 | .929  | .947  | .971  |
|                    |       |       |       | 14                 | .998  | .997  | .999  | 14                 | .966  | .977  | .990  |
|                    |       |       |       |                    |       |       |       | 15                 | .993  | .997  | .999  |
| n = 17             |       |       |       | n = 18             |       |       |       | n = 19             |       |       |       |
| 0                  | .127  | .162  | .237  | 0                  | .120  | .153  | .226  | 0                  | .114  | .146  | .215+ |
| 1                  | .210  | .250  | .332  | 1                  | .199  | .238  | .316  | 1                  | .190  | .226  | .302  |
| 2                  | .284  | .326  | .410  | 2                  | .269  | .310  | .391  | 2                  | .257  | .296  | .374  |
| 3                  | .352  | .396  | .480  | 3                  | .334  | .377  | .458  | 3                  | .319  | .359  | .439  |
| 4                  | .416  | .461  | .543  | 4                  | .396  | .439  | .520  | 4                  | .378  | .419  | .498  |
| 5                  | .478  | .522  | .603  | 5                  | .455+ | .498  | .577  | 5                  | .434  | .476  | .554  |
| 6                  | .537  | .580  | .658  | 6                  | .512  | .554  | .631  | 6                  | .489  | .530  | .606  |
| 7                  | .594  | .636  | .709  | 7                  | .567  | .608  | .681  | 7                  | .541  | .582  | .655+ |
| 8                  | .650  | .689  | .758  | 8                  | .620  | .659  | .729  | 8                  | .592  | .632  | .702  |
| 9                  | .708  | .740  | .803  | 9                  | .671  | .709  | .774  | 9                  | .642  | .680  | .746  |
| 10                 | .754  | .788  | .845- | 10                 | .721  | .756  | .816  | 10                 | .690  | .726  | .788  |
| 11                 | .803  | .834  | .883  | 11                 | .769  | .801  | .855- | 11                 | .737  | .770  | .827  |
| 12                 | .849  | .876  | .918  | 12                 | .815- | .844  | .890  | 12                 | .782  | .812  | .863  |
| 13                 | .893  | .915+ | .948  | 13                 | .858  | .884  | .923  | 13                 | .825- | .853  | .897  |
| 14                 | .933  | .950  | .973  | 14                 | .899  | .920  | .951  | 14                 | .866  | .890  | .927  |
| 15                 | .968  | .979  | .991  | 15                 | .937  | .953  | .975- | 15                 | .905- | .925- | .954  |
| 16                 | .994  | .997  | .999  | 16                 | .970  | .980  | .992  | 16                 | .941  | .956  | .976  |
|                    |       |       |       | 17                 | .994  | .997  | .999  | 17                 | .972  | .981  | .992  |
|                    |       |       |       |                    |       |       |       | 18                 | .994  | .997  | .999  |
| n = 20             |       |       |       | n = 21             |       |       |       | n = 22             |       |       |       |
| 0                  | .109  | .139  | .206  | 0                  | .104  | .133  | .197  | 0                  | .099  | .127  | .189  |
| 1                  | .181  | .216  | .289  | 1                  | .173  | .207  | .277  | 1                  | .166  | .198  | .266  |
| 2                  | .245- | .283  | .358  | 2                  | .234  | .271  | .344  | 2                  | .224  | .259  | .330  |
| 3                  | .304  | .344  | .421  | 3                  | .291  | .329  | .404  | 3                  | .279  | .316  | .389  |
| 4                  | .361  | .401  | .478  | 4                  | .345+ | .384  | .460  | 4                  | .331  | .369  | .443  |
| 5                  | .415- | .456  | .532  | 5                  | .397  | .437  | .512  | 5                  | .381  | .420  | .493  |
| 6                  | .467  | .508  | .583  | 6                  | .448  | .487  | .561  | 6                  | .430  | .468  | .541  |
| 7                  | .518  | .558  | .631  | 7                  | .497  | .536  | .608  | 7                  | .477  | .515+ | .587  |
| 8                  | .567  | .606  | .677  | 8                  | .544  | .583  | .653  | 8                  | .523  | .561  | .630  |
| 9                  | .615+ | .653  | .720  | 9                  | .590  | .628  | .695+ | 9                  | .568  | .605- | .672  |
| 10                 | .662  | .698  | .761  | 10                 | .636  | .672  | .736  | 10                 | .611  | .647  | .712  |
| 11                 | .707  | .741  | .800  | 11                 | .679  | .714  | .774  | 11                 | .654  | .689  | .750  |
| 12                 | .751  | .783  | .837  | 12                 | .722  | .755+ | .811  | 12                 | .695+ | .729  | .786  |
| 13                 | .793  | .823  | .871  | 13                 | .764  | .794  | .845+ | 13                 | .736  | .767  | .821  |
| 14                 | .834  | .860  | .902  | 14                 | .804  | .832  | .878  | 14                 | .775+ | .804  | .853  |
| 15                 | .873  | .896  | .931  | 15                 | .842  | .868  | .908  | 15                 | .813  | .840  | .884  |
| 16                 | .910  | .929  | .956  | 16                 | .879  | .901  | .935- | 16                 | .850  | .874  | .912  |
| 17                 | .944  | .958  | .977  | 17                 | .914  | .932  | .959  | 17                 | .885+ | .906  | .933  |
| 18                 | .973  | .982  | .992  | 18                 | .946  | .960  | .978  | 18                 | .918  | .935+ | .961  |
| 19                 | .995- | .997  | .999  | 19                 | .974  | .983  | .993  | 19                 | .949  | .962  | .979  |
|                    |       |       |       | 20                 | .995- | .988  | 1.000 | 20                 | .976  | .984  | .993  |
|                    |       |       |       |                    |       |       |       | 21                 | .995+ | .998  | 1.000 |

## TABLES

TABLE A-23 (Continued). CONFIDENCE LIMITS FOR A PROPORTION (ONE-SIDED)

| r      | 90%   | 95%   | 99%   | r      | 90%   | 95%   | 99%   | r      | 90%   | 95%   | 99%   |
|--------|-------|-------|-------|--------|-------|-------|-------|--------|-------|-------|-------|
| n = 23 |       |       |       | n = 24 |       |       |       | n = 25 |       |       |       |
| 0      | .095+ | .122  | .181  | 0      | .091  | .117  | .175- | 0      | .088  | .113  | .168  |
| 1      | .159  | .190  | .256  | 1      | .153  | .183  | .246  | 1      | .147  | .176  | .237  |
| 2      | .215+ | .249  | .318  | 2      | .207  | .240  | .307  | 2      | .199  | .231  | .296  |
| 3      | .268  | .304  | .374  | 3      | .258  | .292  | .361  | 3      | .248  | .282  | .349  |
| 4      | .318  | .355- | .427  | 4      | .306  | .342  | .412  | 4      | .295- | .330  | .398  |
| 5      | .366  | .404  | .476  | 5      | .352  | .389  | .460  | 5      | .340  | .375+ | .444  |
| 6      | .413  | .451  | .522  | 6      | .398  | .435- | .505- | 6      | .383  | .420  | .488  |
| 7      | .459  | .496  | .567  | 7      | .442  | .479  | .548  | 7      | .426  | .462  | .531  |
| 8      | .503  | .540  | .609  | 8      | .484  | .521  | .590  | 8      | .467  | .504  | .571  |
| 9      | .546  | .583  | .650  | 9      | .526  | .563  | .630  | 9      | .508  | .544  | .610  |
| 10     | .589  | .625- | .689  | 10     | .567  | .603  | .668  | 10     | .548  | .583  | .648  |
| 11     | .630  | .665- | .727  | 11     | .608  | .642  | .705- | 11     | .587  | .621  | .684  |
| 12     | .670  | .704  | .763  | 12     | .647  | .681  | .740  | 12     | .625- | .659  | .719  |
| 13     | .710  | .742  | .797  | 13     | .685+ | .718  | .774  | 13     | .662  | .695- | .752  |
| 14     | .748  | .778  | .829  | 14     | .723  | .754  | .806  | 14     | .699  | .730  | .784  |
| 15     | .786  | .814  | .860  | 15     | .759  | .788  | .837  | 15     | .735- | .764  | .815+ |
| 16     | .822  | .848  | .889  | 16     | .795+ | .822  | .867  | 16     | .770  | .798  | .845+ |
| 17     | .857  | .880  | .916  | 17     | .830  | .854  | .894  | 17     | .804  | .830  | .873  |
| 18     | .890  | .910  | .941  | 18     | .863  | .885+ | .920  | 18     | .837  | .861  | .899  |
| 19     | .922  | .938  | .962  | 19     | .895+ | .914  | .943  | 19     | .869  | .890  | .923  |
| 20     | .951  | .963  | .980  | 20     | .925+ | .941  | .964  | 20     | .899  | .918  | .946  |
| 21     | .977  | .984  | .993  | 21     | .953  | .965+ | .981  | 21     | .928  | .943  | .966  |
| 22     | .995+ | .998  | 1.000 | 22     | .973  | .985- | .994  | 22     | .955+ | .966  | .982  |
|        |       |       |       | 23     | .996  | .998  | 1.000 | 23     | .979  | .986  | .994  |
|        |       |       |       |        |       |       |       | 24     | .996  | .998  | 1.000 |
| n = 26 |       |       |       | n = 27 |       |       |       | n = 28 |       |       |       |
| 0      | .085- | .109  | .162  | 0      | .082  | .105+ | .157  | 0      | .079  | .101  | .152  |
| 1      | .142  | .170  | .229  | 1      | .137  | .164  | .222  | 1      | .132  | .159  | .215- |
| 2      | .192  | .223  | .286  | 2      | .185+ | .215+ | .277  | 2      | .179  | .208  | .268  |
| 3      | .239  | .272  | .337  | 3      | .231  | .263  | .326  | 3      | .223  | .254  | .316  |
| 4      | .284  | .318  | .385- | 4      | .275- | .308  | .373  | 4      | .265+ | .298  | .361  |
| 5      | .328  | .363  | .430  | 5      | .317  | .351  | .417  | 5      | .306  | .339  | .404  |
| 6      | .370  | .405+ | .473  | 6      | .358  | .392  | .458  | 6      | .346  | .380  | .445- |
| 7      | .411  | .447  | .514  | 7      | .397  | .432  | .498  | 7      | .385- | .419  | .484  |
| 8      | .451  | .487  | .554  | 8      | .436  | .471  | .537  | 8      | .422  | .457  | .521  |
| 9      | .491  | .526  | .592  | 9      | .475- | .509  | .574  | 9      | .459  | .494  | .558  |
| 10     | .529  | .564  | .628  | 10     | .512  | .547  | .610  | 10     | .496  | .530  | .593  |
| 11     | .567  | .602  | .664  | 11     | .549  | .583  | .645+ | 11     | .532  | .565+ | .627  |
| 12     | .604  | .638  | .698  | 12     | .585- | .618  | .679  | 12     | .567  | .600  | .660  |
| 13     | .641  | .673  | .731  | 13     | .620  | .653  | .711  | 13     | .601  | .634  | .692  |
| 14     | .676  | .708  | .763  | 14     | .655+ | .687  | .743  | 14     | .635+ | .667  | .723  |
| 15     | .711  | .742  | .794  | 15     | .689  | .720  | .773  | 15     | .669  | .699  | .753  |
| 16     | .746  | .774  | .823  | 16     | .723  | .752  | .802  | 16     | .701  | .731  | .782  |
| 17     | .779  | .806  | .851  | 17     | .756  | .783  | .831  | 17     | .733  | .762  | .810  |
| 18     | .812  | .837  | .878  | 18     | .788  | .814  | .857  | 18     | .765- | .792  | .837  |
| 19     | .843  | .866  | .903  | 19     | .819  | .843  | .883  | 19     | .796  | .821  | .863  |
| 20     | .874  | .894  | .927  | 20     | .849  | .871  | .907  | 20     | .826  | .849  | .888  |
| 21     | .903  | .921  | .948  | 21     | .879  | .899  | .930  | 21     | .855+ | .876  | .911  |
| 22     | .931  | .946  | .967  | 22     | .907  | .924  | .950  | 22     | .883  | .902  | .932  |
| 23     | .957  | .968  | .983  | 23     | .934  | .948  | .963  | 23     | .911  | .927  | .952  |
| 24     | .979  | .986  | .994  | 24     | .958  | .969  | .983  | 24     | .936  | .950  | .969  |
| 25     | .996  | .998  | 1.000 | 25     | .980  | .987  | .994  | 25     | .960  | .970  | .984  |
|        |       |       |       | 26     | .996  | .998  | 1.000 | 26     | .981  | .987  | .995- |
|        |       |       |       |        |       |       |       | 27     | .996  | .998  | 1.000 |

## TABLES

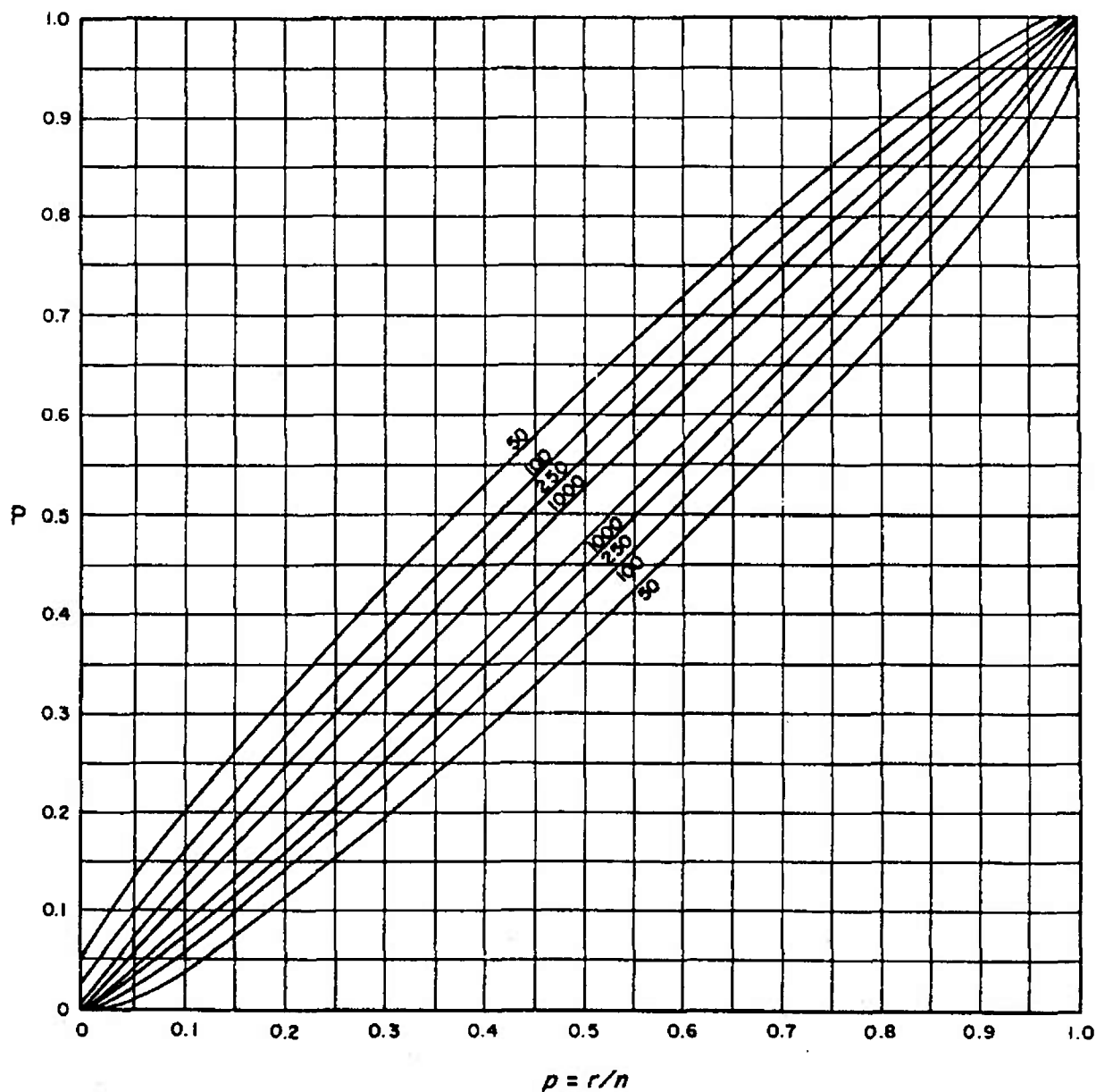
TABLE A-23 (Continued). CONFIDENCE LIMITS FOR A PROPORTION (ONE-SIDED)

| r      | 90%    | 95%    | 99%    | r      | 90%    | 95%    | 99%    |
|--------|--------|--------|--------|--------|--------|--------|--------|
| n = 29 |        |        |        | n = 30 |        |        |        |
| 0      | .076   | .098   | .147   | 0      | .074   | .095 + | .142   |
| 1      | .128   | .153   | .208   | 1      | .124   | .149   | .202   |
| 2      | .173   | .202   | .260   | 2      | .168   | .195 + | .252   |
| 3      | .216   | .246   | .307   | 3      | .209   | .239   | .298   |
| 4      | .257   | .288   | .350   | 4      | .249   | .280   | .340   |
| 5      | .297   | .329   | .392   | 5      | .287   | .319   | .381   |
| 6      | .335 - | .368   | .432   | 6      | .325 - | .357   | .420   |
| 7      | .372   | .406   | .470   | 7      | .361   | .394   | .457   |
| 8      | .409   | .443   | .507   | 8      | .397   | .430   | .493   |
| 9      | .445 + | .479   | .542   | 9      | .432   | .465 + | .527   |
| 10     | .481   | .514   | .577   | 10     | .466   | .499   | .561   |
| 11     | .515 + | .549   | .610   | 11     | .500   | .533   | .594   |
| 12     | .550   | .583   | .643   | 12     | .533   | .566   | .626   |
| 13     | .583   | .616   | .674   | 13     | .566   | .598   | .657   |
| 14     | .616   | .648   | .705 - | 14     | .599   | .630   | .687   |
| 15     | .649   | .680   | .734   | 15     | .630   | .661   | .716   |
| 16     | .681   | .711   | .763   | 16     | .662   | .692   | .744   |
| 17     | .712   | .741   | .791   | 17     | .692   | .721   | .772   |
| 18     | .743   | .771   | .818   | 18     | .723   | .750   | .799   |
| 19     | .774   | .800   | .843   | 19     | .752   | .779   | .824   |
| 20     | .803   | .828   | .868   | 20     | .782   | .807   | .849   |
| 21     | .832   | .855 - | .892   | 21     | .810   | .834   | .873   |
| 22     | .860   | .881   | .914   | 22     | .838   | .860   | .896   |
| 23     | .888   | .906   | .935 - | 23     | .865 + | .885 + | .917   |
| 24     | .914   | .930   | .954   | 24     | .891   | .909   | .937   |
| 25     | .938   | .951   | .970   | 25     | .917   | .932   | .955 + |
| 26     | .961   | .971   | .985 - | 26     | .941   | .953   | .972   |
| 27     | .982   | .988   | .995 - | 27     | .963   | .972   | .985 + |
| 28     | .996   | .998   | 1.000  | 28     | .982   | .988   | .995 - |
|        |        |        |        | 29     | .996   | .998   | 1.000  |

## TABLES

**TABLE A-24. CONFIDENCE BELTS FOR PROPORTIONS FOR  $n > 30$**   
**(CONFIDENCE COEFFICIENT .90)**

For tables of confidence limits for  $n \leq 30$ , see Tables A-22 and A-23

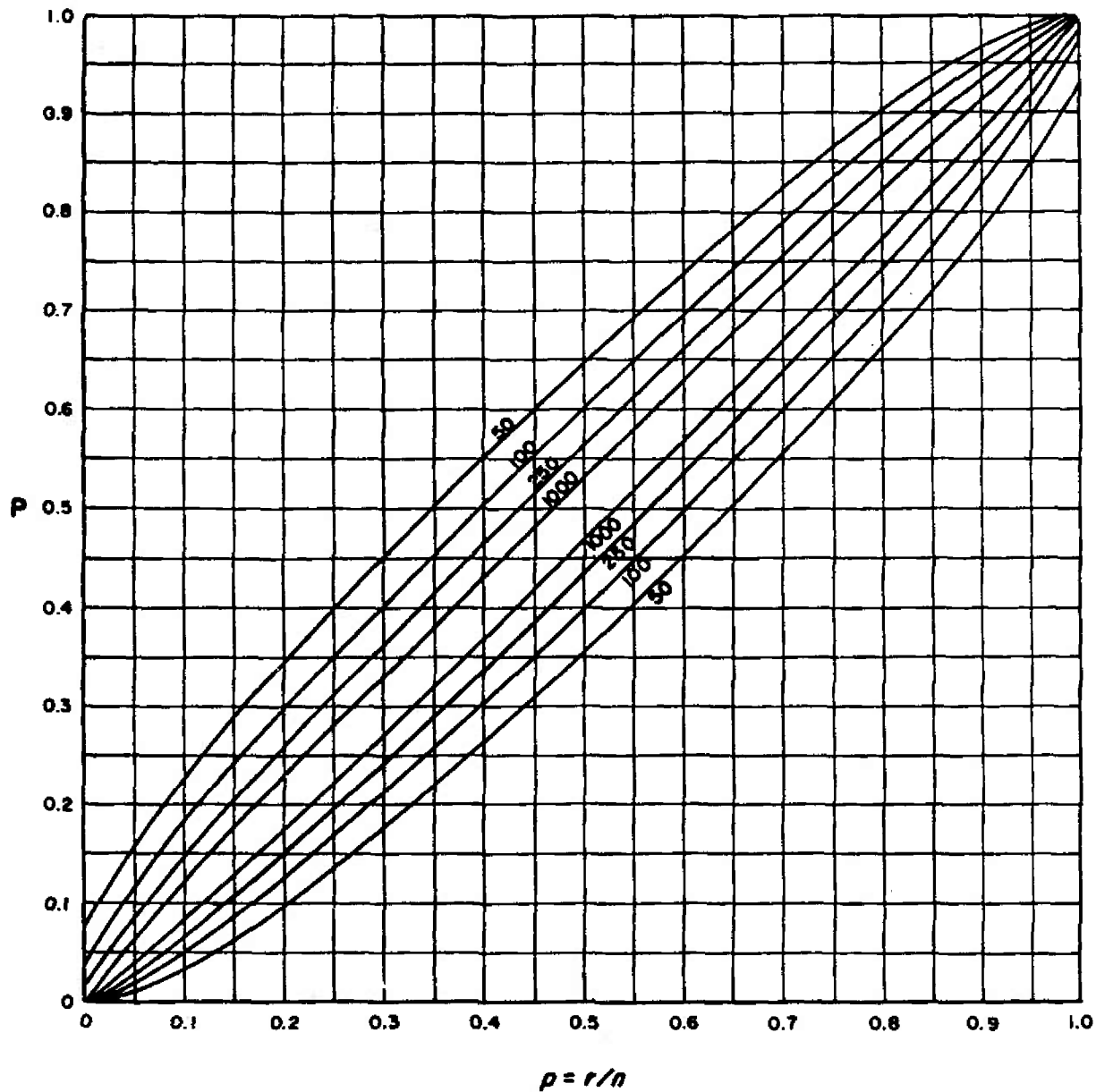


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## TABLES

**TABLE A-24 (Continued). CONFIDENCE BELTS FOR PROPORTIONS FOR  $n > 30$**   
**(CONFIDENCE COEFFICIENT .95)**

For tables of confidence limits for  $n \leq 30$ , see Tables A-22 and A-23

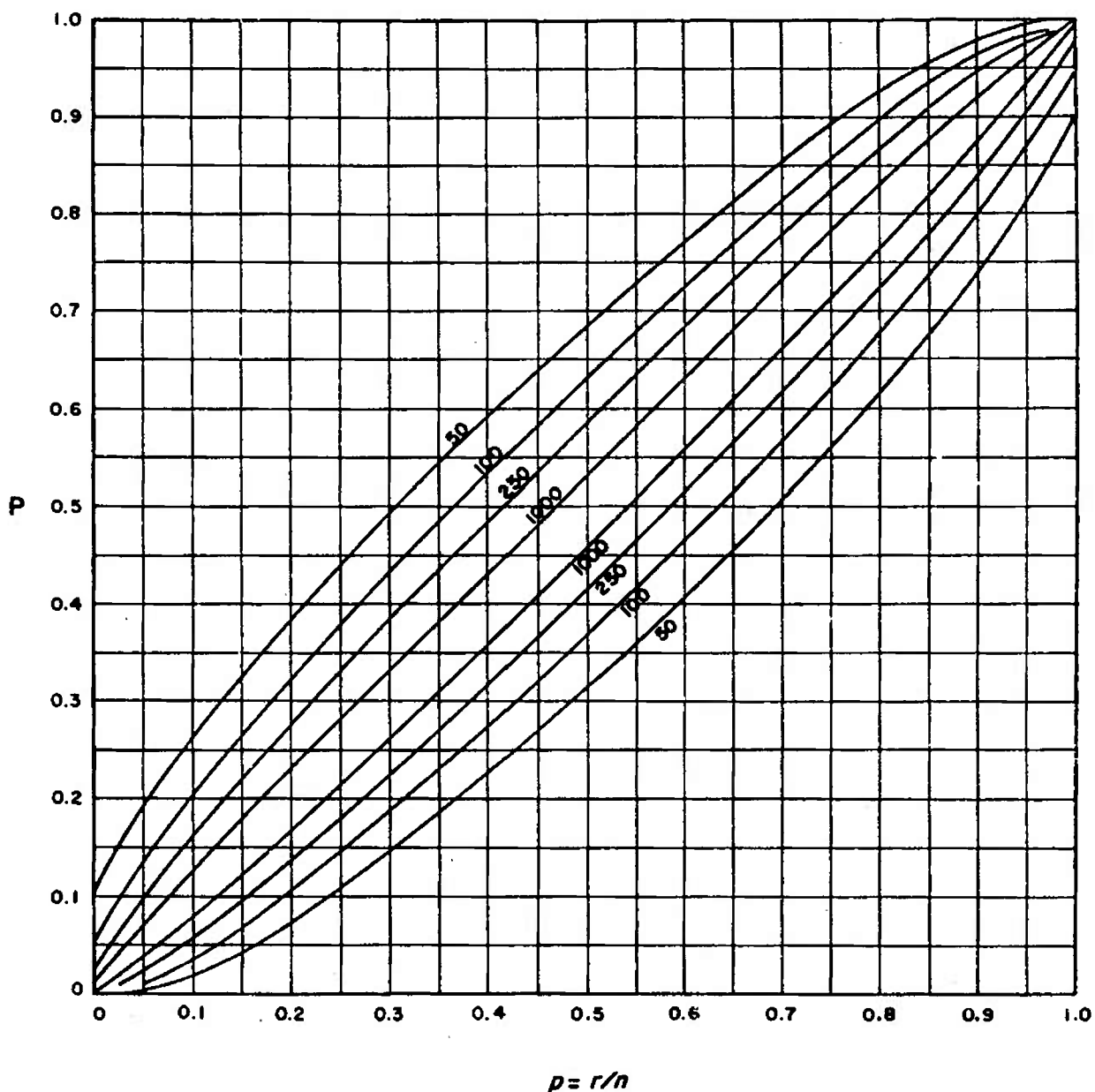


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## TABLES

**TABLE A-24 (Continued). CONFIDENCE BELTS FOR PROPORTIONS FOR  $n > 30$   
(CONFIDENCE COEFFICIENT .99)**

For tables of confidence limits for  $n \leq 30$ , see Tables A-22 and A-23



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## TABLES

**TABLE A-25. SAMPLE SIZE REQUIRED FOR COMPARING A PROPORTION WITH A STANDARD PROPORTION WHEN THE SIGN OF THE DIFFERENCE IS NOT IMPORTANT**

The use of Table A-25 (or equivalent use of Tables A-27 and A-8) is based on the inverse-sine transformation of the binomial to an approximately normal distribution.

Exact determination of required sample size could be made from tables of the binomial distribution, so far as the tables are available. (See *Tables of the Cumulative Binomial Probability Distribution*, Staff, Computation Laboratory, Harvard University, Section IV of the "Introduction" entitled "Applications", Harvard University Press, 1955.)

The entries computed for the tables were rounded to three significant figures, and the rounding was always upward.

These tables also may be used to determine the sample size required for comparing two proportions, as discussed in Chapter 8.

$$\alpha = .05, 1 - \beta = .50$$

| Larger Proportion | Smaller Proportion |      |      |     |     |     |     |     |     |     |     |     |
|-------------------|--------------------|------|------|-----|-----|-----|-----|-----|-----|-----|-----|-----|
|                   | .001               | .002 | .005 | .01 | .02 | .05 | .10 | .20 | .30 | .40 | .45 | .50 |
| .01               | 205                | 313  | 1120 | —   | —   | —   | —   | —   | —   | —   | —   | —   |
| .02               | 80                 | 102  | 190  | 551 | —   | —   | —   | —   | —   | —   | —   | —   |
| .05               | 26                 | 30   | 41   | 62  | 138 | —   | —   | —   | —   | —   | —   | —   |
| .10               | 12                 | 13   | 16   | 20  | 30  | 104 | —   | —   | —   | —   | —   | —   |
| .20               | 6                  | 6    | 7    | 8   | 10  | 17  | 48  | —   | —   | —   | —   | —   |
| .30               | 4                  | 4    | 4    | 5   | 6   | 8   | 15  | 72  | —   | —   | —   | —   |
| .40               | 3                  | 3    | 3    | 3   | 4   | 5   | 8   | 20  | 88  | —   | —   | —   |
| .45               | 2                  | 3    | 3    | 3   | 3   | 4   | 6   | 14  | 40  | 376 | —   | —   |
| .50               | 2                  | 2    | 2    | 3   | 3   | 4   | 5   | 10  | 23  | 95  | 383 | —   |
| .55               | 2                  | 2    | 2    | 2   | 2   | 3   | 4   | 7   | 15  | 43  | 96  | 383 |
| .60               | 2                  | 2    | 2    | 2   | 2   | 3   | 4   | 6   | 11  | 24  | 43  | 95  |
| .70               | 2                  | 2    | 2    | 2   | 2   | 2   | 3   | 4   | 6   | 11  | 15  | 23  |
| .80               | 1                  | 1    | 1    | 1   | 2   | 2   | 2   | 3   | 4   | 6   | 7   | 10  |
| .90               | 1                  | 1    | 1    | 1   | 1   | 1   | 2   | 2   | 3   | 4   | 4   | 5   |
| 1.00              | 1                  | 1    | 1    | 1   | 1   | 1   | 1   | 1   | 1   | 2   | 2   | 2   |



## TABLES

TABLE A-25 (Continued). SAMPLE SIZE REQUIRED FOR COMPARING A PROPORTION WITH A STANDARD PROPORTION WHEN THE SIGN OF THE DIFFERENCE IS NOT IMPORTANT

$$\alpha = .05, 1 - \beta = .80$$

| Larger Proportion | Smaller Proportion |      |      |      |     |     |     |     |     |     |     |     |
|-------------------|--------------------|------|------|------|-----|-----|-----|-----|-----|-----|-----|-----|
|                   | .001               | .002 | .005 | .01  | .02 | .05 | .10 | .20 | .30 | .40 | .45 | .50 |
| .01               | 419                | 640  | 2280 | —    | —   | —   | —   | —   | —   | —   | —   | —   |
| .02               | 162                | 208  | 388  | 1130 | —   | —   | —   | —   | —   | —   | —   | —   |
| .05               | 53                 | 61   | 82   | 125  | 281 | —   | —   | —   | —   | —   | —   | —   |
| .10               | 24                 | 26   | 32   | 40   | 61  | 212 | —   | —   | —   | —   | —   | —   |
| .20               | 11                 | 12   | 13   | 15   | 19  | 35  | 98  | —   | —   | —   | —   | —   |
| .30               | 7                  | 7    | 8    | 9    | 11  | 16  | 30  | 146 | —   | —   | —   | —   |
| .40               | 5                  | 5    | 6    | 6    | 7   | 10  | 15  | 41  | 178 | —   | —   | —   |
| .45               | 4                  | 5    | 5    | 5    | 6   | 8   | 12  | 27  | 82  | 767 | —   | —   |
| .50               | 4                  | 4    | 4    | 5    | 5   | 7   | 10  | 19  | 47  | 194 | 782 | —   |
| .55               | 4                  | 4    | 4    | 4    | 5   | 6   | 8   | 15  | 30  | 87  | 196 | 782 |
| .60               | 3                  | 3    | 3    | 4    | 4   | 5   | 7   | 11  | 21  | 49  | 87  | 194 |
| .70               | 3                  | 3    | 3    | 3    | 3   | 4   | 5   | 8   | 12  | 21  | 30  | 47  |
| .80               | 2                  | 2    | 2    | 2    | 3   | 3   | 4   | 5   | 8   | 11  | 15  | 19  |
| .90               | 2                  | 2    | 2    | 2    | 2   | 2   | 3   | 4   | 5   | 7   | 8   | 10  |
| 1.00              | 1                  | 1    | 1    | 1    | 1   | 2   | 2   | 2   | 2   | 3   | 3   | 4   |

$$\alpha = .05, 1 - \beta = .90$$

| Larger Proportion | Smaller Proportion |      |      |      |     |     |     |     |     |      |      |      |
|-------------------|--------------------|------|------|------|-----|-----|-----|-----|-----|------|------|------|
|                   | .001               | .002 | .005 | .01  | .02 | .05 | .10 | .20 | .30 | .40  | .45  | .50  |
| .01               | 560                | 857  | 3040 | —    | —   | —   | —   | —   | —   | —    | —    | —    |
| .02               | 217                | 279  | 520  | 1510 | —   | —   | —   | —   | —   | —    | —    | —    |
| .05               | 70                 | 81   | 110  | 168  | 376 | —   | —   | —   | —   | —    | —    | —    |
| .10               | 32                 | 35   | 42   | 54   | 82  | 284 | —   | —   | —   | —    | —    | —    |
| .20               | 15                 | 15   | 18   | 20   | 26  | 47  | 131 | —   | —   | —    | —    | —    |
| .30               | 9                  | 10   | 11   | 12   | 14  | 21  | 40  | 196 | —   | —    | —    | —    |
| .40               | 7                  | 7    | 7    | 8    | 9   | 13  | 20  | 54  | 239 | —    | —    | —    |
| .45               | 6                  | 6    | 6    | 7    | 8   | 11  | 16  | 36  | 109 | 1030 | —    | —    |
| .50               | 5                  | 5    | 6    | 6    | 7   | 9   | 13  | 26  | 63  | 260  | 1050 | —    |
| .55               | 5                  | 5    | 5    | 5    | 6   | 8   | 10  | 20  | 41  | 116  | 262  | 1050 |
| .60               | 4                  | 4    | 4    | 5    | 5   | 7   | 9   | 15  | 28  | 65   | 116  | 260  |
| .70               | 3                  | 3    | 4    | 4    | 4   | 5   | 6   | 10  | 16  | 28   | 41   | 63   |
| .80               | 3                  | 3    | 3    | 3    | 3   | 4   | 5   | 7   | 10  | 15   | 20   | 26   |
| .90               | 2                  | 2    | 2    | 2    | 3   | 3   | 4   | 5   | 6   | 9    | 10   | 13   |
| 1.00              | 2                  | 2    | 2    | 2    | 2   | 2   | 2   | 3   | 3   | 4    | 4    | 5    |

## TABLES

TABLE A-25 (Continued). SAMPLE SIZE REQUIRED FOR COMPARING A PROPORTION WITH A STANDARD PROPORTION WHEN THE SIGN OF THE DIFFERENCE IS NOT IMPORTANT

$$\alpha = .05, 1 - \beta = .95$$

| Larger Proportion | Smaller Proportion |      |      |      |     |     |     |     |     |      |      |      |
|-------------------|--------------------|------|------|------|-----|-----|-----|-----|-----|------|------|------|
|                   | .001               | .002 | .005 | .01  | .02 | .05 | .10 | .20 | .30 | .40  | .45  | .50  |
| .01               | 693                | 1060 | 3760 | —    | —   | —   | —   | —   | —   | —    | —    | —    |
| .02               | 268                | 345  | 642  | 1870 | —   | —   | —   | —   | —   | —    | —    | —    |
| .05               | 87                 | 100  | 136  | 207  | 465 | —   | —   | —   | —   | —    | —    | —    |
| .10               | 39                 | 43   | 52   | 67   | 101 | 351 | —   | —   | —   | —    | —    | —    |
| .20               | 18                 | 19   | 22   | 25   | 32  | 58  | 162 | —   | —   | —    | —    | —    |
| .30               | 11                 | 12   | 13   | 15   | 17  | 26  | 49  | 242 | —   | —    | —    | —    |
| .40               | 8                  | 8    | 9    | 10   | 12  | 16  | 25  | 67  | 295 | —    | —    | —    |
| .45               | 7                  | 7    | 8    | 9    | 10  | 13  | 19  | 45  | 135 | 1270 | —    | —    |
| .50               | 6                  | 6    | 7    | 7    | 8   | 11  | 16  | 32  | 77  | 321  | 1300 | —    |
| .55               | 6                  | 6    | 6    | 7    | 7   | 9   | 13  | 24  | 50  | 143  | 324  | 1300 |
| .60               | 5                  | 5    | 5    | 6    | 6   | 8   | 11  | 19  | 35  | 81   | 143  | 321  |
| .70               | 4                  | 4    | 4    | 5    | 5   | 6   | 8   | 12  | 20  | 35   | 50   | 77   |
| .80               | 3                  | 3    | 4    | 4    | 4   | 5   | 6   | 8   | 12  | 19   | 24   | 32   |
| .90               | 3                  | 3    | 3    | 3    | 3   | 4   | 4   | 6   | 8   | 11   | 13   | 16   |
| 1.00              | 2                  | 2    | 2    | 2    | 2   | 2   | 3   | 3   | 4   | 5    | 5    | 6    |

$$\alpha = .05, 1 - \beta = .99$$

| Larger Proportion | Smaller Proportion |      |      |      |     |     |     |     |     |      |      |      |
|-------------------|--------------------|------|------|------|-----|-----|-----|-----|-----|------|------|------|
|                   | .001               | .002 | .005 | .01  | .02 | .05 | .10 | .20 | .30 | .40  | .45  | .50  |
| .01               | 979                | 1500 | 5320 | —    | —   | —   | —   | —   | —   | —    | —    | —    |
| .02               | 378                | 487  | 908  | 2640 | —   | —   | —   | —   | —   | —    | —    | —    |
| .05               | 128                | 141  | 192  | 293  | 658 | —   | —   | —   | —   | —    | —    | —    |
| .10               | 55                 | 60   | 73   | 94   | 142 | 496 | —   | —   | —   | —    | —    | —    |
| .20               | 25                 | 27   | 30   | 35   | 45  | 81  | 229 | —   | —   | —    | —    | —    |
| .30               | 16                 | 17   | 18   | 20   | 24  | 37  | 70  | 342 | —   | —    | —    | —    |
| .40               | 11                 | 12   | 13   | 14   | 16  | 22  | 35  | 94  | 417 | —    | —    | —    |
| .45               | 10                 | 10   | 11   | 12   | 14  | 18  | 27  | 63  | 190 | 1800 | —    | —    |
| .50               | 9                  | 9    | 9    | 10   | 12  | 15  | 22  | 45  | 109 | 453  | 1830 | —    |
| .55               | 8                  | 8    | 8    | 9    | 10  | 13  | 18  | 34  | 71  | 202  | 458  | 1830 |
| .60               | 7                  | 7    | 7    | 8    | 9   | 11  | 15  | 26  | 49  | 114  | 202  | 453  |
| .70               | 5                  | 6    | 6    | 6    | 7   | 8   | 11  | 17  | 28  | 49   | 71   | 109  |
| .80               | 4                  | 5    | 5    | 5    | 5   | 6   | 8   | 12  | 17  | 26   | 34   | 45   |
| .90               | 4                  | 4    | 4    | 4    | 4   | 5   | 6   | 8   | 11  | 15   | 18   | 22   |
| 1.00              | 2                  | 2    | 3    | 3    | 3   | 3   | 3   | 4   | 5   | 6    | 7    | 8    |

## TABLES

**TABLE A-26. SAMPLE SIZE REQUIRED FOR COMPARING A PROPORTION WITH A STANDARD PROPORTION WHEN THE SIGN OF THE DIFFERENCE IS IMPORTANT**

The use of Table A-26 (or the equivalent use of Tables A-27 and A-9) is based on the inverse-sine transformation of the binomial to an approximately normal distribution.

Exact determination of required sample size could be made from tables of the binomial distribution, so far as the tables are available. (See *Tables of the Cumulative Binomial Distribution*, Staff, Computation Laboratory, Harvard University, Section IV of the "Introduction" entitled "Applications", Harvard University Press, 1955.)

The entries computed for the tables were rounded to three significant figures, and the rounding was always upward.

These tables may also be used to determine the sample size required for comparing two proportions, as discussed in Chapter 8.

$$\alpha = .05, \quad 1 - \beta = .50$$

| Larger Proportion | Smaller Proportion |      |      |     |     |     |     |     |     |     |     |     |
|-------------------|--------------------|------|------|-----|-----|-----|-----|-----|-----|-----|-----|-----|
|                   | .001               | .002 | .005 | .01 | .02 | .05 | .10 | .20 | .30 | .40 | .45 | .50 |
| .01               | 145                | 221  | 783  | —   | —   | —   | —   | —   | —   | —   | —   | —   |
| .02               | 56                 | 72   | 134  | 389 | —   | —   | —   | —   | —   | —   | —   | —   |
| .05               | 19                 | 21   | 29   | 44  | 97  | —   | —   | —   | —   | —   | —   | —   |
| .10               | 9                  | 9    | 11   | 14  | 21  | 74  | —   | —   | —   | —   | —   | —   |
| .20               | 4                  | 4    | 5    | 6   | 7   | 12  | 34  | —   | —   | —   | —   | —   |
| .30               | 3                  | 3    | 3    | 3   | 4   | 6   | 11  | 51  | —   | —   | —   | —   |
| .40               | 2                  | 2    | 2    | 2   | 3   | 4   | 6   | 14  | 62  | —   | —   | —   |
| .45               | 2                  | 2    | 2    | 2   | 2   | 3   | 4   | 10  | 28  | 265 | —   | —   |
| .50               | 2                  | 2    | 2    | 2   | 2   | 3   | 4   | 7   | 16  | 67  | 270 | —   |
| .55               | 2                  | 2    | 2    | 2   | 2   | 2   | 3   | 5   | 11  | 30  | 58  | 270 |
| .60               | 1                  | 1    | 2    | 2   | 2   | 2   | 3   | 4   | 8   | 17  | 30  | 67  |
| .70               | 1                  | 1    | 1    | 1   | 1   | 2   | 2   | 3   | 4   | 8   | 11  | 16  |
| .80               | 1                  | 1    | 1    | 1   | 1   | 1   | 2   | 2   | 3   | 4   | 5   | 7   |
| .90               | 1                  | 1    | 1    | 1   | 1   | 1   | 1   | 2   | 2   | 3   | 3   | 4   |
| 1.00              | 1                  | 1    | 1    | 1   | 1   | 1   | 1   | 1   | 1   | 1   | 1   | 2   |

## TABLES

TABLE A-26 (Continued). SAMPLE SIZE REQUIRED FOR COMPARING A PROPORTION WITH A STANDARD PROPORTION WHEN THE SIGN OF THE DIFFERENCE IS IMPORTANT

$\alpha = .05, 1 - \beta = .80$

| Larger Proportion | Smaller Proportion |      |      |     |     |     |     |     |     |     |     |     |
|-------------------|--------------------|------|------|-----|-----|-----|-----|-----|-----|-----|-----|-----|
|                   | .001               | .002 | .005 | .01 | .02 | .05 | .10 | .20 | .30 | .40 | .45 | .50 |
| .01               | 330                | 504  | 1790 | —   | —   | —   | —   | —   | —   | —   | —   | —   |
| .02               | 128                | 164  | 306  | 888 | —   | —   | —   | —   | —   | —   | —   | —   |
| .05               | 42                 | 48   | 65   | 99  | 222 | —   | —   | —   | —   | —   | —   | —   |
| .10               | 19                 | 21   | 25   | 32  | 48  | 167 | —   | —   | —   | —   | —   | —   |
| .20               | 9                  | 9    | 11   | 12  | 15  | 28  | 77  | —   | —   | —   | —   | —   |
| .30               | 6                  | 6    | 6    | 7   | 9   | 13  | 24  | 115 | —   | —   | —   | —   |
| .40               | 4                  | 4    | 5    | 5   | 6   | 8   | 12  | 32  | 141 | —   | —   | —   |
| .45               | 4                  | 4    | 4    | 4   | 5   | 6   | 10  | 21  | 64  | 604 | —   | —   |
| .50               | 3                  | 3    | 4    | 4   | 4   | 5   | 8   | 15  | 37  | 153 | 617 | —   |
| .55               | 3                  | 3    | 3    | 3   | 4   | 5   | 6   | 12  | 24  | 68  | 155 | 617 |
| .60               | 3                  | 3    | 3    | 3   | 3   | 4   | 5   | 9   | 17  | 39  | 68  | 153 |
| .70               | 2                  | 2    | 2    | 2   | 3   | 3   | 4   | 6   | 10  | 17  | 24  | 37  |
| .80               | 2                  | 2    | 2    | 2   | 2   | 2   | 3   | 4   | 6   | 9   | 12  | 15  |
| .90               | 2                  | 2    | 2    | 2   | 2   | 2   | 2   | 3   | 4   | 5   | 6   | 8   |
| 1.00              | 1                  | 1    | 1    | 1   | 1   | 1   | 1   | 2   | 2   | 2   | 3   | 3   |

$\alpha = .05, 1 - \beta = .90$

| Larger Proportion | Smaller Proportion |      |      |      |     |     |     |     |     |     |     |     |
|-------------------|--------------------|------|------|------|-----|-----|-----|-----|-----|-----|-----|-----|
|                   | .001               | .002 | .005 | .01  | .02 | .05 | .10 | .20 | .30 | .40 | .45 | .50 |
| .01               | 457                | 698  | 2480 | —    | —   | —   | —   | —   | —   | —   | —   | —   |
| .02               | 177                | 227  | 424  | 1230 | —   | —   | —   | —   | —   | —   | —   | —   |
| .05               | 57                 | 66   | 90   | 137  | 307 | —   | —   | —   | —   | —   | —   | —   |
| .10               | 26                 | 28   | 34   | 44   | 67  | 232 | —   | —   | —   | —   | —   | —   |
| .20               | 12                 | 13   | 14   | 17   | 21  | 38  | 107 | —   | —   | —   | —   | —   |
| .30               | 8                  | 8    | 9    | 10   | 12  | 18  | 33  | 160 | —   | —   | —   | —   |
| .40               | 6                  | 6    | 6    | 7    | 8   | 11  | 17  | 44  | 195 | —   | —   | —   |
| .45               | 5                  | 5    | 5    | 6    | 7   | 9   | 13  | 30  | 89  | 837 | —   | —   |
| .50               | 4                  | 4    | 5    | 5    | 6   | 7   | 10  | 21  | 51  | 212 | 854 | —   |
| .55               | 4                  | 4    | 4    | 4    | 5   | 6   | 9   | 16  | 33  | 95  | 214 | 854 |
| .60               | 3                  | 4    | 4    | 4    | 4   | 5   | 7   | 13  | 23  | 53  | 95  | 212 |
| .70               | 3                  | 3    | 3    | 3    | 3   | 4   | 5   | 8   | 13  | 23  | 33  | 51  |
| .80               | 2                  | 2    | 2    | 3    | 3   | 3   | 4   | 6   | 8   | 13  | 16  | 21  |
| .90               | 2                  | 2    | 2    | 2    | 2   | 3   | 3   | 4   | 5   | 7   | 9   | 10  |
| 1.00              | 1                  | 1    | 1    | 1    | 2   | 2   | 2   | 2   | 3   | 3   | 4   | 4   |

## TABLES

TABLE A-26 (Continued). SAMPLE SIZE REQUIRED FOR COMPARING A PROPORTION WITH A STANDARD PROPORTION WHEN THE SIGN OF THE DIFFERENCE IS IMPORTANT

$$\alpha = .05, 1 - \beta = .95$$

| Larger Proportion | Smaller Proportion |      |      |      |     |     |     |     |     |      |      |      |
|-------------------|--------------------|------|------|------|-----|-----|-----|-----|-----|------|------|------|
|                   | .001               | .002 | .005 | .01  | .02 | .05 | .10 | .20 | .30 | .40  | .45  | .50  |
| .01               | 577                | 882  | 3140 | —    | —   | —   | —   | —   | —   | —    | —    | —    |
| .02               | 223                | 287  | 535  | 1560 | —   | —   | —   | —   | —   | —    | —    | —    |
| .05               | 73                 | 83   | 113  | 173  | 388 | —   | —   | —   | —   | —    | —    | —    |
| .10               | 33                 | 36   | 43   | 56   | 84  | 293 | —   | —   | —   | —    | —    | —    |
| .20               | 15                 | 16   | 18   | 21   | 27  | 48  | 135 | —   | —   | —    | —    | —    |
| .30               | 10                 | 10   | 11   | 12   | 15  | 22  | 41  | 202 | —   | —    | —    | —    |
| .40               | 7                  | 7    | 8    | 8    | 10  | 13  | 21  | 56  | 246 | —    | —    | —    |
| .45               | 6                  | 6    | 7    | 7    | 8   | 11  | 16  | 37  | 112 | 1060 | —    | —    |
| .50               | 5                  | 5    | 6    | 6    | 7   | 9   | 13  | 27  | 64  | 267  | 1080 | —    |
| .55               | 5                  | 5    | 5    | 6    | 6   | 8   | 11  | 20  | 42  | 119  | 270  | 1080 |
| .60               | 4                  | 4    | 5    | 5    | 5   | 7   | 9   | 16  | 29  | 67   | 119  | 267  |
| .70               | 3                  | 4    | 4    | 4    | 4   | 5   | 7   | 10  | 16  | 29   | 42   | 64   |
| .80               | 3                  | 3    | 3    | 3    | 3   | 4   | 5   | 7   | 10  | 16   | 20   | 27   |
| .90               | 2                  | 2    | 2    | 3    | 3   | 3   | 4   | 5   | 7   | 9    | 11   | 13   |
| 1.00              | 2                  | 2    | 2    | 2    | 2   | 2   | 2   | 3   | 3   | 4    | 4    | 5    |

$$\alpha = .05, 1 - \beta = .99$$

| Larger Proportion | Smaller Proportion |      |      |      |     |     |     |     |     |      |      |      |
|-------------------|--------------------|------|------|------|-----|-----|-----|-----|-----|------|------|------|
|                   | .001               | .002 | .005 | .01  | .02 | .05 | .10 | .20 | .30 | .40  | .45  | .50  |
| .01               | 841                | 1290 | 4570 | —    | —   | —   | —   | —   | —   | —    | —    | —    |
| .02               | 325                | 418  | 779  | 2270 | —   | —   | —   | —   | —   | —    | —    | —    |
| .05               | 105                | 121  | 165  | 251  | 565 | —   | —   | —   | —   | —    | —    | —    |
| .10               | 47                 | 52   | 68   | 81   | 122 | 426 | —   | —   | —   | —    | —    | —    |
| .20               | 22                 | 23   | 26   | 30   | 39  | 70  | 196 | —   | —   | —    | —    | —    |
| .30               | 14                 | 14   | 16   | 18   | 21  | 32  | 60  | 293 | —   | —    | —    | —    |
| .40               | 10                 | 10   | 11   | 12   | 14  | 19  | 30  | 81  | 358 | —    | —    | —    |
| .45               | 8                  | 9    | 9    | 10   | 12  | 16  | 24  | 54  | 163 | 1540 | —    | —    |
| .50               | 7                  | 8    | 8    | 9    | 10  | 13  | 19  | 39  | 94  | 389  | 1580 | —    |
| .55               | 7                  | 7    | 7    | 8    | 9   | 11  | 15  | 29  | 61  | 174  | 393  | 1580 |
| .60               | 6                  | 6    | 6    | 7    | 8   | 10  | 13  | 23  | 42  | 98   | 174  | 389  |
| .70               | 5                  | 5    | 5    | 5    | 6   | 7   | 9   | 15  | 24  | 42   | 61   | 94   |
| .80               | 4                  | 4    | 4    | 4    | 5   | 6   | 7   | 10  | 15  | 23   | 29   | 39   |
| .90               | 3                  | 3    | 3    | 3    | 4   | 4   | 5   | 7   | 9   | 13   | 15   | 19   |
| 1.00              | 2                  | 2    | 2    | 2    | 2   | 3   | 3   | 4   | 5   | 6    | 6    | 7    |

## TABLES

TABLE A-27. TABLE OF ARC SINE TRANSFORMATION FOR PROPORTIONS

$$\theta = 2 \arcsin \sqrt{P}$$

| P   | $\theta$ | P   | $\theta$ | P   | $\theta$ | P    | $\theta$ |
|-----|----------|-----|----------|-----|----------|------|----------|
| .00 | .00      | .25 | 1.05     | .50 | 1.57     | .75  | 2.09     |
| .01 | .20      | .26 | 1.07     | .51 | 1.59     | .76  | 2.12     |
| .02 | .28      | .27 | 1.09     | .52 | 1.61     | .77  | 2.14     |
| .03 | .35      | .28 | 1.12     | .53 | 1.63     | .78  | 2.17     |
| .04 | .40      | .29 | 1.14     | .54 | 1.65     | .79  | 2.19     |
| .05 | .45      | .30 | 1.16     | .55 | 1.67     | .80  | 2.21     |
| .06 | .49      | .31 | 1.18     | .56 | 1.69     | .81  | 2.24     |
| .07 | .54      | .32 | 1.20     | .57 | 1.71     | .82  | 2.27     |
| .08 | .57      | .33 | 1.22     | .58 | 1.73     | .83  | 2.29     |
| .09 | .61      | .34 | 1.25     | .59 | 1.75     | .84  | 2.32     |
| .10 | .64      | .35 | 1.27     | .60 | 1.77     | .85  | 2.35     |
| .11 | .68      | .36 | 1.29     | .61 | 1.79     | .86  | 2.37     |
| .12 | .71      | .37 | 1.31     | .62 | 1.81     | .87  | 2.40     |
| .13 | .74      | .38 | 1.33     | .63 | 1.83     | .88  | 2.43     |
| .14 | .77      | .39 | 1.35     | .64 | 1.85     | .89  | 2.47     |
| .15 | .80      | .40 | 1.37     | .65 | 1.88     | .90  | 2.50     |
| .16 | .82      | .41 | 1.39     | .66 | 1.90     | .91  | 2.53     |
| .17 | .85      | .42 | 1.41     | .67 | 1.92     | .92  | 2.57     |
| .18 | .88      | .43 | 1.43     | .68 | 1.94     | .93  | 2.61     |
| .19 | .90      | .44 | 1.45     | .69 | 1.96     | .94  | 2.65     |
| .20 | .93      | .45 | 1.47     | .70 | 1.98     | .95  | 2.69     |
| .21 | .95      | .46 | 1.49     | .71 | 2.00     | .96  | 2.74     |
| .22 | .98      | .47 | 1.51     | .72 | 2.03     | .97  | 2.79     |
| .23 | 1.00     | .48 | 1.53     | .73 | 2.05     | .98  | 2.86     |
| .24 | 1.02     | .49 | 1.55     | .74 | 2.07     | .99  | 2.94     |
|     |          |     |          |     |          | 1.00 | 3.14     |

## TABLES

TABLE A-28. MINIMUM CONTRASTS REQUIRED FOR SIGNIFICANCE IN  
 $2 \times 2$  TABLES WITH EQUAL SAMPLES

Note that some entries in this table have been omitted in instances where they are easy to supply. For example, see  $n_A = n_B = 80$ , 5% Level. There is an entry (16,29) followed by an entry (23,36). The difference between the first numbers of these pairs is the same as the difference between the second numbers of the pairs. Thus contrast pairs (17,30), (18,31), (19,32), etc., are also significant contrasts, but have been omitted to save space.

In many cases this table can be used to give a good idea of the significance of an observed contrast for values of  $n$  intermediate to those tabulated. For example, consider two samples of  $n = 320$  items each:

|          | Class I | Class II | Total |
|----------|---------|----------|-------|
| Sample A | 92      | 228      | 320   |
| Sample B | 117     | 203      | 320   |

We find the entry (95,119) in the table for  $n = 300$ , hence (92,116) is a significant contrast for  $n = 300$ . For  $n = 400$ , we find (100,126), hence (92,118) is a significant contrast for  $n = 400$ . We conclude that the observed contrast (92,117) is approximately significant at the 5% level.

If this method is not considered sufficient in a particular case, use the  $\chi^2$  method described in Chapter 8. The  $\chi^2$  method is an approximation which gives good results for cases not covered by this table.

| 5% Level, Two-Sided (Is $P_A$ different from $P_B$ ?)<br>2.5% Level, One-Sided (Is $P_A$ larger than $P_B$ ?) |                          | 1% Level, Two-Sided (Is $P_A$ different from $P_B$ ?)<br>0.5% Level, One-Sided (Is $P_A$ larger than $P_B$ ?) |                    |
|---|--------------------------|---|--------------------|
| Sample Size<br>$n_A = n_B$  | $A_1, A_2$               | Sample Size<br>$n_A = n_B$  | $A_1, A_2$         |
| 4   | 0,4                      |   |                    |
| 5   | 0,4                      | 5   | 0,5                |
| 6   | 0,5                      | 6   | 0,6                |
| 7   | 0,5    1,6               | 7   | 0,6                |
| 8   | 0,5    1,6               | 8   | 0,6                |
| 9   | 0,5    1,6               | 9   | 0,6    1,8         |
| 10  | 0,5    1,7    2,8        | 10  | 0,7    1,8         |
| 11  | 0,5    1,7    2,8        | 11  | 0,7    1,8    2,9  |
| 12  | 0,5    1,7    2,8    3,9 | 12  | 0,7    1,8    2,10 |

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## TABLES

TABLE A-28 (Continued). MINIMUM CONTRASTS REQUIRED FOR SIGNIFICANCE IN  
2 × 2 TABLES WITH EQUAL SAMPLES

| 5% Level, Two-Sided (Is $P_A$ different from $P_B$ ?)<br>2.5% Level, One-Sided (Is $P_A$ larger than $P_B$ ?) |                              |                              |                                |                                | 1% Level, Two-Sided (Is $P_A$ different from $P_B$ ?)<br>0.5% Level, One-Sided (Is $P_A$ larger than $P_B$ ?) |                              |                                |                       |                       |
|---|------------------------------|------------------------------|--------------------------------|--------------------------------|---|------------------------------|--------------------------------|-----------------------|-----------------------|
| Sample<br>Size<br>$n_A = n_B$   | $A_1, A_2$                   |                              |                                |                                | Sample<br>Size<br>$n_A = n_B$   | $A_1, A_2$                   |                                |                       |                       |
| 13  | 0,5                          | 1,7                          | 2,8                            | 3,9                            | 13  | 0,7                          | 1,9                            | 2,10                  |                       |
| 14  | 0,5                          | 1,7                          | 2,8                            | 3,10                           | 14  | 0,7                          | 1,9                            | 2,10                  | 3,11                  |
| 15  | 0,5                          | 1,7                          | 2,9                            | 3,10<br>4,11                   | 15  | 0,7                          | 1,9                            | 2,10                  | 3,11                  |
| 16  | 0,5<br>4,11                  | 1,7                          | 2,9                            | 3,10                           | 16  | 0,7                          | 1,9                            | 2,10                  | 3,12                  |
| 17  | 0,5<br>4,11                  | 1,7<br>5,12                  | 2,9                            | 3,10                           | 17  | 0,7<br>4,13                  | 1,9                            | 2,11                  | 3,12                  |
| 18  | 0,5<br>4,11                  | 1,7<br>5,12                  | 2,9                            | 3,10                           | 18  | 0,7<br>4,13                  | 1,9                            | 2,11                  | 3,12                  |
| 19  | 0,5<br>4,11                  | 1,7<br>5,12                  | 2,9                            | 3,10                           | 19  | 0,7<br>4,13                  | 1,9<br>5,14                    | 2,11                  | 3,12                  |
| 20  | 0,5<br>4,11                  | 1,7<br>5,13                  | 2,9<br>6,14                    | 3,10                           | 20  | 0,7<br>4,13                  | 1,9<br>5,15                    | 2,11                  | 3,12                  |
| 30  | 0,6<br>4,12<br>8,17          | 1,8<br>5,13<br>9,18          | 2,9<br>6,15<br>10,19           | 3,11<br>7,16                   | 30  | 0,8<br>4,15                  | 1,10<br>9,20                   | 2,12                  | 3,13                  |
| 40  | 0,6<br>4,12<br>8,18          | 1,8<br>5,14<br>9,19          | 2,9<br>6,15<br>10,20           | 3,11<br>7,16<br>15,25          | 40  | 0,8<br>4,15<br>13,26         | 1,10<br>5,17                   | 2,12<br>8,20          | 3,14<br>9,22          |
| 50  | 0,6<br>4,13<br>8,18<br>19,30 | 1,8<br>5,14<br>9,19          | 2,10<br>6,15<br>10,20          | 3,11<br>7,17<br>11,22          | 50  | 0,8<br>4,15<br>9,22          | 1,10<br>5,17<br>10,24          | 2,12<br>6,18<br>18,32 | 3,14<br>7,20          |
| 60  | 0,6<br>4,13<br>8,18<br>12,23 | 1,8<br>5,14<br>9,20<br>13,24 | 2,10<br>6,16<br>10,21<br>14,26 | 3,11<br>7,17<br>11,22<br>24,36 | 60  | 0,8<br>4,16<br>9,23<br>20,36 | 1,10<br>5,17<br>11,25<br>22,38 | 2,12<br>6,19<br>12,27 | 3,14<br>8,21<br>19,34 |



## TABLES

TABLE A-28 (Continued). MINIMUM CONTRASTS REQUIRED FOR SIGNIFICANCE IN  
2 × 2 TABLES WITH EQUAL SAMPLES

| 5% Level, Two-Sided (Is $P_A$ different from $P_B$ )?<br>2.5% Level, One-Sided (Is $P_A$ larger than $P_B$ ?) |            |       |        |       | 1% Level, Two-Sided (Is $P_A$ different from $P_B$ )?<br>0.5% Level, One-Sided (Is $P_A$ larger than $P_B$ ?) |            |        |       |       |
|---|------------|-------|--------|-------|---|------------|--------|-------|-------|
| Sample<br>Size<br>$n_A = n_B$   | $A_1, A_2$ |       |        |       | Sample<br>Size<br>$n_A = n_B$   | $A_1, A_2$ |        |       |       |
| 70  | 0,6        | 1,8   | 2,10   | 3,11  | 70  | 0,8        | 1,10   | 2,12  | 3,14  |
|   | 4,13       | 5,14  | 6,16   | 7,17  |   | 4,16       | 5,17   | 6,19  | 7,20  |
|   | 8,18       | 9,20  | 10,21  | 11,22 |   | 8,22       | 10,24  | 11,26 | 14,29 |
|   | 12,23      | 13,25 | 18,30  | 19,32 |   | 15,31      | 21,37  | 22,39 | 26,43 |
|   | 20,33      | 28,41 |        |       |   |            |        |       |       |
| 80  | 0,6        | 1,8   | 2,10   | 3,11  | 80  | 0,8        | 1,10   | 2,12  | 3,14  |
|   | 4,13       | 5,14  | 6,16   | 7,17  |   | 4,16       | 5,18   | 6,19  | 7,21  |
|   | 8,19       | 9,20  | 10,21  | 11,22 |   | 9,23       | 10,25  | 12,27 | 13,29 |
|   | 12,24      | 13,25 | 14,26  | 15,27 |   | 16,32      | 17,34  | 24,41 | 25,43 |
|   | 16,29      | 23,36 | 24,38  | 33,47 |   | 31,49      |        |       |       |
| 90  | 0,6        | 1,8   | 2,10   | 3,11  | 90  | 0,8        | 1,10   | 2,12  | 3,14  |
|   | 4,13       | 5,14  | 6,16   | 7,17  |   | 4,16       | 5,18   | 6,19  | 7,21  |
|   | 8,19       | 9,20  | 10,21  | 11,23 |   | 8,22       | 9,24   | 11,26 | 12,28 |
|   | 12,24      | 13,25 | 14,26  | 15,28 |   | 15,31      | 16,33  | 19,36 | 20,38 |
|   | 20,33      | 21,35 | 31,45  | 32,47 |   | 28,46      | 29,48  | 35,54 |       |
| 100   | 0,6        | 1,8   | 2,10   | 3,11  | 100   | 0,8        | 1,10   | 2,13  | 3,14  |
|   | 4,13       | 5,15  | 6,16   | 7,17  |   | 4,16       | 5,18   | 6,19  | 7,21  |
|   | 8,19       | 9,20  | 10,21  | 11,23 |   | 8,22       | 9,24   | 10,25 | 11,27 |
|   | 12,24      | 13,25 | 14,27  | 18,31 |   | 14,30      | 15,32  | 18,35 | 19,37 |
|   | 19,33      | 25,39 | 26,41  | 42,57 |   | 23,41      | 24,43  | 33,52 | 34,54 |
| 150   | 0,6        | 1,8   | 2,10   | 3,12  | 150   | 0,8        | 1,11   | 2,13  | 3,15  |
|   | 4,13       | 5,15  | 6,16   | 7,18  |   | 4,16       | 5,18   | 6,20  | 7,21  |
|   | 8,19       | 9,20  | 10,22  | 11,23 |   | 8,23       | 9,24   | 10,26 | 11,27 |
|   | 12,24      | 13,26 | 14,27  | 15,28 |   | 12,29      | 14,31  | 15,33 | 17,35 |
|   | 16,30      | 19,33 | 20,35  | 25,40 |   | 18,37      | 21,40  | 22,42 | 26,46 |
| 200   | 26,42      | 32,48 | 33,50  | 41,58 | 200   | 27,48      | 31,52  | 32,54 | 39,61 |
|   | 42,60      | 66,84 |        |       |   | 40,63      | 51,74  | 52,76 | 63,87 |
|   | 0,6        | 1,8   | 2,10   | 3,12  |   | 0,8        | 1,11   | 2,13  | 3,15  |
|   | 4,13       | 5,15  | 6,16   | 7,18  |   | 4,16       | 5,18   | 6,20  | 7,21  |
|   | 8,19       | 9,21  | 10,22  | 11,23 |   | 8,23       | 9,24   | 10,26 | 11,27 |
| 200   | 12,25      | 13,26 | 14,27  | 15,29 | 200   | 12,29      | 13,30  | 14,32 | 16,34 |
|   | 18,32      | 19,34 | 22,37  | 23,39 |   | 17,36      | 19,38  | 20,40 | 23,43 |
|   | 27,43      | 28,45 | 33,50  | 34,52 |   | 24,45      | 26,47  | 27,49 | 31,53 |
|   | 41,59      | 42,61 | 51,70  | 52,72 |   | 32,55      | 36,59  | 37,61 | 43,67 |
|   | 65,85      | 66,87 | 89,110 |       |   | 44,69      | 51,76  | 52,78 | 63,89 |
|   |            |       |        |       |   | 64,91      | 86,118 |       |       |

## TABLES

TABLE A-28 (Continued). MINIMUM CONTRASTS REQUIRED FOR SIGNIFICANCE IN  
2 × 2 TABLES WITH EQUAL SAMPLES

| 5% Level, Two-Sided (Is $P_A$ different from $P_B$ )?<br>2.5% Level, One-Sided (Is $P_A$ larger than $P_B$ ?) |            |         |         |         | 1% Level, Two-Sided (Is $P_A$ different from $P_B$ )?<br>0.5% Level, One-Sided (Is $P_A$ larger than $P_B$ ?) |            |         |         |         |
|---|------------|---------|---------|---------|---|------------|---------|---------|---------|
| Sample Size<br>$n_A = n_B$  | $A_1, A_2$ |         |         |         | Sample Size<br>$n_A = n_B$  | $A_1, A_2$ |         |         |         |
| 300   | 0,6        | 1,8     | 2,10    | 3,12    | 300   | 0,8        | 1,11    | 2,13    | 3,15    |
|   | 4,13       | 5,15    | 6,16    | 7,18    |   | 4,17       | 5,18    | 6,20    | 7,22    |
|   | 8,19       | 9,21    | 10,22   | 11,24   |   | 8,23       | 9,25    | 10,26   | 11,28   |
|   | 12,25      | 13,26   | 14,28   | 15,29   |   | 12,29      | 13,31   | 15,33   | 16,35   |
|   | 16,30      | 17,31   | 18,33   | 19,34   |   | 17,36      | 18,38   | 20,40   | 21,42   |
|   | 20,35      | 21,37   | 24,40   | 25,42   |   | 23,44      | 24,46   | 27,49   | 28,51   |
|   | 29,46      | 30,48   | 35,53   | 36,55   |   | 31,54      | 32,56   | 35,59   | 36,61   |
|   | 41,60      | 42,62   | 48,68   | 49,70   |   | 40,65      | 41,67   | 45,71   | 46,73   |
|   | 56,77      | 57,79   | 66,88   | 67,90   |   | 51,78      | 52,80   | 58,86   | 59,88   |
|   | 78,101     | 79,103  | 95,119  | 96,121  |   | 66,95      | 67,97   | 76,106  | 77,108  |
|   | 137,162    |         |         |         |   | 88,119     | 89,121  | 107,139 | 108,141 |
|   |            |         |         |         |   | 133,166    |         |         |         |
| 400   | 0,6        | 1,8     | 2,10    | 3,12    | 400   | 0,8        | 1,11    | 2,13    | 3,15    |
|   | 4,13       | 5,15    | 6,17    | 7,18    |   | 4,17       | 5,18    | 6,20    | 7,22    |
|   | 8,19       | 9,21    | 10,22   | 11,24   |   | 8,23       | 9,25    | 10,26   | 11,28   |
|   | 12,25      | 13,26   | 14,28   | 15,29   |   | 12,29      | 13,31   | 14,32   | 15,34   |
|   | 16,30      | 17,32   | 20,35   | 21,37   |   | 17,36      | 18,38   | 19,39   | 20,41   |
|   | 24,40      | 25,42   | 28,45   | 29,47   |   | 22,43      | 23,45   | 26,48   | 27,50   |
|   | 33,51      | 34,53   | 38,57   | 39,59   |   | 29,52      | 30,54   | 33,57   | 34,59   |
|   | 44,64      | 45,66   | 51,72   | 52,74   |   | 37,62      | 38,64   | 41,67   | 42,69   |
|   | 58,80      | 59,82   | 67,90   | 68,92   |   | 46,73      | 47,75   | 52,80   | 53,82   |
|   | 76,100     | 77,102  | 87,112  | 88,114  |   | 57,86      | 58,88   | 64,94   | 65,96   |
|   | 100,128    | 101,128 | 117,144 | 118,146 |   | 71,102     | 72,104  | 79,111  | 80,113  |
|   | 141,169    | 142,171 | 185,214 |         |   | 88,121     | 89,123  | 98,132  | 99,134  |
|   |            |         |         |         |   | 111,146    | 112,148 | 127,163 | 128,165 |
| 500   | 0,6        | 1,8     | 2,10    | 3,12    | 500   | 0,8        | 1,11    | 2,13    | 3,15    |
|   | 4,13       | 5,15    | 6,17    | 7,18    |   | 4,17       | 5,18    | 6,20    | 7,22    |
|   | 8,19       | 9,21    | 10,22   | 11,24   |   | 8,24       | 9,25    | 10,27   | 11,28   |
|   | 12,25      | 13,26   | 14,28   | 15,29   |   | 12,30      | 14,32   | 15,34   | 16,35   |
|   | 16,30      | 17,32   | 18,33   | 19,34   |   | 17,37      | 19,39   | 20,41   | 22,43   |
|   | 20,36      | 23,39   | 24,41   | 27,44   |   | 23,45      | 25,47   | 26,49   | 28,51   |
|   | 28,46      | 32,50   | 33,52   | 37,56   |   | 29,53      | 32,56   | 33,58   | 35,60   |
|   | 38,58      | 42,62   | 43,64   | 48,69   |   | 36,62      | 40,66   | 41,68   | 44,71   |
|   | 49,71      | 55,77   | 56,79   | 62,85   |   | 45,73      | 49,77   | 50,79   | 54,83   |
|   | 63,87      | 70,94   | 71,96   | 79,104  |   | 55,85      | 59,89   | 60,91   | 65,96   |
|   | 80,106     | 89,115  | 90,117  | 100,127 |   | 66,98      | 72,104  | 73,106  | 79,112  |
|   | 101,129    | 113,141 | 114,143 | 128,157 |   | 80,114     | 86,120  | 87,122  | 95,130  |
|   | 129,159    | 147,177 | 148,179 | 172,203 |   | 96,132     | 104,140 | 105,142 | 115,152 |
| 178,205   | 234,266    |         |         |         |   | 116,154    | 127,165 | 128,167 | 141,180 |
|   |            |         |         |         |   | 142,182    | 159,199 | 160,201 | 184,225 |
|   |            |         |         |         |   | 185,227    | 229,271 |         |         |

## TABLES

TABLE A-29. TABLES FOR TESTING SIGNIFICANCE IN  $2 \times 2$  TABLES WITH UNEQUAL SAMPLES

Table A-29 shows (1) in bold type for given  $a_1$ ,  $n_1$ , and  $n_2$ , the value of  $a_2$  which is just significant at the probability level quoted in parentheses for a two-sided test and without parentheses for a one-sided test, (2) in small type, for given  $n_1$ ,  $n_2$ , and  $a_1 + a_2$ , the exact probability (if there is independence) that  $a_2$  is equal to or less than the integer shown in bold type.

|         |         | Significance Level |                |                 |                |                 |         | Significance Level |            |                |                 |                |                 |
|---------|---------|--------------------|----------------|-----------------|----------------|-----------------|---------|--------------------|------------|----------------|-----------------|----------------|-----------------|
|         |         | $\alpha_1$         | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |         |                    | $\alpha_1$ | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |
| $n_1=3$ | $n_2=3$ | 3                  | 0.050          | —               | —              | —               | $n_1=8$ | $n_2=8$            | 8          | 4.038          | 3.013           | 2.003          | 2.003           |
| $n_1=4$ | $n_2=4$ | 4                  | 0.014          | 0.014           | —              | —               |         | 7                  | 2.030      | 2.030          | 1.008 +         | 0.001          |                 |
|         | 3       | 4                  | 0.029          | —               | —              | —               |         | 6                  | 1.020      | 1.030          | 0.003           | 0.003          |                 |
|         |         | 5                  | 0.013          | 0.013           | —              | —               |         | 5                  | 0.038      | —              | —               | —              |                 |
| $n_1=5$ | $n_2=5$ | 5                  | 1.024          | 1.024           | 0.004          | 0.004           |         | 7                  | 8          | 3.028          | 2.007           | 2.007          | 1.001           |
|         | 4       | 4                  | 0.034          | 0.034           | —              | —               | 7       |                    | 2.035      | 1.009          | 1.009           | 0.001          |                 |
|         |         | 5                  | 1.048          | 0.008           | 0.008          | —               | 6       |                    | 1.033      | 0.008          | 0.008           | —              |                 |
|         |         | 4                  | 0.040          | —               | —              | —               | 5       |                    | 0.019      | 0.019          | —               | —              |                 |
|         | 3       | 5                  | 0.018          | 0.018           | —              | —               | 6       | 8                  | 2.015      | 2.015          | 1.003           | 1.003          |                 |
| 4       |         | 5                  | 0.018          | 0.018           | —              | —               |         | 7                  | 1.018      | 1.018          | 0.002           | 0.002          |                 |
|         |         | 6                  | 0.009          | 0.009           | 0.009          | —               |         | 6                  | 0.009      | 0.009          | 0.009           | —              |                 |
| 2       |         | 5                  | 0.048          | —               | —              | 5               |         | 0.025              | —          | —              | —               |                |                 |
| $n_1=6$ |         | $n_2=6$            | 6              | 2.030           | 1.008          | 1.008           | 0.001   | 5                  | 8          | 2.035          | 1.007           | 1.007          | 0.001           |
|         | 5       | 5                  | 1.040          | 0.008           | 0.008          | —               | 7       |                    | 1.033      | 0.005          | 0.005           | 0.005          |                 |
|         |         | 4                  | 0.020          | —               | —              | —               | 6       |                    | 0.015      | 0.015          | —               | —              |                 |
|         |         | 5                  | 6              | 1.015 +         | 1.015 +        | 0.002           | 0.002   |                    | 5          | 0.044          | —               | —              | —               |
|         | 4       | 5                  | 0.013          | 0.013           | —              | —               | 4       | 8                  | 1.018      | 1.018          | 0.002           | 0.002          |                 |
|         |         | 4                  | 0.045 +        | —               | —              | —               |         | 7                  | 0.010 +    | 0.010 +        | —               | —              |                 |
|         |         | 6                  | 0.030          | —               | —              | —               |         | 6                  | 0.030      | —              | —               | —              |                 |
|         | 3       | 6                  | 1.033          | 0.005           | 0.005          | 0.005           | 3       | 8                  | 0.008      | 0.008          | 0.008           | —              |                 |
|         |         | 5                  | 0.034          | 0.034           | —              | —               |         | 7                  | 0.024      | 0.024          | —               | —              |                 |
|         |         | 2                  | 6              | 0.013           | 0.013          | —               | —       | 2                  | 8          | 0.023          | 0.023           | —              | —               |
| 2       | 6       | 0.026              | —              | —               | —              | $n_1=9$         | $n_2=9$ | 9                  | 5.041      | 4.018          | 3.005           | 3.005          |                 |
|         | 7       | 7                  | 3.025          | 2.010 +         | 1.003          |                 | 1.003   | 8                  | 3.023      | 3.023          | 2.008           | 1.002          |                 |
| 6       |         | 1.018              | 1.018          | 0.003           | 0.003          |                 | 7       | 2.023              | 1.008      | 1.008          | 0.001           |                |                 |
| 5       |         | 0.010 +            | 0.010 +        | —               | —              |                 | 6       | 1.025              | 1.025      | 0.005          | 0.005           |                |                 |
| 4       |         | 0.035              | —              | —               | —              |                 | 5       | 0.015              | 0.015      | —              | —               |                |                 |
| 6       | 7       | 2.031              | 2.031          | 1.003           | 1.005          |                 | 8       | 9                  | 4.039      | 3.009          | 3.009           | 2.002          |                 |
|         | 6       | 1.025 +            | 0.004          | 0.004           | 0.004          |                 |         | 8                  | 3.043      | 2.013          | 1.003           | 1.003          |                 |
|         | 5       | 0.015              | 0.015          | —               | —              |                 |         | 7                  | 2.044      | 1.013          | 0.002           | 0.002          |                 |
|         | 4       | 0.045              | —              | —               | —              |                 |         | 6                  | 1.035      | 0.007          | 0.007           | —              |                 |
| 5       | 7       | 2.045 +            | 1.018 +        | 0.001           | 0.001          |                 | 7       | 5                  | 0.030      | 0.030          | —               | —              |                 |
|         | 6       | 1.045 +            | 0.008          | 0.008           | —              | 9               |         | 3.019              | 3.019      | 2.005          | 2.005           |                |                 |
|         | 5       | 0.037              | —              | —               | —              | 8               |         | 2.024              | 2.024      | 1.006          | 0.001           |                |                 |
| 4       | 7       | 1.024              | 1.024          | 0.003           | 0.003          | 6               |         | 7                  | 1.030      | 1.030          | 0.003           | 0.003          |                 |
|         | 6       | 0.015 +            | 0.015 +        | —               | —              |                 | 6       | 0.010 +            | 0.010 +    | —              | —               |                |                 |
|         | 5       | 0.045 +            | —              | —               | —              |                 | 5       | 0.029              | —          | —              | —               |                |                 |
| 3       | 7       | 0.008              | 0.008          | 0.008           | —              |                 | 6       | 9                  | 2.044      | 2.011          | 1.002           | 1.002          |                 |
|         | 6       | 0.033              | —              | —               | —              | 8               |         | 2.047              | 1.011      | 0.001          | 0.001           |                |                 |
| 2       | 7       | 0.028              | —              | —               | —              | 7               |         | 1.035              | 0.006      | 0.006          | —               |                |                 |
|         |         |                    |                |                 |                | 6               |         | 0.017              | 0.017      | —              | —               |                |                 |
|         |         |                    |                |                 |                | 5               | 0.043   | —                  | —          | —              |                 |                |                 |

Adapted from a table of the same form with probabilities to 4 decimals prepared in the Statistical Engineering Laboratory, National Bureau of Standards, by Anna M. Glinski and John Van Dyke from *Tables of the Hypergeometric Probability Distribution* by Gerald J. Lieberman and Donald B. Owen, Technical Report No. 50 (Contract Nonr-225(53)) (NR 642 002). Applied Mathematics and Statistics Laboratories, Stanford University, Stanford, California.

## TABLES

TABLE A-29 (Continued). TABLES FOR TESTING SIGNIFICANCE IN  $2 \times 2$  TABLES WITH UNEQUAL SAMPLES

|                       | $n_1$ | Significance Level |                 |                |                 |                       | $n_1$ | Significance Level |                 |                |                 |
|-----------------------|-------|--------------------|-----------------|----------------|-----------------|-----------------------|-------|--------------------|-----------------|----------------|-----------------|
|                       |       | 0.05<br>(0.10)     | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |                       |       | 0.05<br>(0.10)     | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |
| $n_1=9 \quad n_2=5$   | 9     | 2.027              | 1.005 -         | 1.005 -        | 1.005 -         | $n_1=10 \quad n_2=4$  | 10    | 1.011              | 1.011           | 0.001          | 0.001           |
|                       | 8     | 1.022              | 1.022           | 0.003          | 0.003           |                       | 9     | 1.041              | 0.005 -         | 0.005 -        | 0.005 -         |
|                       | 7     | 0.010 +            | 0.010 +         | —              | —               |                       | 8     | 0.015 -            | 0.015 -         | —              | —               |
|                       | 6     | 0.028              | —               | —              | —               |                       | 7     | 0.025 -            | —               | —              | —               |
|                       | 4     | 1.014              | 1.014           | 0.001          | 0.001           |                       | 3     | 1.028              | 0.003           | 0.003          | 0.003           |
|                       |       | 0.007              | 0.007           | 0.007          | —               |                       |       | 0.014              | 0.014           | —              | —               |
|                       |       | 0.021              | 0.021           | —              | —               |                       |       | 0.025 -            | —               | —              | —               |
|                       |       | 0.049              | —               | —              | —               |                       |       | 0.016 +            | 0.016 +         | —              | —               |
|                       | 3     | 1.045 +            | 0.005 -         | 0.005 -        | 0.005 -         |                       | 2     | 0.045 +            | —               | —              | —               |
|                       |       | 0.015              | 0.015           | —              | —               |                       |       | —                  | —               | —              | —               |
|                       |       | 0.045 +            | —               | —              | —               |                       |       | —                  | —               | —              | —               |
|                       | 2     | 0.018              | 0.018           | —              | —               | $n_1=11 \quad n_2=11$ | 11    | 7.045 +            | 6.018           | 5.006          | 4.002           |
| $n_1=10 \quad n_2=10$ | 10    | 6.043              | 5.018           | 4.005 +        | 3.002           |                       | 10    | 5.022              | 4.012           | 3.004          | 3.004           |
|                       | 9     | 4.029              | 3.010 -         | 2.010 -        | 2.003           |                       | 9     | 4.040              | 3.015 -         | 2.004          | 2.004           |
|                       | 8     | 3.035 -            | 2.012           | 1.003          | 1.003           |                       | 8     | 3.043              | 2.018 -         | 1.004          | 1.004           |
|                       | 7     | 2.035 -            | 1.010 -         | 1.010 -        | 0.002           |                       | 7     | 2.040              | 1.012           | 0.002          | 0.002           |
|                       | 6     | 1.029              | 0.008 +         | 0.008 +        | —               |                       | 6     | 1.032              | 0.006           | 0.006          | —               |
|                       | 5     | 0.016              | 0.016           | —              | —               |                       | 5     | 0.018              | 0.018           | —              | —               |
|                       | 4     | 0.043              | —               | —              | —               |                       | 4     | 0.045 +            | —               | —              | —               |
|                       | 9     | 10                 | 5.033           | 4.011          | 3.003           |                       | 10    | 11                 | 6.035 +         | 5.012          | 4.004           |
|                       |       | 9                  | 4.050 -         | 3.017          | 2.005 -         |                       |       | 10                 | 4.021           | 4.021          | 3.007           |
|                       |       | 8                  | 2.019           | 2.019          | 1.004           |                       |       | 9                  | 3.024           | 3.024          | 2.007           |
|                       |       | 7                  | 1.015 -         | 1.015 -        | 0.002           |                       |       | 8                  | 2.023           | 2.023          | 1.006           |
|                       |       | 6                  | 1.040           | 0.008          | 0.008           |                       |       | 7                  | 1.017           | 1.017          | 0.003           |
|                       |       | 5                  | 0.022           | 0.022          | —               |                       |       | 6                  | 1.043           | 0.009          | 0.009           |
|                       | 8     | 10                 | 4.023           | 4.023          | 3.007           |                       | 9     | 11                 | 5.024           | 4.008          | 4.006           |
|                       |       | 9                  | 3.032           | 2.009          | 2.009           |                       |       | 10                 | 4.035           | 3.012          | 2.003           |
|                       |       | 8                  | 2.031           | 1.008          | 1.008           |                       |       | 9                  | 3.040           | 2.012          | 1.003           |
|                       |       | 7                  | 1.022           | 1.022          | 0.004           |                       |       | 8                  | 2.035 -         | 1.009          | 1.009           |
|                       |       | 6                  | 0.011           | 0.011          | —               |                       |       | 7                  | 1.025 -         | 1.025 -        | 0.004           |
|                       |       | 5                  | 0.029           | —              | —               |                       |       | 6                  | 0.012           | 0.012          | —               |
|                       | 7     | 10                 | 3.015 -         | 3.015 -        | 2.003           |                       | 8     | 11                 | 4.015           | 4.015          | 3.005 -         |
|                       |       | 9                  | 2.015           | 2.015          | 1.004           |                       |       | 10                 | 3.024           | 3.024          | 2.006           |
|                       |       | 8                  | 1.012           | 1.012          | 0.002           |                       |       | 9                  | 2.022           | 2.022          | 1.005 -         |
|                       |       | 7                  | 1.026           | 0.006          | 0.006           |                       |       | 8                  | 1.015 -         | 1.015 -        | 0.002           |
|                       |       | 6                  | 0.017           | 0.017          | —               |                       |       | 7                  | 1.027           | 0.007          | 0.007           |
|                       |       | 5                  | 0.041           | —              | —               |                       |       | 6                  | 0.017           | 0.017          | —               |
|                       | 6     | 10                 | 3.028           | 2.008          | 2.008           |                       | 7     | 11                 | 4.043           | 3.011          | 2.002           |
|                       |       | 9                  | 2.026           | 1.008          | 1.008           |                       |       | 10                 | 3.047           | 2.013          | 1.002           |
|                       |       | 8                  | 1.024           | 1.024          | 0.002           |                       |       | 9                  | 2.039           | 1.009          | 1.009           |
|                       |       | 7                  | 0.010 +         | 0.010 +        | —               |                       |       | 8                  | 1.025 -         | 1.025 -        | 0.004           |
|                       | 5     | 10                 | 2.022           | 2.022          | 1.004           |                       | 6     | 11                 | 3.029           | 2.006          | 2.006           |
|                       |       | 9                  | 1.017           | 1.017          | 0.002           |                       |       | 10                 | 2.025           | 1.005 +        | 1.005 +         |
|                       |       | 8                  | 1.047           | 0.007          | 0.007           |                       |       | 9                  | 1.018           | 1.018          | 0.002           |
|                       |       | 7                  | 0.019           | 0.019          | —               |                       |       | 8                  | 0.025 -         | 0.025 -        | —               |

## TABLES

TABLE A-29 (Continued). TABLES FOR TESTING SIGNIFICANCE IN  $2 \times 2$  TABLES WITH UNEQUAL SAMPLES

|                       | $a_1$ | Significance Level |                 |                |                 |                       | $a_1$ | Significance Level |                 |                |                 |
|-----------------------|-------|--------------------|-----------------|----------------|-----------------|-----------------------|-------|--------------------|-----------------|----------------|-----------------|
|                       |       | 0.05<br>(0.10)     | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |                       |       | 0.05<br>(0.10)     | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |
| $n_1=9 \quad n_2=5$   | 9     | 2.027              | 1.005 -         | 1.005 -        | 1.005 -         | $n_1=10 \quad n_2=4$  | 10    | 1.011              | 1.011           | 0.001          | 0.001           |
|                       |       | 1.023              | 1.023           | 0.003          | 0.005           |                       |       | 1.041              | 0.005 -         | 0.005 -        | 0.005 -         |
|                       |       | 0.010 +            | 0.010 +         | —              | —               |                       |       | 0.015 -            | 0.015 -         | —              | —               |
|                       |       | 0.028              | —               | —              | —               |                       |       | 0.035 -            | —               | —              | —               |
|                       | 4     | 1.014              | 1.014           | 0.001          | 0.001           |                       | 3     | 1.038              | 0.003           | 0.003          | 0.003           |
|                       |       | 0.007              | 0.007           | 0.007          | —               |                       |       | 0.014              | 0.014           | —              | —               |
|                       |       | 0.031              | 0.021           | —              | —               |                       |       | 0.025 -            | —               | —              | —               |
|                       |       | 0.049              | —               | —              | —               |                       |       | 0.015 +            | 0.015 +         | —              | —               |
|                       | 3     | 1.045 +            | 0.005 -         | 0.005 -        | 0.005 -         |                       | 2     | 0.045 +            | —               | —              | —               |
|                       |       | 0.018              | 0.018           | —              | —               |                       |       | —                  | —               | —              | —               |
|                       |       | 0.045 +            | —               | —              | —               | $n_1=11 \quad n_2=11$ | 11    | 7.045 +            | 6.018           | 5.006          | 4.002           |
| $n_1=10 \quad n_2=10$ | 10    | 6.043              | 5.016           | 4.005 +        | 3.003           |                       |       | 5.032              | 4.012           | 3.004          | 2.004           |
|                       |       | 4.039              | 3.010 -         | 3.010 -        | 2.003           |                       |       | 4.040              | 3.015 -         | 2.004          | 2.004           |
|                       |       | 3.035 -            | 2.013           | 1.003          | 1.003           |                       |       | 3.043              | 2.015 -         | 1.004          | 1.004           |
|                       |       | 2.035 -            | 1.010 -         | 1.010 -        | 0.002           |                       |       | 2.040              | 1.012           | 0.002          | 0.002           |
|                       | 9     | 1.029              | 0.005 +         | 0.005 +        | —               |                       |       | 1.023              | 0.006           | 0.006          | —               |
|                       |       | 0.016              | 0.016           | —              | —               |                       |       | 0.018              | 0.018           | —              | —               |
|                       |       | 0.043              | —               | —              | —               |                       |       | 0.045 +            | —               | —              | —               |
|                       |       | 0.043              | —               | —              | —               |                       | 10    | 6.025 +            | 5.012           | 4.004          | 4.004           |
|                       | 8     | 5.033              | 4.011           | 3.003          | 3.003           |                       |       | 4.021              | 4.021           | 3.007          | 2.002           |
|                       |       | 4.050 -            | 3.017           | 2.005 -        | 2.005 -         |                       |       | 3.024              | 3.024           | 2.007          | 1.002           |
|                       |       | 3.019              | 2.019           | 1.004          | 1.004           |                       |       | 2.023              | 2.023           | 1.006          | 0.001           |
|                       |       | 2.019              | 2.019           | 1.004          | 1.004           |                       |       | 1.017              | 1.017           | 0.003          | 0.003           |
|                       | 7     | 1.015 -            | 1.015 -         | 0.002          | 0.002           |                       | 9     | 1.043              | 0.009           | 0.009          | —               |
|                       |       | 1.040              | 0.008           | 0.008          | —               |                       |       | 0.023              | 0.023           | —              | —               |
|                       |       | 0.022              | 0.022           | —              | —               |                       |       | 5.023              | 4.008           | 4.008          | 3.002           |
|                       |       | 4.023              | 4.023           | 3.007          | 2.002           |                       |       | 4.023              | 3.012           | 2.003          | 2.003           |
|                       | 6     | 3.032              | 2.009           | 2.009          | 1.002           |                       |       | 3.040              | 2.013           | 1.003          | 1.003           |
|                       |       | 2.031              | 1.008           | 1.008          | 0.001           |                       |       | 2.025 -            | 1.009           | 1.009          | 0.001           |
|                       |       | 1.023              | 1.023           | 0.004          | 0.004           |                       |       | 1.025 -            | 1.025 -         | 0.004          | 0.004           |
|                       |       | 0.011              | 0.011           | —              | —               |                       | 8     | 0.012              | 0.012           | —              | —               |
|                       | 5     | 0.029              | —               | —              | —               |                       |       | 0.020              | —               | —              | —               |
|                       |       | 3.015 -            | 3.015 -         | 2.002          | 2.002           |                       |       | 4.018              | 4.018           | 3.005 -        | 3.005 -         |
|                       |       | 2.018              | 2.018           | 1.004          | 1.004           |                       | 7     | 3.024              | 3.024           | 2.005          | 1.001           |
|                       | 4     | 1.015              | 1.015           | 0.002          | 0.002           |                       |       | 2.022              | 2.022           | 1.005 -        | 1.005 -         |
|                       |       | 1.029              | 0.008           | 0.008          | —               |                       |       | 1.015 -            | 1.015 -         | 0.002          | 0.002           |
|                       |       | 0.017              | 0.017           | —              | —               |                       |       | 1.037              | 0.007           | 0.007          | —               |
|                       |       | 0.041              | —               | —              | —               |                       |       | 0.017              | 0.017           | —              | —               |
|                       | 3     | 3.028              | 2.008           | 2.008          | 1.001           |                       | 6     | 0.040              | —               | —              | —               |
|                       |       | 2.026              | 1.008           | 1.008          | 0.001           |                       |       | 4.042              | 3.011           | 2.003          | 2.003           |
|                       |       | 1.024              | 1.024           | 0.003          | 0.003           |                       |       | 3.047              | 2.013           | 1.003          | 1.003           |
|                       |       | 0.010 +            | 0.010 +         | —              | —               |                       |       | 2.029              | 1.009           | 1.009          | 0.001           |
|                       | 2     | 0.026              | —               | —              | —               |                       |       | 1.025 -            | 1.025 -         | 0.004          | 0.004           |
|                       |       | 2.022              | 2.022           | 1.004          | 1.004           |                       | 5     | 0.010 +            | 0.010 +         | —              | —               |
|                       |       | 1.017              | 1.017           | 0.003          | 0.003           |                       |       | 0.025 -            | 0.025 -         | —              | —               |
|                       |       | 1.047              | 0.007           | 0.007          | —               |                       |       | 3.029              | 2.008           | 2.008          | 1.001           |
|                       | 1     | 0.019              | 0.019           | —              | —               |                       |       | 2.028              | 1.005 +         | 1.005 +        | 0.001           |
|                       |       | 0.042              | —               | —              | —               |                       |       | 1.018              | 1.018           | 0.002          | 0.002           |

## TABLES

TABLE A-29 (Continued). TABLES FOR TESTING SIGNIFICANCE IN  $2 \times 2$  TABLES WITH UNEQUAL SAMPLES

|                       |                       | Significance Level |                |                 |                       |                       |                       | Significance Level    |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|-----------------------|-----------------------|--------------------|----------------|-----------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-------|-------|-------|-------|-------|-------|
|                       |                       | $\alpha_1$         | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02)        | 0.005<br>(0.01)       |                       |                       | $\alpha_1$            | 0.05<br>(0.10)        | 0.025<br>(0.05)       | 0.01<br>(0.02)        | 0.005<br>(0.01)       |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
| $n_1=11 \quad n_2=6$  | 8                     | 8                  | 1.043          | 0.007           | 0.007                 | —                     | $n_1=12 \quad n_2=9$  | 7                     | 7                     | 1.037                 | 0.007                 | 0.007                 | —                     |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 7                  | 0.017          | 0.017           | —                     | —                     |                       |                       | 6                     | 0.017                 | 0.017                 | —                     | —                     |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 6                  | 0.037          | —               | —                     | —                     |                       |                       | 5                     | 0.039                 | —                     | —                     | —                     |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       | 5                     | 11                 | 2.018          | 2.018           | 1.003                 | 1.003                 |                       | 8                     | 12                    | 5.049                 | 4.014                 | 3.004                 | 3.004                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 10                 | 1.013          | 1.013           | 0.001                 | 0.001                 |                       |                       | 11                    | 3.018                 | 3.018                 | 2.004                 | 2.004                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 9                  | 1.036          | 0.005           | 0.005                 | 0.005                 |                       |                       | 10                    | 2.015 +               | 2.015 +               | 1.003                 | 1.003                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 8                  | 0.013          | 0.013           | —                     | —                     |                       |                       | 9                     | 2.040                 | 1.010                 | 1.010                 | 0.001                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 7                  | 0.029          | —               | —                     | —                     |                       |                       | 8                     | 1.025                 | 1.025                 | 0.004                 | 0.004                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       | 4                     | 11                 | 1.009          | 1.009           | 1.009                 | 0.001                 |                       | 7                     | 12                    | 4.036                 | 3.009                 | 3.009                 | 2.002                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 10                 | 1.033          | 0.004           | 0.004                 | 0.004                 |                       |                       | 11                    | 3.058                 | 2.010                 | 2.010                 | 1.002                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 9                  | 0.011          | 0.011           | —                     | —                     |                       |                       | 10                    | 2.029                 | 1.006                 | 1.006                 | 0.001                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 8                  | 0.026          | —               | —                     | —                     |                       |                       | 9                     | 1.017                 | 1.017                 | 0.002                 | 0.002                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       | 3                     | 11                 | 1.033          | 0.003           | 0.003                 | 0.003                 |                       | 6                     | 12                    | 4.036                 | 3.009                 | 3.009                 | 2.002                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 10                 | 0.011          | 0.011           | —                     | —                     |                       |                       | 11                    | 3.058                 | 2.010                 | 2.010                 | 1.002                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 9                  | 0.027          | —               | —                     | —                     |                       |                       | 10                    | 2.029                 | 1.006                 | 1.006                 | 0.001                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       | 2                     | 11                 | 0.013          | 0.013           | —                     | —                     |                       | 5                     | 12                    | 4.036                 | 3.009                 | 3.009                 | 2.002                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 10                 | 0.026          | —               | —                     | —                     |                       |                       | 11                    | 3.058                 | 2.010                 | 2.010                 | 1.002                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
| $n_1=12 \quad n_2=12$ | 12                    | 12                 | 8.047          | 7.019           | 6.007                 | 5.002                 | 11                    | 12                    | 7.027                 | 6.014                 | 5.005                 | 5.005                 | —                     |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 11                 | 6.034          | 5.014           | 4.005                 | 4.005                 |                       | 11                    | 5.024                 | 5.024                 | 4.006                 | 3.002                 | —                     |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 10                 | 5.045          | 4.018           | 3.006                 | 2.002                 |                       | 10                    | 4.029                 | 3.010 +               | 2.003                 | 2.003                 | —                     |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 9                  | 4.050          | 3.020           | 2.006                 | 1.001                 |                       | 9                     | 3.030                 | 2.009                 | 2.009                 | 1.002                 | —                     |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 8                  | 3.050          | 2.018           | 1.005                 | 1.005                 |                       | 8                     | 2.026                 | 1.007                 | 1.007                 | 0.001                 | —                     |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 7                  | 2.045          | 1.014           | 0.002                 | 0.002                 |                       | 7                     | 1.019                 | 1.019                 | 0.003                 | 0.003                 | —                     |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 6                  | 1.034          | 0.007           | 0.007                 | —                     |                       | 6                     | 1.045                 | 0.009                 | 0.009                 | —                     | —                     |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 5                  | 0.019          | 0.019           | —                     | —                     |                       | 5                     | 0.024                 | 0.024                 | —                     | —                     | —                     |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 4                  | 0.047          | —               | —                     | —                     |                       | 4                     | 0.047                 | —                     | —                     | —                     | —                     |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       | 11                    | 12                 | 7.027          | 6.014           | 5.005                 | 5.005                 |                       | 10                    | 12                    | 6.029                 | 5.010                 | 5.010                 | 4.003                 | —                     |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 11                 | 5.024          | 5.024           | 4.006                 | 3.002                 |                       |                       | 11                    | 5.045                 | 4.016 +               | 3.006                 | 3.006                 | —                     |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 10                 | 4.029          | 3.010 +         | 2.003                 | 2.003                 |                       |                       | 10                    | 4.048                 | 3.017                 | 2.005                 | 2.005                 | —                     |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 9                  | 3.030          | 2.009           | 2.009                 | 1.002                 |                       |                       | 9                     | 3.048                 | 2.013                 | 1.004                 | 1.004                 | —                     |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 8                  | 2.026          | 1.007           | 1.007                 | 0.001                 |                       |                       | 8                     | 2.038                 | 1.010 +               | 0.002                 | 0.002                 | —                     |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 7                  | 1.019          | 1.019           | 0.003                 | 0.003                 |                       |                       | 7                     | 1.026                 | 0.005                 | 0.005                 | 0.005                 | —                     |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       | 10                    | 12                 | 6.029          | 5.010           | 5.010                 | 4.003                 | 9                     | 12                    | 5.021                 | 5.021                 | 4.006                 | 3.002                 | —                     |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 11                 | 5.045          | 4.016 +         | 3.006                 | 3.006                 |                       | 11                    | 4.029                 | 3.009                 | 3.009                 | 2.002                 | —                     |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 10                 | 4.048          | 3.017           | 2.005                 | 2.005                 |                       | 10                    | 3.029                 | 2.008                 | 2.008                 | 1.002                 | —                     |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 9                  | 3.048          | 2.013           | 1.004                 | 1.004                 |                       | 9                     | 2.024                 | 2.024                 | 1.006                 | 0.001                 | —                     |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 8                  | 2.038          | 1.010 +         | 0.002                 | 0.002                 |                       | 8                     | 1.016                 | 1.016                 | 0.002                 | 0.002                 | —                     |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 7                  | 1.026          | 0.005           | 0.005                 | 0.005                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       | $n_1=13 \quad n_2=13$ | 13                 | 13             | 9.048           | 8.020                 | 7.007                 | 6.003                 | $n_1=13 \quad n_2=13$ | 13                    | 13                    | 9.048                 | 8.020                 | 7.007                 | 6.003                 |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       |                    | 12             | 7.027           | 6.015 +               | 5.006                 | 4.002                 |                       |                       | $n_1=13 \quad n_2=13$ | 13                    | 13                    | 9.048                 | 8.020                 | 7.007                 | 6.003                 |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       |                    | 11             | 6.046           | 5.021                 | 4.008                 | 3.002                 |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ | 13                    | 13                    | 9.048                 | 8.020                 | 7.007                 | 6.003                 |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 10                 | 4.024          | 4.024           | 3.008                 | 2.002                 | $n_1=13 \quad n_2=13$ |                       | 13                    |                       |                       |                       |                       | 13                    | 9.048                 | 8.020                 | 7.007                 | 6.003                 |                       |                       |                       |                       |       |       |       |       |       |       |
|                       |                       | 9                  | 3.024          | 3.024           | 2.008                 | 1.002                 |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       | 13                    | 13                    | 9.048                 | 8.020                 | 7.007                 | 6.003                 |                       |                       |                       |       |       |       |       |       |       |
| 8                     |                       | 2.021              | 2.021          | 1.006           | 0.001                 | $n_1=13 \quad n_2=13$ |                       |                       |                       |                       |                       |                       | 13                    |                       | 13                    | 9.048                 | 8.020                 | 7.007                 | 6.003                 |                       |                       |                       |       |       |       |       |       |       |
|                       |                       |                    |                |                 |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       |                       |                       |                       | 13                    | 13                    | 9.048                 | 8.020                 | 7.007                 | 6.003                 |                       |                       |       |       |       |       |       |       |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       | 13                    | 13                    | 9.048                 | 8.020                 | 7.007                 | 6.003                 |                       |       |       |       |       |       |       |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       |                       | 13                    | 13                    | 9.048                 | 8.020                 | 7.007                 | 6.003                 |       |       |       |       |       |       |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       | 13                    | 13                    | 9.048                 | 8.020                 | 7.007                 | 6.003 |       |       |       |       |       |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       | 13                    | 13                    | 9.048                 | 8.020                 | 7.007 | 6.003 |       |       |       |       |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       | 13                    | 13                    | 9.048                 | 8.020 | 7.007 | 6.003 |       |       |       |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       | 13                    | 13                    | 9.048 | 8.020 | 7.007 | 6.003 |       |       |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       | 13                    | 13    | 9.048 | 8.020 | 7.007 | 6.003 |       |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       | 13    | 13    | 9.048 | 8.020 | 7.007 | 6.003 |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |       | 13    | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |       |       | 13    | 13    | 9.048 | 8.020 |
|                       |                       |                    |                |                 | $n_1=13 \quad n_2=13$ |                       |                       | 13                    |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | 13    |       |       | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | 13    | 13    |       | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |       | 13    | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       | $n_1=13 \quad n_2=13$ | 13                    |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | 13    |       | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       | $n_1=13 \quad n_2=13$ |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |       | 13    | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       |                       | $n_1=13 \quad n_2=13$ | 13                    |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       |                       |                       |                       |                       |                       |                       | 13    |       | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       |                       |                       |                       |                       |                       |                       |                       |       | 13    | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       |                       |                       |                       | 13                    |                       |                       |                       |                       |                       |                       |                       |       |       | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       |                       |                       |                       |                       | 13    |       | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       |                       |                       |                       |       | 13    | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       | 13                    |                       |                       |                       |                       |       |       | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       |                       | 13    |       | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       |       | 13    | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       | 13                    |                       |       |       | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ | 13    |       | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 | $n_1=13 \quad n_2=13$ |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |       | 13    | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | 13                    |                       |       |       | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | 13    |       | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |       | 13    | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       | $n_1=13 \quad n_2=13$ |                       |                       |                       |                       |                       |                       |                       |                       |                       | 13                    |                       |       |       | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       | $n_1=13 \quad n_2=13$ |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       | 13    |       | 13    | 9.048 | 8.020 | 7.007 |
|                       |                       |                    |                |                 |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |                       |       |       |       |       |       |       |

TABLES

TABLE A-29 (Continued). TABLES FOR TESTING SIGNIFICANCE IN  $2 \times 2$  TABLES WITH UNEQUAL SAMPLES

| Significance Level | $\alpha$ | $n_1 = 18 \quad n_2 = 13$ |         |       |       |       |       |       |       |       |       |       |       | Significance Level |
|--------------------|----------|---------------------------|---------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------------------|
|                    |          | 7                         | 8       | 9     | 10    | 11    | 12    | 13    | 14    | 15    | 16    | 17    | 18    |                    |
| 0.05               | 0.05     | 2.046                     | 1.018 + | 0.007 | 0.007 | 0.007 | 0.007 | 0.007 | 0.007 | 0.007 | 0.007 | 0.007 | 0.007 | 0.05               |
|                    |          | 0.046                     | 0.030   | 0.030 | 0.030 | 0.030 | 0.030 | 0.030 | 0.030 | 0.030 | 0.030 | 0.030 | 0.030 |                    |
|                    |          | 0.037                     | 0.027   | 0.027 | 0.027 | 0.027 | 0.027 | 0.027 | 0.027 | 0.027 | 0.027 | 0.027 | 0.027 |                    |
|                    |          | 0.028                     | 0.020   | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 |                    |
|                    |          | 0.020                     | 0.016   | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 |                    |
|                    |          | 0.016                     | 0.010   | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 |                    |
|                    |          | 0.012                     | 0.008   | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 |                    |
|                    |          | 0.008                     | 0.006   | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 |                    |
|                    |          | 0.006                     | 0.004   | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 |                    |
|                    |          | 0.004                     | 0.003   | 0.003 | 0.003 | 0.003 | 0.003 | 0.003 | 0.003 | 0.003 | 0.003 | 0.003 | 0.003 |                    |
|                    |          | 0.003                     | 0.002   | 0.002 | 0.002 | 0.002 | 0.002 | 0.002 | 0.002 | 0.002 | 0.002 | 0.002 | 0.002 |                    |
|                    |          | 0.002                     | 0.001   | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 |                    |
| 0.025              | 0.025    | 1.018 +                   | 0.008   | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.025              |
|                    |          | 0.030                     | 0.020   | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 |                    |
|                    |          | 0.027                     | 0.020   | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 |                    |
|                    |          | 0.020                     | 0.016   | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 |                    |
|                    |          | 0.016                     | 0.010   | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 |                    |
|                    |          | 0.012                     | 0.008   | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 |                    |
|                    |          | 0.008                     | 0.006   | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 |                    |
|                    |          | 0.006                     | 0.004   | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 |                    |
|                    |          | 0.004                     | 0.003   | 0.003 | 0.003 | 0.003 | 0.003 | 0.003 | 0.003 | 0.003 | 0.003 | 0.003 | 0.003 |                    |
|                    |          | 0.003                     | 0.002   | 0.002 | 0.002 | 0.002 | 0.002 | 0.002 | 0.002 | 0.002 | 0.002 | 0.002 | 0.002 |                    |
|                    |          | 0.002                     | 0.001   | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 |                    |
|                    |          | 0.001                     | 0.000   | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |                    |
| 0.01               | 0.01     | 0.046                     | 0.030   | 0.030 | 0.030 | 0.030 | 0.030 | 0.030 | 0.030 | 0.030 | 0.030 | 0.030 | 0.030 | 0.01               |
|                    |          | 0.037                     | 0.027   | 0.027 | 0.027 | 0.027 | 0.027 | 0.027 | 0.027 | 0.027 | 0.027 | 0.027 | 0.027 |                    |
|                    |          | 0.028                     | 0.020   | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 |                    |
|                    |          | 0.020                     | 0.016   | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 |                    |
|                    |          | 0.016                     | 0.010   | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 |                    |
|                    |          | 0.012                     | 0.008   | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 |                    |
|                    |          | 0.008                     | 0.006   | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 | 0.006 |                    |
|                    |          | 0.006                     | 0.004   | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 | 0.004 |                    |
|                    |          | 0.004                     | 0.003   | 0.003 | 0.003 | 0.003 | 0.003 | 0.003 | 0.003 | 0.003 | 0.003 | 0.003 | 0.003 |                    |
|                    |          | 0.003                     | 0.002   | 0.002 | 0.002 | 0.002 | 0.002 | 0.002 | 0.002 | 0.002 | 0.002 | 0.002 | 0.002 |                    |
|                    |          | 0.002                     | 0.001   | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 | 0.001 |                    |
|                    |          | 0.001                     | 0.000   | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |                    |

## TABLES

TABLE A-29 (Continued). TABLES FOR TESTING SIGNIFICANCE IN  $2 \times 2$  TABLES WITH UNEQUAL SAMPLES

|                       | $\alpha_1$ | Significance Level |                 |                |                 |                      | $\alpha_1$            | Significance Level |                 |                |                 |          |         |         |         |
|-----------------------|------------|--------------------|-----------------|----------------|-----------------|----------------------|-----------------------|--------------------|-----------------|----------------|-----------------|----------|---------|---------|---------|
|                       |            | 0.05<br>(0.10)     | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |                      |                       | 0.05<br>(0.10)     | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |          |         |         |         |
| $n_1=14 \quad n_2=18$ | 7          | 1.021              | 1.021           | 0.004          | 0.004           | $n_1=14 \quad n_2=7$ | 14                    | 4.026              | 3.006           | 3.006          | 2.001           |          |         |         |         |
|                       | 6          | 1.048              | 0.010 +         | —              | —               |                      | 13                    | 3.025              | 2.006           | 2.006          | 1.001           |          |         |         |         |
|                       | 5          | 0.025 -            | 0.025 -         | —              | —               |                      | 12                    | 2.017              | 2.017           | 1.003          | 1.003           |          |         |         |         |
| 12                    | 14         | 8.033              | 7.012           | 6.004          | 6.004           |                      | 11                    | 2.041              | 1.009           | 1.009          | 0.001           |          |         |         |         |
|                       | 18         | 6.021              | 6.021           | 3.007          | 4.002           |                      | 10                    | 1.021              | 1.021           | 0.003          | 0.003           |          |         |         |         |
|                       | 12         | 3.025 +            | 4.009           | 4.009          | 3.003           |                      | 9                     | 1.043              | 0.007           | 0.007          | —               |          |         |         |         |
|                       | 11         | 4.026              | 3.009           | 3.009          | 2.002           |                      | 8                     | 0.015 -            | 0.015 -         | —              | —               |          |         |         |         |
|                       | 10         | 3.024              | 3.024           | 2.007          | 1.002           |                      | 7                     | 0.030              | —               | —              | —               |          |         |         |         |
|                       | 9          | 2.019              | 2.019           | 1.005 -        | 1.005 -         | 6                    | 14                    | 3.018              | 3.018           | 2.003          | 2.003           |          |         |         |         |
|                       | 8          | 2.042              | 1.012           | 0.002          | 0.002           |                      | 13                    | 2.014              | 2.014           | 1.002          | 1.002           |          |         |         |         |
|                       | 7          | 1.026              | 0.005 +         | 0.005 +        | —               |                      | 12                    | 2.037              | 1.007           | 1.007          | 0.001           |          |         |         |         |
|                       | 6          | 0.013              | 0.013           | —              | —               |                      | 11                    | 1.018              | 1.018           | 0.002          | 0.002           |          |         |         |         |
|                       | 5          | 0.030              | —               | —              | —               |                      | 10                    | 1.038              | 0.005 +         | 0.005 +        | —               |          |         |         |         |
| 11                    | 14         | 7.026              | 6.009           | 6.009          | 5.003           |                      |                       | 9                  | 0.012           | 0.012          | —               | —        |         |         |         |
|                       | 13         | 6.039              | 5.014           | 4.004          | 4.004           |                      |                       | 8                  | 0.024           | 0.024          | —               | —        |         |         |         |
|                       | 12         | 5.043              | 4.016           | 3.005 -        | 3.005 -         |                      |                       | 7                  | 0.044           | —              | —               | —        |         |         |         |
|                       | 11         | 4.042              | 3.015 -         | 2.004          | 2.004           |                      | 5                     | 14                 | 2.010 +         | 2.010 +        | 1.001           | 1.001    |         |         |         |
|                       | 10         | 3.036              | 2.011           | 1.003          | 1.003           |                      |                       | 13                 | 2.037           | 1.006          | 1.006           | 0.001    |         |         |         |
|                       | 9          | 2.027              | 1.007           | 1.007          | 0.001           | 12                   |                       | 1.017              | 1.017           | 0.002          | 0.002           |          |         |         |         |
|                       | 8          | 1.017              | 1.017           | 0.003          | 0.003           | 11                   |                       | 1.038              | 0.005 -         | 0.005 -        | 0.005 -         |          |         |         |         |
|                       | 7          | 1.028              | 0.007           | 0.007          | —               | 10                   |                       | 0.011              | 0.011           | —              | —               |          |         |         |         |
|                       | 6          | 0.017              | 0.017           | —              | —               | 9                    |                       | 0.022              | 0.022           | —              | —               |          |         |         |         |
|                       | 5          | 0.036              | —               | —              | —               | 8                    |                       | 0.040              | —               | —              | —               |          |         |         |         |
| 10                    | 14         | 6.020              | 6.020           | 5.006          | 4.002           | 4                    |                       | 14                 | 2.039           | 1.005 -        | 1.005 -         | 1.005 -  |         |         |         |
|                       | 13         | 5.028              | 4.009           | 4.009          | 3.002           |                      |                       | 13                 | 1.019           | 1.019          | 0.002           | 0.002    |         |         |         |
|                       | 12         | 4.028              | 3.009           | 3.009          | 2.002           |                      |                       | 12                 | 1.044           | 0.005 -        | 0.005 -         | 0.005 -  |         |         |         |
|                       | 11         | 3.024              | 3.024           | 2.007          | 1.001           |                      | 11                    | 0.011              | 0.011           | —              | —               |          |         |         |         |
|                       | 10         | 2.018              | 2.018           | 1.004          | 1.004           |                      | 10                    | 0.023              | 0.023           | —              | —               |          |         |         |         |
|                       | 9          | 2.040              | 1.011           | 0.002          | 0.002           |                      | 9                     | 0.041              | —               | —              | —               |          |         |         |         |
|                       | 8          | 1.024              | 1.024           | 0.004          | 0.004           |                      | 3                     | 14                 | 1.022           | 1.022          | 0.001           | 0.001    |         |         |         |
|                       | 7          | 0.010 -            | 0.010 -         | 0.010 -        | —               |                      |                       | 13                 | 0.006           | 0.006          | 0.006           | —        |         |         |         |
|                       | 6          | 0.022              | 0.022           | —              | —               |                      |                       | 12                 | 0.015 -         | 0.015 -        | —               | —        |         |         |         |
|                       | 5          | 0.047              | —               | —              | —               |                      |                       | 11                 | 0.029           | —              | —               | —        |         |         |         |
| 9                     | 14         | 6.047              | 5.014           | 4.004          | 4.004           | 2                    | 14                    | 0.008              | 0.008           | 0.008          | —               |          |         |         |         |
|                       | 13         | 4.018              | 4.018           | 3.005 -        | 3.005 -         |                      | 13                    | 0.025              | 0.025           | —              | —               |          |         |         |         |
|                       | 12         | 3.017              | 3.017           | 2.004          | 2.004           |                      | 12                    | 0.050              | —               | —              | —               |          |         |         |         |
|                       | 11         | 3.042              | 2.012           | 1.002          | 1.002           |                      | $n_1=15 \quad n_2=15$ |                    |                 |                |                 |          |         |         |         |
|                       | 10         | 2.029              | 1.007           | 1.007          | 0.001           | 15                   |                       |                    |                 |                |                 | 11.050 - | 10.021  | 9.008   | 8.003   |
|                       | 9          | 1.017              | 1.017           | 0.002          | 0.002           | 14                   |                       |                    |                 |                |                 | 9.040    | 8.018   | 7.007   | 6.003   |
|                       | 8          | 1.036              | 0.008           | 0.008          | —               | 13                   |                       |                    |                 |                |                 | 7.025 +  | 6.010 + | 5.004   | 5.004   |
|                       | 7          | 0.014              | 0.014           | —              | —               | 12                   |                       |                    |                 |                |                 | 6.030    | 5.013   | 4.005 - | 4.005 - |
|                       | 6          | 0.030              | —               | —              | —               | 11                   |                       |                    |                 |                |                 | 5.033    | 4.013   | 3.005 - | 3.005 - |
| 8                     | 14         | 5.036              | 4.010 -         | 4.010 -        | 3.002           | 10                   |                       |                    |                 |                |                 | 4.033    | 3.013   | 2.004   | 2.004   |
|                       | 13         | 4.039              | 3.011           | 2.002          | 2.002           | 9                    |                       |                    |                 |                |                 | 3.030    | 2.010 + | 1.003   | 1.003   |
|                       | 12         | 3.032              | 2.006           | 2.006          | 1.001           | 8                    |                       |                    |                 |                |                 | 2.025 +  | 1.007   | 1.007   | 0.001   |
|                       | 11         | 2.022              | 2.022           | 1.005 -        | 1.005 -         | 7                    |                       |                    |                 |                |                 | 1.018    | 1.018   | 0.003   | 0.003   |
|                       | 10         | 2.046              | 1.012           | 0.002          | 0.002           | 6                    |                       |                    |                 |                |                 | 1.040    | 0.008   | 0.008   | —       |
|                       | 9          | 1.026              | 0.004           | 0.004          | 0.004           | 5                    |                       |                    |                 |                |                 | 0.021    | 0.021   | —       | —       |
|                       | 8          | 0.009              | 0.009           | 0.009          | —               | 4                    |                       |                    |                 |                |                 | 0.050 -  | —       | —       | —       |
|                       | 7          | 0.020              | 0.020           | —              | —               |                      |                       |                    |                 |                |                 |          |         |         |         |
|                       | 6          | 0.040              | —               | —              | —               |                      |                       |                    |                 |                |                 |          |         |         |         |



## TABLES

TABLE A-29 (Continued). TABLES FOR TESTING SIGNIFICANCE IN  $2 \times 2$  TABLES WITH UNEQUAL SAMPLES

|          |          | Significance Level |                |                 |                |                 |          | Significance Level |            |                |                 |                |                 |
|----------|----------|--------------------|----------------|-----------------|----------------|-----------------|----------|--------------------|------------|----------------|-----------------|----------------|-----------------|
|          |          | $\alpha_1$         | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |          |                    | $\alpha_1$ | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |
| $n_1=15$ | $n_2=14$ | 15                 | 10.043         | 9.017           | 8.006          | 7.002           | $n_1=15$ | $n_2=9$            | 13         | 4.042          | 3.013           | 2.003          | 2.003           |
|          |          | 14                 | 8.031          | 7.013           | 6.005          | 6.005           |          |                    | 12         | 3.032          | 2.009           | 2.009          | 1.003           |
|          |          | 13                 | 7.041          | 6.017           | 5.007          | 4.002           |          |                    | 11         | 2.031          | 2.021           | 1.005          | 1.005           |
|          |          | 12                 | 6.046          | 5.020           | 4.007          | 3.002           |          |                    | 10         | 2.046          | 1.011           | 0.002          | 0.002           |
|          |          | 11                 | 5.048          | 4.020           | 3.007          | 2.002           |          |                    | 9          | 1.024          | 1.024           | 0.004          | 0.004           |
|          |          | 10                 | 4.046          | 3.018           | 2.005          | 1.001           |          |                    | 8          | 1.048          | 0.009           | 0.009          | —               |
|          |          | 9                  | 3.041          | 2.014           | 1.004          | 1.004           |          |                    | 7          | 0.019          | 0.019           | —              | —               |
|          |          | 8                  | 2.033          | 1.009           | 1.009          | 0.001           |          |                    | 6          | 0.037          | —               | —              | —               |
|          |          | 7                  | 1.032          | 1.022           | 0.004          | 0.004           |          |                    |            |                |                 |                |                 |
|          |          | 6                  | 1.049          | 0.011           | —              | —               |          |                    |            |                |                 |                |                 |
| 5        | 0.035 +  | —                  | —              | —               |                |                 |          |                    |            |                |                 |                |                 |
| 13       | 15       | 9.035              | 8.013          | 7.006           | 7.005          | 8               | 15       | 5.032              | 4.008      | 4.008          | 3.003           |                |                 |
|          | 14       | 7.032              | 7.022          | 6.009           | 5.003          | 14              | 4.032    | 3.009              | 3.009      | 2.002          |                 |                |                 |
|          | 13       | 6.039              | 5.011          | 4.004           | 4.004          | 13              | 3.025    | 2.008              | 2.008      | 1.001          |                 |                |                 |
|          | 12       | 5.031              | 4.013          | 3.004           | 3.004          | 12              | 2.017    | 2.017              | 1.003      | 1.003          |                 |                |                 |
|          | 11       | 4.030              | 3.011          | 2.003           | 2.003          | 11              | 2.037    | 1.008              | 1.008      | 0.001          |                 |                |                 |
|          | 10       | 3.026              | 2.008          | 2.008           | 1.002          | 10              | 1.019    | 1.019              | 0.003      | 0.003          |                 |                |                 |
|          | 9        | 2.020              | 2.020          | 1.005 +         | 0.001          | 9               | 1.038    | 0.008              | 0.005      | —              |                 |                |                 |
|          | 8        | 2.043              | 1.013          | 0.003           | 0.003          | 8               | 0.013    | 0.013              | —          | —              |                 |                |                 |
|          | 7        | 1.039              | 0.005 +        | 0.005 +         | —              | 7               | 0.025    | —                  | —          | —              |                 |                |                 |
|          | 6        | 0.013              | 0.013          | —               | —              | 6               | 0.050 -  | —                  | —          | —              |                 |                |                 |
| 5        | 0.031    | —                  | —              | —               |                |                 |          |                    |            |                |                 |                |                 |
| 12       | 15       | 8.038              | 7.010          | 7.010           | 6.003          | 7               | 15       | 4.023              | 4.023      | 3.005          | 3.005           |                |                 |
|          | 14       | 7.043              | 6.016          | 5.006           | 4.003          | 14              | 3.021    | 3.021              | 2.004      | 2.004          |                 |                |                 |
|          | 13       | 6.049              | 5.019          | 4.007           | 3.003          | 13              | 2.014    | 2.014              | 1.002      | 1.002          |                 |                |                 |
|          | 12       | 5.049              | 4.019          | 3.008           | 2.002          | 12              | 2.032    | 1.007              | 1.007      | 0.001          |                 |                |                 |
|          | 11       | 4.046 +            | 3.017          | 2.005           | 2.005          | 11              | 1.015 +  | 1.016 +            | 0.002      | 0.002          |                 |                |                 |
|          | 10       | 3.038              | 2.013          | 1.003           | 1.003          | 10              | 1.022    | 0.005 -            | 0.005 -    | 0.005          |                 |                |                 |
|          | 9        | 2.038              | 1.007          | 1.007           | 0.001          | 9               | 0.010 +  | 0.010 +            | —          | —              |                 |                |                 |
|          | 8        | 1.018              | 1.018          | 0.003           | 0.003          | 8               | 0.020    | 0.020              | —          | —              |                 |                |                 |
|          | 7        | 1.038              | 0.007          | 0.007           | —              | 7               | 0.038    | —                  | —          | —              |                 |                |                 |
|          | 6        | 0.017              | 0.017          | —               | —              |                 |          |                    |            |                |                 |                |                 |
| 5        | 0.037    | —                  | —              | —               |                |                 |          |                    |            |                |                 |                |                 |
| 11       | 15       | 7.022              | 7.022          | 6.007           | 5.002          | 6               | 15       | 3.015 +            | 3.015 +    | 2.003          | 2.003           |                |                 |
|          | 14       | 6.032              | 5.011          | 4.003           | 4.003          | 14              | 2.011    | 2.011              | 1.002      | 1.002          |                 |                |                 |
|          | 13       | 5.024              | 4.012          | 3.003           | 3.003          | 13              | 2.031    | 1.006              | 1.006      | 0.001          |                 |                |                 |
|          | 12       | 4.032              | 3.010 +        | 2.003           | 2.003          | 12              | 1.014    | 1.014              | 0.002      | 0.002          |                 |                |                 |
|          | 11       | 3.026              | 2.008          | 2.008           | 1.002          | 11              | 1.039    | 0.004              | 0.004      | 0.004          |                 |                |                 |
|          | 10       | 2.019              | 2.019          | 1.004           | 1.004          | 10              | 0.009    | 0.009              | 0.009      | —              |                 |                |                 |
|          | 9        | 2.040              | 1.011          | 0.002           | 0.002          | 9               | 0.017    | 0.017              | —          | —              |                 |                |                 |
|          | 8        | 1.024              | 1.024          | 0.004           | 0.004          | 8               | 0.033    | —                  | —          | —              |                 |                |                 |
|          | 7        | 1.049              | 0.010 -        | 0.010 -         | —              |                 |          |                    |            |                |                 |                |                 |
|          | 6        | 0.022              | 0.022          | —               | —              |                 |          |                    |            |                |                 |                |                 |
| 5        | 0.046    | —                  | —              | —               |                |                 |          |                    |            |                |                 |                |                 |
| 10       | 15       | 6.017              | 6.017          | 5.005           | 5.005          | 5               | 15       | 2.009              | 2.009      | 2.009          | 1.001           |                |                 |
|          | 14       | 5.023              | 5.023          | 4.007           | 3.002          | 14              | 2.022    | 1.005              | 1.005      | 1.005          |                 |                |                 |
|          | 13       | 4.022              | 4.022          | 3.007           | 2.001          | 13              | 1.014    | 1.014              | 0.001      | 0.001          |                 |                |                 |
|          | 12       | 3.018              | 3.018          | 2.005           | 2.005          | 12              | 1.031    | 0.004              | 0.004      | 0.004          |                 |                |                 |
|          | 11       | 3.042              | 2.013          | 1.003           | 1.003          | 11              | 0.008    | 0.008              | 0.008      | —              |                 |                |                 |
|          | 10       | 2.029              | 1.007          | 1.007           | 0.001          | 10              | 0.016    | 0.016              | —          | —              |                 |                |                 |
|          | 9        | 1.016              | 1.016          | 0.002           | 0.002          | 9               | 0.030    | —                  | —          | —              |                 |                |                 |
|          | 8        | 1.024              | 0.006          | 0.006           | —              |                 |          |                    |            |                |                 |                |                 |
|          | 7        | 0.013              | 0.013          | —               | —              |                 |          |                    |            |                |                 |                |                 |
|          | 6        | 0.028              | —              | —               | —              |                 |          |                    |            |                |                 |                |                 |
| 9        | 15       | 6.042              | 5.012          | 4.003           | 4.003          | 4               | 15       | 2.035 +            | 1.004      | 1.004          | 1.004           |                |                 |
|          | 14       | 5.047              | 4.015          | 3.004           | 3.004          | 14              | 1.016    | 1.016              | 0.001      | 0.001          |                 |                |                 |
|          |          |                    |                |                 |                | 13              | 1.037    | 0.004              | 0.004      | 0.004          |                 |                |                 |
|          |          |                    |                |                 |                | 12              | 0.009    | 0.009              | 0.009      | —              |                 |                |                 |
|          |          |                    |                |                 |                | 11              | 0.018    | 0.018              | —          | —              |                 |                |                 |
|          |          |                    |                |                 |                | 10              | 0.033    | —                  | —          | —              |                 |                |                 |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |
|          | 15       | 6.042              | 5.012          | 4.003           | 4.003          | 3               | 15       | 1.020              | 1.020      | 0.001          | 0.001           |                |                 |
|          | 14       | 5.047              | 4.015          | 3.004           | 3.004          | 14              | 0.006    | 0.005              | 0.005      | 0.005          |                 |                |                 |
|          |          |                    |                |                 |                | 13              | 0.012    | 0.012              | —          | —              |                 |                |                 |
|          |          |                    |                |                 |                | 12              | 0.035    | 0.035              | —          | —              |                 |                |                 |
|          |          |                    |                |                 |                | 11              | 0.043    | —                  | —          | —              |                 |                |                 |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |
|          | 15       | 6.042              | 5.012          | 4.003           | 4.003          | 2               | 15       | 0.007              | 0.007      | 0.007          | —               |                |                 |
|          | 14       | 5.047              | 4.015          | 3.004           | 3.004          | 14              | 0.022    | 0.022              | —          | —              |                 |                |                 |
|          |          |                    |                |                 |                | 13              | 0.044    | —                  | —          | —              |                 |                |                 |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |

## TABLES

TABLE A-29 (Continued). TABLES FOR TESTING SIGNIFICANCE IN  $2 \times 2$  TABLES WITH UNEQUAL SAMPLES

|          |          | Significance Level |                |                 |                |                 |          | Significance Level |            |                |                 |                |                 |
|----------|----------|--------------------|----------------|-----------------|----------------|-----------------|----------|--------------------|------------|----------------|-----------------|----------------|-----------------|
|          |          | $\alpha_1$         | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |          |                    | $\alpha_1$ | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |
| $n_1=16$ | $n_2=16$ | 16                 | 11.022         | 11.022          | 10.009         | 9.003           | $n_1=16$ | $n_2=12$           | 16         | 8.024          | 8.024           | 7.008          | 6.002           |
|          |          | 15                 | 10.041         | 9.019           | 8.008          | 7.003           |          |                    | 15         | 7.036          | 6.013           | 5.004          | 5.004           |
|          |          | 14                 | 8.027          | 7.012           | 6.006          | 6.006           |          |                    | 14         | 6.040          | 5.016           | 4.005          | 4.006           |
|          |          | 13                 | 7.033          | 6.016           | 5.008          | 4.002           |          |                    | 13         | 5.039          | 4.014           | 3.004          | 3.004           |
|          |          | 12                 | 6.037          | 5.016           | 4.006          | 3.002           |          |                    | 12         | 4.034          | 3.012           | 2.003          | 2.003           |
|          |          | 11                 | 5.038          | 4.016           | 3.005          | 2.002           |          |                    | 11         | 3.027          | 2.008           | 2.008          | 1.002           |
|          |          | 10                 | 4.037          | 3.015           | 2.005          | 2.005           |          |                    | 10         | 2.019          | 2.019           | 1.005          | 1.006           |
|          |          | 9                  | 3.033          | 2.012           | 1.003          | 1.003           |          |                    | 9          | 2.040          | 1.011           | 0.002          | 0.002           |
|          |          | 8                  | 2.027          | 1.008           | 1.008          | 0.001           |          |                    | 8          | 1.024          | 1.024           | 0.004          | 0.004           |
|          |          | 7                  | 1.019          | 1.019           | 0.003          | 0.003           |          |                    | 7          | 1.048          | 0.010           | 0.010          | —               |
|          | 6        | 1.041              | 0.009          | 0.009           | —              | 6               |          | 0.021              | 0.021      | —              | —               |                |                 |
|          | 5        | 0.022              | 0.022          | —               | —              | 5               |          | 0.044              | —          | —              | —               |                |                 |
|          | 15       | 16                 | 11.043         | 10.018          | 9.007          | 8.002           |          | 11                 | 16         | 7.019          | 7.019           | 6.008          | 5.002           |
|          |          | 15                 | 9.033          | 8.014           | 7.006 +        | 6.002           |          |                    | 15         | 6.027          | 5.009           | 5.009          | 4.002           |
|          |          | 14                 | 8.044          | 7.019           | 6.008          | 5.003           |          |                    | 14         | 5.027          | 4.009           | 4.009          | 3.002           |
|          |          | 13                 | 6.022          | 6.023           | 5.009          | 4.003           |          |                    | 13         | 4.024          | 4.024           | 3.008          | 2.002           |
|          |          | 12                 | 5.024          | 5.024           | 4.009          | 3.003           |          |                    | 12         | 3.019          | 3.019           | 2.005 +        | 1.001           |
|          |          | 11                 | 4.022          | 4.022           | 3.008          | 2.002           |          |                    | 11         | 3.041          | 2.013           | 1.003          | 1.003           |
|          |          | 10                 | 4.040          | 3.020           | 2.006          | 1.001           |          |                    | 10         | 2.028          | 1.007           | 1.007          | 0.001           |
|          |          | 9                  | 3.042          | 2.016           | 1.004          | 1.004           |          |                    | 9          | 1.016          | 1.016           | 0.002          | 0.002           |
| 8        |          | 2.036 -            | 1.010 +        | 0.002           | 0.002          | 8               | 1.033    |                    | 0.008      | 0.006          | —               |                |                 |
| 7        |          | 1.023              | 1.023          | 0.004           | 0.004          | 7               | 0.013    |                    | 0.013      | —              | —               |                |                 |
| 6        | 0.011    | 0.011              | —              | —               | 6              | 0.027           | —        | —                  | —          |                |                 |                |                 |
| 5        | 0.026    | —                  | —              | —               | 10             | 16              | 7.048    | 6.014              | 5.004      | 5.004          |                 |                |                 |
| 14       | 16       | 10.037             | 9.014          | 8.006 +         |                | 7.002           | 15       | 5.018              | 5.018      | 4.006 +        | 3.001           |                |                 |
|          | 15       | 8.026 +            | 7.010 -        | 7.010 -         |                | 6.003           | 14       | 4.017              | 4.017      | 3.005 -        | 3.006           |                |                 |
|          | 14       | 7.032              | 6.012          | 5.005 -         |                | 5.006 -         | 13       | 4.042              | 3.014      | 2.003          | 2.003           |                |                 |
|          | 13       | 6.035 +            | 5.014          | 4.006 +         |                | 3.001           | 12       | 3.032              | 2.009      | 2.009          | 1.002           |                |                 |
|          | 12       | 5.035 +            | 4.014          | 3.006 -         |                | 3.005 -         | 11       | 2.021              | 2.021      | 1.005 -        | 1.006           |                |                 |
|          | 11       | 4.023              | 3.012          | 2.004           |                | 2.004           | 10       | 2.042              | 1.011      | 0.002          | 0.002           |                |                 |
|          | 10       | 3.028              | 2.009          | 2.009           |                | 1.002           | 9        | 1.023              | 1.023      | 0.004          | 0.004           |                |                 |
|          | 9        | 2.021              | 2.021          | 1.008           |                | 0.001           | 8        | 1.046 -            | 0.008      | 0.008          | —               |                |                 |
|          | 8        | 2.046 -            | 1.012          | 0.002           |                | 0.002           | 7        | 0.017              | 0.017      | —              | —               |                |                 |
|          | 7        | 1.020              | 0.006          | 0.006           | —              | 6               | 0.036 -  | —                  | —          | —              |                 |                |                 |
| 6        | 0.013    | 0.013              | —              | —               | 9              | 16              | 6.037    | 5.010 -            | 5.010 -    | 4.002          |                 |                |                 |
| 13       | 18       | 9.020              | 8.011          | 7.004           |                | 7.004           | 15       | 5.040              | 4.012      | 3.003          | 3.003           |                |                 |
|          | 15       | 8.047              | 7.019          | 6.007           |                | 5.002           | 14       | 4.034              | 3.010 -    | 3.010 -        | 2.002           |                |                 |
|          | 14       | 6.022              | 6.022          | 5.008           |                | 4.003           | 13       | 3.026 +            | 2.007      | 2.007          | 1.001           |                |                 |
|          | 13       | 5.022              | 5.022          | 4.008           |                | 3.003           | 12       | 2.016              | 2.016      | 1.003          | 1.003           |                |                 |
|          | 12       | 4.022              | 4.022          | 3.007           |                | 2.002           | 11       | 2.033              | 1.008      | 1.008          | 0.001           |                |                 |
|          | 11       | 4.043              | 3.018          | 2.006 +         |                | 1.001           | 10       | 1.017              | 1.017      | 0.002          | 0.002           |                |                 |
|          | 10       | 3.029              | 2.013          | 1.003           |                | 1.003           | 9        | 1.034              | 0.006      | 0.006          | —               |                |                 |
|          | 9        | 2.029              | 1.003          | 1.008           |                | 0.001           | 8        | 0.612              | 0.012      | —              | —               |                |                 |
|          | 8        | 1.013              | 1.013          | 0.003           |                | 0.002           | 7        | 0.024              | 0.024      | —              | —               |                |                 |
|          | 7        | 1.028              | 0.007          | 0.007           | —              | 6               | 0.046 +  | —                  | —          | —              |                 |                |                 |
| 6        | 0.017    | 0.017              | —              | —               |                |                 |          |                    |            |                |                 |                |                 |
| 5        | 0.037    | —                  | —              | —               |                |                 |          |                    |            |                |                 |                |                 |

## TABLES

TABLE A-29 (Continued). TABLES FOR TESTING SIGNIFICANCE IN  $2 \times 2$  TABLES WITH UNEQUAL SAMPLES

|                      | $\alpha_1$ | Significance Level |                 |                |                 |                       | $\alpha_1$ | Significance Level |                 |                |                 |   |
|----------------------|------------|--------------------|-----------------|----------------|-----------------|-----------------------|------------|--------------------|-----------------|----------------|-----------------|---|
|                      |            | 0.05<br>(0.10)     | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |                       |            | 0.05<br>(0.10)     | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |   |
| $n_1=16 \quad n_2=8$ | 16         | 5.038              | 4.007           | 4.007          | 3.001           | $n_1=16 \quad n_2=3$  | 16         | 1.018              | 1.018           | 0.001          | 0.001           |   |
|                      | 15         | 4.038              | 3.007           | 3.007          | 2.001           |                       | 15         | 0.004              | 0.004           | 0.004          | 0.004           |   |
|                      | 14         | 3.031              | 3.031           | 2.005          | 2.005           |                       | 14         | 0.010 +            | 0.010 +         | —              | —               |   |
|                      | 13         | 3.047              | 2.013           | 1.003          | 1.003           |                       | 13         | 0.021              | 0.021           | —              | —               |   |
|                      | 12         | 2.028              | 1.006           | 1.006          | 0.001           |                       | 12         | 0.038              | —               | —              | —               |   |
|                      | 11         | 1.014              | 1.014           | 0.003          | 0.003           |                       | 2          | 16                 | 0.007           | 0.007          | 0.007           | — |
|                      | 10         | 1.037              | 0.004           | 0.004          | 0.004           |                       |            | 15                 | 0.020           | 0.020          | —               | — |
|                      | 9          | 0.009              | 0.009           | 0.009          | —               |                       |            | 14                 | 0.029           | —              | —               | — |
|                      | 8          | 0.017              | 0.017           | —              | —               |                       |            |                    |                 |                |                 |   |
|                      | 7          | 0.033              | —               | —              | —               |                       |            |                    |                 |                |                 |   |
| 7                    | 16         | 4.020              | 4.020           | 3.004          | 3.004           | $n_1=17 \quad n_2=17$ | 17         | 12.022             | 12.022          | 11.009         | 10.004          |   |
|                      | 15         | 3.017              | 3.017           | 2.003          | 2.003           |                       | 16         | 11.043             | 10.020          | 9.008          | 8.003           |   |
|                      | 14         | 3.048 +            | 2.011           | 1.003          | 1.003           |                       | 15         | 8.029              | 8.013           | 7.005 +        | 6.002           |   |
|                      | 13         | 2.028              | 1.005           | 1.005          | 1.005           |                       | 14         | 8.038 +            | 7.016           | 6.007          | 5.002           |   |
|                      | 12         | 1.013              | 1.013           | 0.001          | 0.001           |                       | 13         | 7.040              | 6.018           | 5.007          | 4.003           |   |
|                      | 11         | 1.034              | 1.034           | 0.003          | 0.003           |                       | 12         | 6.042              | 5.019           | 4.007          | 3.002           |   |
|                      | 10         | 1.045              | 0.007           | 0.007          | —               |                       | 11         | 5.043              | 4.018           | 3.007          | 2.002           |   |
|                      | 9          | 0.014              | 0.014           | —              | —               |                       | 10         | 4.040              | 3.016           | 2.005 +        | 1.001           |   |
|                      | 8          | 0.028              | —               | —              | —               |                       | 9          | 3.025 +            | 2.013           | 1.003          | 1.003           |   |
|                      | 7          | 0.047              | —               | —              | —               |                       | 8          | 2.029              | 1.008           | 1.008          | 0.001           |   |
| 6                    | 16         | 3.012              | 3.012           | 2.003          | 2.003           | 16                    | 7          | 1.020              | 1.020           | 0.004          | 0.004           |   |
|                      | 15         | 3.046              | 2.009           | 2.009          | 1.001           |                       | 6          | 1.043              | 0.009           | 0.009          | —               |   |
|                      | 14         | 2.028 +            | 1.004           | 1.004          | 1.004           |                       | 5          | 0.022              | 0.022           | —              | —               |   |
|                      | 13         | 1.011              | 1.011           | 0.001          | 0.001           |                       | 17         | 12.044             | 11.018          | 10.007         | 9.003           |   |
|                      | 12         | 1.023              | 1.023           | 0.003          | 0.003           |                       | 16         | 10.025             | 9.016           | 8.006          | 7.003           |   |
|                      | 11         | 1.043              | 0.006           | 0.006          | —               |                       | 15         | 9.046              | 8.021           | 7.009          | 6.002           |   |
|                      | 10         | 0.013              | 0.013           | —              | —               |                       | 14         | 7.025 +            | 6.011           | 5.004          | 5.004           |   |
|                      | 9          | 0.023              | 0.023           | —              | —               |                       | 13         | 6.037              | 5.011           | 4.004          | 4.004           |   |
|                      | 8          | 0.040              | —               | —              | —               |                       | 12         | 5.027              | 4.011           | 3.004          | 3.004           |   |
|                      |            |                    |                 |                |                 |                       | 11         | 4.025 +            | 3.009           | 3.009          | 2.002           |   |
| 5                    | 16         | 3.048              | 2.008           | 2.008          | 1.001           | 15                    | 10         | 3.022              | 3.022           | 2.007          | 1.002           |   |
|                      | 15         | 2.028              | 1.004           | 1.004          | 1.004           |                       | 9          | 3.046              | 2.017           | 1.004          | 1.004           |   |
|                      | 14         | 1.011              | 1.011           | 0.001          | 0.001           |                       | 8          | 2.036              | 1.011           | 0.002          | 0.002           |   |
|                      | 13         | 1.035 +            | 0.003           | 0.003          | 0.003           |                       | 7          | 1.024              | 1.024           | 0.005          | 0.005           |   |
|                      | 12         | 1.047              | 0.006           | 0.006          | —               |                       | 6          | 0.011              | 0.011           | —              | —               |   |
|                      | 11         | 0.013              | 0.013           | —              | —               |                       | 5          | 0.038              | —               | —              | —               |   |
|                      | 10         | 0.022              | 0.022           | —              | —               |                       | 17         | 11.028             | 10.015          | 9.006          | 8.003           |   |
|                      | 9          | 0.039              | —               | —              | —               |                       | 16         | 9.027              | 8.011           | 7.004          | 7.004           |   |
|                      |            |                    |                 |                |                 |                       | 15         | 8.025 +            | 7.015           | 6.006          | 5.003           |   |
|                      |            |                    |                 |                |                 |                       | 14         | 7.040              | 6.017           | 5.006          | 4.002           |   |
| 4                    | 16         | 2.022              | 1.004           | 1.004          | 1.004           | 13                    | 6.041      | 5.017              | 4.006           | 3.003          |                 |   |
|                      | 15         | 1.013              | 1.013           | 0.001          | 0.001           | 12                    | 5.039      | 4.016              | 3.005 +         | 2.001          |                 |   |
|                      | 14         | 1.023              | 0.003           | 0.003          | 0.003           | 11                    | 4.035 +    | 3.013              | 2.004           | 2.004          |                 |   |
|                      | 13         | 0.007              | 0.007           | 0.007          | —               | 10                    | 3.029      | 2.010              | 2.010           | 1.003          |                 |   |
|                      | 12         | 0.014              | 0.014           | —              | —               | 9                     | 2.022      | 2.022              | 1.006           | 0.001          |                 |   |
|                      | 11         | 0.026              | —               | —              | —               | 8                     | 2.046      | 1.014              | 0.002           | 0.002          |                 |   |
|                      | 10         | 0.042              | —               | —              | —               | 7                     | 1.030      | 0.006              | 0.006           | —              |                 |   |
|                      |            |                    |                 |                |                 | 6                     | 0.014      | 0.014              | —               | —              |                 |   |
|                      |            |                    |                 |                | 5               | 0.031                 | —          | —                  | —               |                |                 |   |

## TABLES

TABLE A-29 (Continued). TABLES FOR TESTING SIGNIFICANCE IN  $2 \times 2$  TABLES WITH UNEQUAL SAMPLES

|                   |    | Significance Level |                |                 |                |                 |                   | Significance Level |            |                |                 |                |                 |
|-------------------|----|--------------------|----------------|-----------------|----------------|-----------------|-------------------|--------------------|------------|----------------|-----------------|----------------|-----------------|
|                   |    | $\alpha_1$         | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |                   |                    | $\alpha_1$ | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |
| $n_1=17$ $n_2=14$ | 17 | 10                 | .032           | .012            | .004           | .004            | $n_1=17$ $n_2=11$ | 13                 | .042       | .014           | .004            | .004           |                 |
|                   | 16 | 8                  | .021           | .021            | .008           | .003            |                   | 12                 | .031       | .009           | .009            | .002           |                 |
|                   | 15 | 7                  | .028           | .010            | .010           | .003            |                   | 11                 | .020       | .020           | .005            | .005           |                 |
|                   | 14 | 6                  | .028           | .011            | .004           | .004            |                   | 10                 | .040       | .011           | .001            | .001           |                 |
|                   | 13 | 5                  | .027           | .010            | .010           | .003            |                   | 9                  | .022       | .022           | .004            | .004           |                 |
|                   | 12 | 4                  | .024           | .024            | .008           | .002            |                   | 8                  | .042       | .008           | .008            | —              |                 |
|                   | 11 | 4                  | .049           | .019            | .008           | .001            |                   | 7                  | .018       | .018           | —               | —              |                 |
|                   | 10 | 3                  | .040           | .014            | .003           | .003            |                   | 6                  | .033       | —              | —               | —              |                 |
|                   | 9  | 2                  | .029           | .008            | .008           | .001            |                   | 10                 | 17         | .041           | .012            | .003           | .003            |
|                   | 8  | 1                  | .018           | .018            | .003           | .003            |                   |                    | 16         | .047           | .016            | .004           | .004            |
|                   | 7  | 1                  | .038           | .007            | .007           | —               |                   |                    | 15         | .043           | .014            | .004           | .004            |
|                   | 6  | 0                  | .017           | .017            | —              | —               |                   |                    | 14         | .034           | .010            | .002           | .002            |
|                   | 5  | 0                  | .038           | —               | —              | —               |                   |                    | 13         | .024           | .024            | .007           | .001            |
|                   | 13 | 17                 | .026           | .009            | .009           | .003            |                   |                    | 12         | .049           | .015            | .003           | .003            |
|                   |    | 16                 | .040           | .018            | .005           | .002            |                   |                    | 11         | .031           | .007            | .007           | .001            |
|                   |    | 15                 | .046           | .018            | .008           | .002            |                   |                    | 10         | .016           | .016            | .002           | .002            |
|                   |    | 14                 | .046           | .018            | .006           | .002            |                   |                    | 9          | .031           | .005            | .005           | —               |
| 13                |    | .042               | .018           | .005            | .001           | 8               | .011              |                    | .011       | —              | —               |                |                 |
| 12                |    | .038               | .013           | .004            | .004           | 7               | .022              | .022               | —          | —              |                 |                |                 |
| 11                |    | .028               | .009           | .009            | .002           | 6               | .042              | —                  | —          | —              |                 |                |                 |
| 10                |    | .019               | .019           | .003            | .005           | 9               | 17                | .032               | .008       | .008           | .002            |                |                 |
| 9                 |    | .040               | .011           | .002            | .002           |                 | 16                | .034               | .010       | .010           | .002            |                |                 |
| 8                 |    | .024               | .024           | .004            | .004           |                 | 15                | .028               | .008       | .008           | .002            |                |                 |
| 7                 |    | .047               | .010           | .010            | —              |                 | 14                | .020               | .020       | .005           | .005            |                |                 |
| 6                 |    | .021               | .021           | —               | —              |                 | 13                | .042               | .012       | .002           | .002            |                |                 |
| 5                 |    | .043               | —              | —               | —              |                 | 12                | .023               | .006       | .006           | .001            |                |                 |
| 12                | 17 | .021               | .021           | .007            | .002           |                 | 11                | .048               | .012       | .002           | .002            |                |                 |
|                   | 16 | .030               | .011           | .003            | .003           | 10              | .024              | .024               | .004       | .004           |                 |                |                 |
|                   | 15 | .033               | .012           | .004            | .004           | 9               | .048              | .008               | .008       | —              |                 |                |                 |
|                   | 14 | .030               | .011           | .003            | .003           | 8               | .016              | .016               | —          | —              |                 |                |                 |
|                   | 13 | .026               | .008           | .008            | .002           | 7               | .030              | —                  | —          | —              |                 |                |                 |
|                   | 12 | .020               | .020           | .006            | .001           | 8               | 17                | .024               | .024       | .006           | .001            |                |                 |
|                   | 11 | .041               | .013           | .003            | .003           |                 | 16                | .023               | .023       | .006           | .001            |                |                 |
|                   | 10 | .026               | .007           | .007            | .001           |                 | 15                | .017               | .017       | .004           | .004            |                |                 |
|                   | 9  | .016               | .016           | .002            | .002           |                 | 14                | .039               | .010       | .010           | .002            |                |                 |
|                   | 8  | .032               | .006           | .006            | —              |                 | 13                | .022               | .022       | .004           | .004            |                |                 |
|                   | 7  | .012               | .012           | —               | —              |                 | 12                | .043               | .010       | .010           | .001            |                |                 |
|                   | 6  | .028               | —              | —               | —              |                 | 11                | .020               | .020       | .003           | .003            |                |                 |
| 11                | 17 | .016               | .016           | .005            | .005           |                 | 10                | .038               | .006       | .006           | —               |                |                 |
|                   | 16 | .022               | .022           | .007            | .002           | 9               | .012              | .012               | —          | —              |                 |                |                 |
|                   | 15 | .022               | .022           | .007            | .002           | 8               | .022              | .022               | —          | —              |                 |                |                 |
|                   | 14 | .019               | .019           | .006            | .001           | 7               | .040              | —                  | —          | —              |                 |                |                 |

## TABLES

TABLE A-29 (Continued). TABLES FOR TESTING SIGNIFICANCE IN  $2 \times 2$  TABLES WITH UNEQUAL SAMPLES

|                      |    | Significance Level |                |                 |                |                 |                       | Significance Level |            |                |                 |                |                 |
|----------------------|----|--------------------|----------------|-----------------|----------------|-----------------|-----------------------|--------------------|------------|----------------|-----------------|----------------|-----------------|
|                      |    | $\alpha_1$         | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |                       |                    | $\alpha_1$ | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |
| $n_1=17 \quad n_2=7$ | 17 | 4.017              | 4.017          | 3.003           | 3.003          |                 | $n_1=18 \quad n_2=18$ | 18                 | 13.033     | 13.033         | 12.010          | 11.004         |                 |
|                      | 16 | 3.014              | 3.014          | 2.003           | 2.003          |                 |                       | 17                 | 12.044     | 11.020         | 10.009          | 9.004          |                 |
|                      | 15 | 3.033              | 2.009          | 2.009           | 1.001          |                 |                       | 16                 | 10.030     | 9.014          | 8.008           | 7.002          |                 |
|                      | 14 | 2.021              | 2.021          | 1.004           | 1.004          |                 |                       | 15                 | 9.038      | 8.018          | 7.008           | 6.003          |                 |
|                      | 13 | 2.042              | 1.009          | 1.009           | 0.001          |                 |                       | 14                 | 8.043      | 7.020          | 6.009           | 5.003          |                 |
|                      | 12 | 1.018              | 1.018          | 0.003           | 0.003          |                 |                       | 13                 | 7.046      | 6.022          | 5.009           | 4.002          |                 |
|                      | 11 | 1.034              | 0.005          | 0.005           | 0.005          |                 |                       | 12                 | 6.047      | 5.022          | 4.009           | 3.003          |                 |
|                      | 10 | 0.010              | 0.010          | 0.010           | —              |                 |                       | 11                 | 5.046      | 4.020          | 3.008           | 2.003          |                 |
|                      | 9  | 0.019              | 0.019          | —               | —              |                 |                       | 10                 | 4.043      | 3.015          | 2.006           | 1.001          |                 |
|                      | 8  | 0.033              | —              | —               | —              |                 |                       | 9                  | 3.033      | 2.014          | 1.004           | 1.004          |                 |
| 6                    | 17 | 3.011              | 3.011          | 2.003           | 2.003          |                 | 17                    | 8                  | 2.030      | 1.009          | 1.009           | 0.001          |                 |
|                      | 16 | 3.040              | 2.008          | 2.008           | 1.001          |                 |                       | 7                  | 1.020      | 1.020          | 0.004           | 0.004          |                 |
|                      | 15 | 2.021              | 2.021          | 1.003           | 1.003          |                 |                       | 6                  | 1.044      | 0.010          | 0.010           | —              |                 |
|                      | 14 | 2.045 +            | 1.009          | 1.009           | 0.001          |                 |                       | 5                  | 0.033      | 0.023          | —               | —              |                 |
|                      | 13 | 1.018              | 1.018          | 0.003           | 0.003          |                 |                       | 18                 | 13.045 +   | 12.019         | 11.008          | 10.003         |                 |
|                      | 12 | 1.035              | 0.005          | 0.005           | 0.005          |                 |                       | 17                 | 11.035     | 10.016         | 9.007           | 8.002          |                 |
|                      | 11 | 0.009              | 0.009          | 0.009           | —              |                 |                       | 16                 | 10.049     | 9.023          | 8.010           | 7.004          |                 |
|                      | 10 | 0.017              | 0.017          | —               | —              |                 |                       | 15                 | 9.038      | 7.012          | 6.006           | 5.005          |                 |
|                      | 9  | 0.020              | —              | —               | —              |                 |                       | 14                 | 7.030      | 6.013          | 5.005 +         | 4.003          |                 |
|                      | 8  | 0.050              | —              | —               | —              |                 |                       | 13                 | 6.031      | 5.013          | 4.005           | 3.004          |                 |
| 5                    | 17 | 3.043              | 2.006          | 2.006           | 1.001          |                 | 12                    | 5.030              | 4.012      | 3.004          | 2.003           |                |                 |
|                      | 16 | 2.024              | 2.024          | 1.003           | 1.003          |                 | 11                    | 4.028              | 3.010 +    | 2.003          | 1.003           |                |                 |
|                      | 15 | 1.009              | 1.009          | 1.009           | 0.001          |                 | 10                    | 3.033              | 3.023      | 2.008          | 1.003           |                |                 |
|                      | 14 | 1.021              | 1.021          | 0.003           | 0.003          |                 | 9                     | 3.047              | 2.018      | 1.005          | 1.005           |                |                 |
|                      | 13 | 1.039              | 0.005          | 0.005           | 0.005          |                 | 8                     | 2.037              | 1.011      | 0.002          | 0.002           |                |                 |
|                      | 12 | 0.010              | 0.010          | 0.010           | —              |                 | 7                     | 1.025              | 1.025      | 0.005          | 0.005           |                |                 |
|                      | 11 | 0.018              | 0.018          | —               | —              |                 | 6                     | 0.011              | 0.011      | —              | —               |                |                 |
|                      | 10 | 0.030              | —              | —               | —              |                 | 5                     | 0.026              | —          | —              | —               |                |                 |
|                      | 9  | 0.049              | —              | —               | —              |                 | 16                    | 18                 | 12.039     | 11.016         | 10.006          | 9.002          |                 |
|                      | 4  | 17                 | 2.029          | 1.003           | 1.003          | 1.003           |                       |                    | 17         | 10.029         | 9.012           | 8.005          | 7.002           |
| 16                   |    | 1.012              | 1.012          | 0.001           | 0.001          |                 |                       | 16                 | 9.038      | 8.017          | 7.007           | 6.002          |                 |
| 15                   |    | 1.028              | 0.003          | 0.003           | 0.003          |                 |                       | 15                 | 8.043      | 7.019          | 6.008           | 5.003          |                 |
| 14                   |    | 0.006              | 0.006          | 0.006           | —              |                 |                       | 14                 | 7.046      | 6.020          | 5.008           | 4.003          |                 |
| 13                   |    | 0.012              | 0.012          | —               | —              |                 |                       | 13                 | 6.045 +    | 5.020          | 4.007           | 3.002          |                 |
| 12                   |    | 0.021              | 0.021          | —               | —              |                 |                       | 12                 | 5.043      | 4.018          | 3.006           | 2.003          |                 |
| 11                   |    | 0.036 +            | —              | —               | —              |                 |                       | 11                 | 4.037      | 3.015          | 2.004           | 1.003          |                 |
| 10                   |    | —                  | —              | —               | —              |                 |                       | 10                 | 3.031      | 2.011          | 1.003           | 0.001          |                 |
| 3                    | 17 | 1.016              | 1.016          | 0.001           | 0.001          |                 |                       | 9                  | 2.023      | 2.023          | 1.006           | 0.002          |                 |
|                      | 16 | 1.046              | 0.004          | 0.004           | 0.004          |                 | 8                     | 2.046              | 1.014      | 0.002          | 0.002           |                |                 |
|                      | 15 | 0.009              | 0.009          | 0.009           | —              |                 | 7                     | 1.030              | 0.006      | 0.006          | —               |                |                 |
|                      | 14 | 0.018              | 0.018          | —               | —              |                 | 6                     | 0.014              | 0.014      | —              | —               |                |                 |
|                      | 13 | 0.031              | —              | —               | —              |                 | 5                     | 0.031              | —          | —              | —               |                |                 |
|                      | 12 | 0.049              | —              | —               | —              |                 | 15                    | 18                 | 11.033     | 10.013         | 9.005           | 8.005          |                 |
|                      | 2  | 17                 | 0.006          | 0.006           | 0.006          | —               |                       |                    | 17         | 9.023          | 8.009           | 7.003          | 6.004           |
| 16                   |    | 0.018              | 0.018          | —               | —              |                 |                       | 16                 | 8.029      | 7.012          | 6.004           | 5.005          |                 |
| 15                   |    | 0.035 +            | —              | —               | —              |                 |                       | 15                 | 7.031      | 6.013          | 5.005           | 4.004          |                 |
|                      |    |                    |                |                 |                |                 |                       | 14                 | 6.031      | 5.013          | 4.004           | 3.004          |                 |
|                      |    |                    |                |                 |                | 13              |                       | 5.029              | 4.011      | 3.004          | 2.003           |                |                 |

## TABLES

TABLE A-29 (Continued). TABLES FOR TESTING SIGNIFICANCE IN  $2 \times 2$  TABLES WITH UNEQUAL SAMPLES

|                   |    | $a_1$   | Significance Level |                 |                |                   |         |         | $a_1$   | Significance Level |                 |                |                 |
|-------------------|----|---------|--------------------|-----------------|----------------|-------------------|---------|---------|---------|--------------------|-----------------|----------------|-----------------|
|                   |    |         | 0.05<br>(0.10)     | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01)   |         |         |         | 0.05<br>(0.10)     | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |
| $n_1=18$ $n_2=15$ | 12 | 4.025 + | 3.009              | 3.009           | 2.003          | $n_1=18$ $n_2=12$ | 10      | 2.038   | 1.010 + | 0.001              | 0.001           |                |                 |
|                   | 11 | 3.030   | 3.030              | 2.008           | 1.001          |                   | 9       | 1.021   | 1.021   | 0.003              | 0.003           |                |                 |
|                   | 10 | 3.041   | 2.014              | 1.004           | 1.004          |                   | 8       | 1.040   | 0.007   | 0.007              | —               |                |                 |
|                   | 9  | 2.030   | 1.008              | 1.003           | 0.001          |                   | 7       | 0.016   | 0.016   | —                  | —               |                |                 |
|                   | 8  | 1.018   | 1.018              | 0.003           | 0.003          |                   | 6       | 0.031   | —       | —                  | —               |                |                 |
|                   | 7  | 1.038   | 0.007              | 0.007           | —              |                   | 11      | 18      | 8.045 + | 7.014              | 6.004           | 6.004          |                 |
|                   | 6  | 0.017   | 0.017              | —               | —              |                   |         | 17      | 6.018   | 6.018              | 5.006           | 4.001          |                 |
|                   | 5  | 0.036   | —                  | —               | —              |                   |         | 16      | 5.018   | 5.018              | 4.005 +         | 3.001          |                 |
|                   | 14 | 18      | 10.028             | 9.010 -         | 9.010 -        |                   |         | 8.003   | 15      | 5.043              | 4.015 -         | 3.004          | 3.004           |
|                   |    | 17      | 9.043              | 8.017           | 7.006          |                   |         | 6.002   | 14      | 4.033              | 3.011           | 2.003          | 2.003           |
|                   |    | 16      | 8.050 -            | 7.021           | 6.008          |                   |         | 5.003   | 13      | 3.023              | 3.023           | 2.007          | 1.001           |
|                   |    | 15      | 6.022              | 6.022           | 5.008          |                   | 4.003   | 12      | 3.046   | 2.014              | 1.003           | 1.003          |                 |
|                   |    | 14      | 6.049              | 5.020           | 4.007          |                   | 3.002   | 11      | 2.029   | 1.007              | 1.007           | 0.001          |                 |
|                   |    | 13      | 5.044              | 4.017           | 3.008          |                   | 2.001   | 10      | 1.015 - | 1.015 -            | 0.002           | 0.002          |                 |
| 12                |    | 4.037   | 3.013              | 2.004           | 2.004          | 9                 | 1.029   | 0.005 - | 0.005 - | 0.005 -            |                 |                |                 |
| 11                |    | 3.028   | 2.009              | 2.009           | 1.003          | 8                 | 0.010 + | 0.010 + | —       | —                  |                 |                |                 |
| 10                |    | 2.020   | 2.020              | 1.005 -         | 1.005 -        | 7                 | 0.020   | 0.020   | —       | —                  |                 |                |                 |
| 9                 |    | 2.039   | 1.011              | 0.002           | 0.002          | 6                 | 0.039   | —       | —       | —                  |                 |                |                 |
| 18                | 8  | 1.024   | 1.024              | 0.004           | 0.004          | 10                | 18      | 7.037   | 6.010 + | 5.003              | 5.003           |                |                 |
|                   | 7  | 1.047   | 0.009              | 0.009           | —              |                   | 17      | 6.041   | 5.013   | 4.003              | 4.003           |                |                 |
|                   | 6  | 0.020   | 0.020              | —               | —              |                   | 16      | 5.036   | 4.011   | 3.003              | 3.003           |                |                 |
|                   | 5  | 0.043   | —                  | —               | —              |                   | 15      | 4.038   | 3.008   | 3.008              | 2.002           |                |                 |
|                   | 18 | 9.023   | 9.023              | 8.008           | 7.002          |                   | 14      | 3.019   | 3.019   | 2.005 -            | 2.005 -         |                |                 |
|                   | 17 | 8.034   | 7.012              | 6.004           | 6.004          |                   | 13      | 3.039   | 2.011   | 1.002              | 1.002           |                |                 |
|                   | 16 | 7.037   | 6.014              | 5.005 -         | 5.005 -        | 12                | 2.023   | 2.023   | 1.005 + | 0.001              |                 |                |                 |
|                   | 15 | 6.036   | 5.014              | 4.004           | 4.004          | 11                | 2.043   | 1.011   | 0.001   | 0.001              |                 |                |                 |
|                   | 14 | 5.033   | 4.012              | 3.004           | 3.004          | 10                | 1.022   | 1.022   | 0.003   | 0.003              |                 |                |                 |
|                   | 13 | 4.027   | 3.009              | 3.009           | 2.002          | 9                 | 1.040   | 0.007   | 0.007   | —                  |                 |                |                 |
|                   | 12 | 3.020   | 3.020              | 2.006           | 1.001          | 8                 | 0.014   | 0.014   | —       | —                  |                 |                |                 |
|                   | 11 | 3.040   | 2.013              | 1.003           | 1.003          | 7                 | 0.037   | —       | —       | —                  |                 |                |                 |
|                   | 10 | 2.027   | 1.007              | 1.007           | 0.001          | 6                 | 0.049   | —       | —       | —                  |                 |                |                 |
|                   | 12 | 9       | 1.015 +            | 1.015 +         | 0.002          | 0.002             | 9       | 18      | 6.029   | 5.007              | 5.007           | 4.002          |                 |
| 8                 |    | 1.031   | 0.006              | 0.006           | —              | 17                |         | 5.030   | 4.008   | 4.008              | 3.002           |                |                 |
| 7                 |    | 0.012   | 0.012              | —               | —              | 16                |         | 4.023   | 4.023   | 3.006              | 2.001           |                |                 |
| 6                 |    | 0.028 + | —                  | —               | —              | 15                |         | 3.016   | 3.016   | 2.004              | 2.004           |                |                 |
| 18                |    | 8.018   | 8.018              | 7.006           | 6.002          | 14                |         | 3.034   | 2.009   | 2.009              | 1.002           |                |                 |
| 17                |    | 7.026   | 6.009              | 6.009           | 5.003          | 13                |         | 2.019   | 2.019   | 1.004              | 1.004           |                |                 |
| 16                |    | 6.027   | 5.009              | 5.009           | 4.003          | 12                | 2.037   | 1.009   | 1.009   | 0.001              |                 |                |                 |
| 15                |    | 5.024   | 5.024              | 4.006           | 3.002          | 11                | 1.018   | 1.018   | 0.003   | 0.002              |                 |                |                 |
| 14                |    | 4.020   | 4.020              | 3.006           | 2.001          | 10                | 1.033   | 0.003 + | 0.003 + | —                  |                 |                |                 |
| 13                |    | 4.043   | 3.014              | 2.004           | 2.004          | 9                 | 0.010 + | 0.010 + | —       | —                  |                 |                |                 |
| 12                |    | 3.030   | 2.009              | 2.009           | 1.002          | 8                 | 0.030   | 0.030   | —       | —                  |                 |                |                 |
| 11                |    | 2.019   | 2.019              | 1.005 -         | 1.005 -        | 7                 | 0.039   | —       | —       | —                  |                 |                |                 |

## TABLES

TABLE A-29 (Continued). TABLES FOR TESTING SIGNIFICANCE IN  $2 \times 2$  TABLES WITH UNEQUAL SAMPLES

|                  |    | Significance Level |                |                 |                |                 |                  | Significance Level |                   |                |                 |                |                 |       |
|------------------|----|--------------------|----------------|-----------------|----------------|-----------------|------------------|--------------------|-------------------|----------------|-----------------|----------------|-----------------|-------|
|                  |    | $\alpha_1$         | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |                  |                    | $\alpha_1$        | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |       |
| $n_1=18$ $n_2=8$ | 18 | 5.022              | 5.022          | 4.005           | —              | 4.005           | $n_1=18$ $n_2=4$ | 13                 | 0.017             | 0.017          | —               | —              | —               |       |
|                  | 17 | 4.020              | 4.020          | 3.004           | —              | 3.004           |                  | 12                 | 0.029             | —              | —               | —              | —               |       |
|                  | 16 | 3.014              | 3.014          | 2.003           | —              | 2.003           |                  | 11                 | 0.045 +           | —              | —               | —              | —               |       |
|                  | 15 | 3.032              | 2.008          | 2.005           | —              | 1.001           |                  | 3                  | 18                | 1.014          | 1.014           | 0.001          | 0.001           | —     |
|                  | 14 | 2.017              | 2.017          | 1.003           | —              | 1.003           |                  |                    | 17                | 1.041          | 0.003           | 0.003          | 0.003           | —     |
|                  | 13 | 2.034              | 1.007          | 1.007           | —              | 0.001           |                  |                    | 16                | 0.008          | 0.008           | 0.008          | —               | —     |
|                  | 12 | 1.015 +            | 1.015 +        | 0.002           | —              | 0.002           |                  |                    | 15                | 0.015 +        | 0.015 +         | —              | —               | —     |
|                  | 11 | 1.028              | 0.004          | 0.004           | —              | 0.004           |                  |                    | 14                | 0.028          | —               | —              | —               | —     |
|                  | 10 | 1.049              | 0.008          | 0.008           | —              | —               |                  | 13                 | 0.042             | —              | —               | —              | —               |       |
|                  | 9  | 0.016              | 0.016          | —               | —              | —               |                  | 2                  | 18                | 0.005 +        | 0.005 +         | 0.005 +        | —               | —     |
|                  | 8  | 0.028              | —              | —               | —              | —               |                  |                    | 17                | 0.016          | 0.016           | —              | —               | —     |
|                  | 7  | 0.048              | —              | —               | —              | —               |                  |                    | 16                | 0.032          | —               | —              | —               | —     |
|                  | 7  | 18                 | 4.015 +        | 4.015 +         | 3.003          | 3.003           |                  |                    | $n_1=19$ $n_2=19$ | 19             | 14.023          | 14.023         | 13.010          | —     |
| 17               |    | 3.012              | 3.012          | 2.002           | 2.002          | 18              | 13.045           |                    |                   | 12.021         | 11.009          | —              | 10.004          |       |
| 16               |    | 3.032              | 2.007          | 2.007           | 1.001          | 17              | 11.031           | 10.015             |                   | 9.006          | —               | 8.003          |                 |       |
| 15               |    | 2.017              | 2.017          | 1.003           | 1.003          | 16              | 10.036           | 9.019              |                   | 8.009          | —               | 7.003          |                 |       |
| 14               |    | 2.034              | 1.007          | 1.007           | 0.001          | 15              | 9.046            | 8.022              |                   | 6.004          | —               | 6.004          |                 |       |
| 13               |    | 1.014              | 1.014          | 0.002           | 0.002          | 14              | 8.050            | 7.024              |                   | 5.004          | —               | 5.004          |                 |       |
| 12               |    | 1.027              | 0.004          | 0.004           | 0.004          | 13              | 6.025 +          | 5.011              |                   | 4.004          | —               | 4.004          |                 |       |
| 11               |    | 1.046              | 0.007          | 0.007           | —              | —               | 12               | 5.024              |                   | 5.024          | 3.003           | —              | 3.003           |       |
| 10               |    | 0.013              | 0.013          | —               | —              | —               | 11               | 5.050              |                   | 4.022          | 3.009           | —              | 2.003           |       |
| 9                |    | 0.024              | 0.024          | —               | —              | —               | 10               | 4.046              |                   | 3.019          | 2.006           | —              | 1.002           |       |
| 8                |    | 0.040              | —              | —               | —              | —               | 9                | 3.039              |                   | 2.015          | 1.004           | —              | 1.004           |       |
| 6                |    | 18                 | 3.010          | 3.010           | 3.010          | 2.001           | 18               | 8                  |                   | 2.031          | 1.009           | 1.009          | —               | 0.002 |
|                  |    | 17                 | 3.035 +        | 2.006           | 2.006          | 1.001           |                  | 7                  |                   | 1.021          | 1.021           | 0.004          | —               | 0.004 |
|                  | 16 | 2.018              | 2.018          | 1.003           | 1.003          | 6               |                  | 1.045              | 0.010             | 0.010          | —               | —              |                 |       |
|                  | 15 | 2.028              | 1.007          | 1.007           | 0.001          | 5               |                  | 0.022              | 0.022             | —              | —               | —              |                 |       |
|                  | 14 | 1.015              | 1.015          | 0.002           | 0.002          | 19              |                  | 14.046             | 13.020            | 12.008         | —               | 11.003         |                 |       |
|                  | 13 | 1.028              | 0.003          | 0.003           | 0.003          | 18              |                  | 12.037             | 11.017            | 10.007         | —               | 9.003          |                 |       |
|                  | 12 | 1.048              | 0.007          | 0.007           | —              | 17              |                  | 10.024             | 10.024            | 8.004          | —               | 8.004          |                 |       |
|                  | 11 | 0.013              | 0.013          | —               | —              | 16              |                  | 9.030              | 8.014             | 7.006          | —               | 6.002          |                 |       |
|                  | 10 | 0.022              | 0.022          | —               | —              | 15              |                  | 8.033              | 7.015 +           | 6.008          | —               | 5.002          |                 |       |
|                  | 9  | 0.037              | —              | —               | —              | 14              |                  | 7.035 +            | 6.016             | 5.006          | —               | 4.002          |                 |       |
|                  | 5  | 18                 | 3.040          | 2.006           | 2.006          | 1.001           |                  | 13                 | 6.035             | 5.015 +        | 4.006           | —              | 3.003           |       |
|                  |    | 17                 | 2.021          | 2.021           | 1.002          | 1.002           |                  | 12                 | 5.023             | 4.014          | 3.005           | —              | 3.005           |       |
|                  |    | 16                 | 2.048          | 1.008           | 1.008          | 0.001           |                  | 11                 | 4.030             | 3.011          | 2.004           | —              | 2.004           |       |
| 15               |    | 1.017              | 1.017          | 0.002           | 0.002          | 10              | 3.025            | 3.025              | 2.008             | —              | 1.002           |                |                 |       |
| 14               |    | 1.033              | 0.004          | 0.004           | 0.004          | 9               | 3.049            | 2.019              | 1.005 +           | —              | 0.001           |                |                 |       |
| 13               |    | 0.007              | 0.007          | 0.007           | —              | 8               | 2.038            | 1.013              | 0.002             | —              | 0.002           |                |                 |       |
| 12               |    | 0.014              | 0.014          | —               | —              | 7               | 1.025 +          | 0.005              | 0.005             | —              | 0.005           |                |                 |       |
| 11               |    | 0.024              | 0.024          | —               | —              | 6               | 0.012            | 0.012              | —                 | —              | —               |                |                 |       |
| 10               |    | 0.028              | —              | —               | —              | 5               | 0.027            | —                  | —                 | —              | —               |                |                 |       |
| 4                |    | 18                 | 2.026          | 1.002           | 1.002          | 1.002           | 17               | 19                 | 13.040            | 12.016         | 11.006          | —              | 10.002          |       |
|                  |    | 17                 | 1.010          | 1.010           | 1.010          | 0.001           |                  | 18                 | 11.030            | 10.013         | 9.005 +         | —              | 8.002           |       |
|                  |    | 16                 | 1.024          | 1.024           | 0.002          | 0.002           |                  | 17                 | 10.040            | 9.018          | 8.008           | —              | 7.003           |       |
|                  |    | 15                 | 1.046          | 0.005           | 0.005          | 0.005           |                  | 16                 | 9.047             | 8.022          | 7.009           | —              | 6.003           |       |
|                  | 14 | 0.010              | 0.010          | 0.010           | —              |                 |                  |                    |                   |                |                 |                |                 |       |

## TABLES

TABLE A-29 (Continued). TABLES FOR TESTING SIGNIFICANCE IN  $2 \times 2$  TABLES WITH UNEQUAL SAMPLES

|                       |        | Significance Level |                |                 |                |                 |                       | Significance Level |            |                |                 |                |                 |
|-----------------------|--------|--------------------|----------------|-----------------|----------------|-----------------|-----------------------|--------------------|------------|----------------|-----------------|----------------|-----------------|
|                       |        | $\alpha_1$         | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |                       |                    | $\alpha_1$ | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |
| $n_1=19 \quad n_2=17$ | 15     | 8.050              | 7.033          | 6.010           | 5.004          |                 | $n_1=19 \quad n_2=18$ | 19                 | 9.030      | 8.020          | 7.006           | 6.003          | 5.002           |
|                       | 14     | 6.023              | 6.033          | 5.010           | 4.003          |                 |                       | 18                 | 8.039      | 7.010          | 6.003           | 5.004          | 4.003           |
|                       | 13     | 6.049              | 5.033          | 4.008           | 3.003          |                 |                       | 17                 | 7.031      | 6.011          | 5.004           | 4.003          | 3.003           |
|                       | 12     | 5.045              | 4.019          | 3.007           | 2.003          |                 |                       | 16                 | 6.039      | 5.011          | 4.003           | 3.004          | 2.003           |
|                       | 11     | 4.039              | 3.015          | 2.005           | 1.003          |                 |                       | 15                 | 5.035      | 4.009          | 3.006           | 2.003          | 1.003           |
|                       | 10     | 3.033              | 2.011          | 1.003           | 0.001          |                 |                       | 14                 | 4.030      | 3.015          | 2.004           | 1.005          | 0.001           |
|                       | 9      | 2.024              | 1.015          | 0.003           | 0.003          |                 |                       | 13                 | 3.029      | 2.009          | 1.005           | 0.007          | 0.003           |
|                       | 8      | 1.031              | 0.008          | 0.008           | —              |                 |                       | 12                 | 2.019      | 1.010          | 0.003           | 0.003          | 0.003           |
|                       | 7      | 0.014              | —              | —               | —              |                 |                       | 11                 | 1.030      | 0.007          | —               | —              | —               |
|                       | 6      | 0.021              | —              | —               | —              |                 |                       | 10                 | 0.015      | —              | —               | —              | —               |
|                       | 5      | —                  | —              | —               | —              |                 |                       | 9                  | 0.030      | —              | —               | —              | —               |
|                       | 16     | 12.035             | 11.013         | 10.005          | 9.004          |                 |                       | 12                 | 9.049      | 8.016          | 7.005           | 6.003          | 5.002           |
|                       | 15     | 10.024             | 9.013          | 8.005           | 7.003          |                 |                       | 11                 | 8.041      | 7.013          | 6.003           | 5.004          | 4.003           |
|                       | 14     | 9.031              | 8.013          | 7.005           | 6.003          |                 |                       | 10                 | 7.047      | 6.016          | 5.004           | 4.003          | 3.003           |
|                       | 13     | 8.025              | 7.015          | 6.006           | 5.003          |                 |                       | 9                  | 6.043      | 5.015          | 4.004           | 3.003          | 2.003           |
|                       | 12     | 7.036              | 6.015          | 5.006           | 4.003          |                 |                       | 8                  | 5.035      | 4.013          | 3.003           | 2.003          | 1.003           |
| 11                    | 6.034  | 5.014              | 4.005          | 3.003           |                | 7               | 4.037                 | 3.018              | 2.005      | 1.002          | 0.001           |                |                 |
| 10                    | 5.031  | 4.013              | 3.004          | 2.003           |                | 6               | 3.035                 | 2.010              | 1.002      | 0.001          | 0.001           |                |                 |
| 9                     | 4.027  | 3.010              | 2.007          | 1.003           |                | 5               | 2.031                 | 1.019              | 0.001      | 0.001          | 0.001           |                |                 |
| 8                     | 3.021  | 2.007              | 1.004          | 0.003           |                | 4               | 1.030                 | 0.006              | 0.003      | 0.003          | 0.003           |                |                 |
| 7                     | 2.030  | 1.009              | 0.003          | 0.003           |                | 3               | 0.013                 | 0.013              | —          | —              | —               |                |                 |
| 6                     | 1.018  | 0.007              | 0.007          | —               |                | 2               | 0.025                 | 0.025              | —          | —              | —               |                |                 |
| 5                     | 0.017  | —                  | —              | —               |                | 1               | 0.046                 | —                  | —          | —              | —               |                |                 |
| 15                    | 11.039 | 10.011             | 9.004          | 8.003           |                | 19              | 7.033                 | 6.009              | 5.003      | 4.003          | 3.003           | 2.001          |                 |
| 14                    | 10.046 | 9.019              | 8.007          | 7.003           |                | 18              | 6.035                 | 5.011              | 4.003      | 3.003          | 2.004           | 1.002          |                 |
| 13                    | 9.023  | 8.023              | 7.009          | 6.003           |                | 17              | 5.030                 | 4.009              | 3.006      | 2.008          | 1.004           | 0.001          |                 |
| 12                    | 8.025  | 7.025              | 6.010          | 5.003           |                | 16              | 4.033                 | 3.015              | 2.004      | 1.004          | 0.003           | 0.003          |                 |
| 11                    | 7.024  | 6.024              | 5.009          | 4.003           |                | 15              | 3.030                 | 2.008              | 1.008      | 0.003          | 0.003           | 0.003          |                 |
| 10                    | 6.023  | 5.023              | 4.008          | 3.003           |                | 14              | 2.017                 | 1.004              | 0.003      | 0.003          | 0.003           | 0.003          |                 |
| 9                     | 5.015  | 4.015              | 3.009          | 2.003           |                | 13              | 1.016                 | 0.002              | 0.002      | 0.002          | 0.002           | 0.002          |                 |
| 8                     | 4.037  | 3.014              | 2.004          | 1.003           |                | 12              | 0.009                 | 0.009              | —          | —              | —               | —              |                 |
| 7                     | 3.029  | 2.009              | 1.003          | 0.003           |                | 11              | 0.009                 | 0.009              | —          | —              | —               | —              |                 |
| 6                     | 2.030  | 1.011              | 0.003          | 0.003           |                | 10              | 0.018                 | 0.018              | —          | —              | —               | —              |                 |
| 5                     | 1.033  | 0.009              | 0.009          | —               |                | 9               | 0.033                 | —                  | —          | —              | —               | —              |                 |
| 14                    | 10.024 | 9.014              | 8.006          | 7.005           |                | 8               | 0.033                 | —                  | —          | —              | —               | —              |                 |
| 13                    | 9.027  | 8.017              | 7.006          | 6.003           |                | 7               | 0.033                 | —                  | —          | —              | —               | —              |                 |
| 12                    | 8.043  | 7.017              | 6.006          | 5.003           |                | 6               | 0.049                 | —                  | —          | —              | —               | —              |                 |
| 11                    | 7.043  | 6.017              | 5.006          | 4.003           |                | 5               | —                     | —                  | —          | —              | —               | —              |                 |
| 10                    | 6.039  | 5.015              | 4.005          | 3.001           |                | 4               | —                     | —                  | —          | —              | —               | —              |                 |
| 9                     | 5.034  | 4.013              | 3.004          | 2.003           |                | 3               | —                     | —                  | —          | —              | —               | —              |                 |
| 8                     | 4.027  | 3.009              | 2.003          | 1.001           |                | 2               | —                     | —                  | —          | —              | —               | —              |                 |
| 7                     | 3.030  | 2.006              | 1.001          | 0.001           |                | 1               | —                     | —                  | —          | —              | —               | —              |                 |
| 6                     | 2.027  | 1.007              | 0.001          | 0.001           |                | 0               | —                     | —                  | —          | —              | —               | —              |                 |
| 5                     | 1.015  | 0.003              | 0.003          | —               |                | 0               | —                     | —                  | —          | —              | —               | —              |                 |
| 4                     | 0.030  | 0.005              | 0.005          | —               |                | 0               | —                     | —                  | —          | —              | —               | —              |                 |
| 3                     | 0.012  | 0.012              | —              | —               |                | 0               | —                     | —                  | —          | —              | —               | —              |                 |
| 2                     | 0.024  | 0.024              | —              | —               |                | 0               | —                     | —                  | —          | —              | —               | —              |                 |
| 1                     | 0.049  | —                  | —              | —               |                | 0               | —                     | —                  | —          | —              | —               | —              |                 |



## TABLES

TABLE A-29 (Continued). TABLES FOR TESTING SIGNIFICANCE IN  $2 \times 2$  TABLES WITH UNEQUAL SAMPLES

|                  |    | Significance Level |                |                 |                |                 |                  | Significance Level |            |                |                 |                |                 |                   |        |        |        |        |        |
|------------------|----|--------------------|----------------|-----------------|----------------|-----------------|------------------|--------------------|------------|----------------|-----------------|----------------|-----------------|-------------------|--------|--------|--------|--------|--------|
|                  |    | $\alpha_1$         | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |                  |                    | $\alpha_1$ | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |                   |        |        |        |        |        |
| $n_1=19$ $n_2=9$ | 8  | 19                 | 6.028          | 5.006           | 5.006          | 4.001           | $n_1=19$ $n_2=5$ | 4                  | 12         | 0.019          | 0.019           | —              | —               |                   |        |        |        |        |        |
|                  |    | 18                 | 5.026          | 4.007           | 4.007          | 3.001           |                  |                    | 11         | 0.030          | —               | —              | —               |                   |        |        |        |        |        |
|                  |    | 17                 | 4.020          | 4.020           | 3.005          | 3.005           |                  |                    | 10         | 0.047          | —               | —              | —               |                   |        |        |        |        |        |
|                  |    | 16                 | 4.044          | 3.013           | 2.003          | 2.003           |                  |                    | 19         | 2.024          | 2.024           | 1.002          | 1.002           |                   |        |        |        |        |        |
|                  |    | 15                 | 3.028          | 2.007           | 2.007          | 1.001           |                  |                    | 18         | 1.009          | 1.009           | 1.009          | 0.001           |                   |        |        |        |        |        |
|                  |    | 14                 | 2.015          | 2.015           | 1.003          | 1.003           |                  |                    | 17         | 1.021          | 1.021           | 0.002          | 0.002           |                   |        |        |        |        |        |
|                  |    | 13                 | 2.029          | 1.006           | 1.006          | 0.001           |                  |                    | 16         | 1.040          | 0.004           | 0.004          | 0.004           |                   |        |        |        |        |        |
|                  |    | 12                 | 1.013          | 1.013           | 0.002          | 0.002           |                  |                    | 15         | 0.008          | 0.008           | 0.008          | —               |                   |        |        |        |        |        |
|                  |    | 11                 | 1.024          | 1.024           | 0.004          | 0.004           |                  |                    | 14         | 0.014          | 0.014           | —              | —               |                   |        |        |        |        |        |
|                  |    | 10                 | 1.042          | 0.007           | 0.007          | —               |                  |                    | 13         | 0.024          | 0.024           | —              | —               |                   |        |        |        |        |        |
|                  |    | 9                  | 0.013          | 0.013           | —              | —               |                  |                    | 12         | 0.037          | —               | —              | —               |                   |        |        |        |        |        |
|                  |    | 8                  | 0.024          | 0.024           | —              | —               |                  |                    | 8          | 19             | 1.013           | 1.013          | 0.001           | 0.001             |        |        |        |        |        |
|                  |    | 7                  | 0.043          | —               | —              | —               |                  |                    |            |                |                 |                |                 |                   |        |        |        |        |        |
|                  | 7  | 19                 | 5.019          | 5.019           | 4.004          | 4.004           |                  | 18                 |            |                |                 |                |                 |                   | 1.038  | 0.003  | 0.003  | 0.003  |        |
|                  |    | 18                 | 4.017          | 4.017           | 3.004          | 3.004           |                  | 17                 |            |                |                 |                |                 |                   | 0.006  | 0.006  | 0.006  | —      |        |
|                  |    | 17                 | 4.044          | 3.011           | 2.002          | 2.002           |                  | 16                 |            |                |                 |                |                 |                   | 0.013  | 0.013  | —      | —      |        |
|                  |    | 16                 | 3.027          | 2.005           | 2.005          | 1.001           |                  | 15                 |            |                |                 |                |                 |                   | 0.023  | 0.023  | —      | —      |        |
|                  |    | 15                 | 2.014          | 2.014           | 1.002          | 1.002           |                  | 14                 | 0.036      | —              | —               | —              |                 |                   |        |        |        |        |        |
|                  |    | 14                 | 2.027          | 1.006           | 1.006          | 0.001           |                  | 2                  | 19         | 0.005          | 0.005           | 0.005          | 0.005           |                   |        |        |        |        |        |
|                  |    | 13                 | 2.049          | 1.011           | 0.001          | 0.001           |                  |                    |            |                |                 |                |                 | 18                | 0.014  | 0.014  | —      | —      |        |
|                  |    | 12                 | 1.021          | 1.021           | 0.003          | 0.003           |                  |                    |            |                |                 |                |                 | 17                | 0.029  | —      | —      | —      |        |
|                  |    | 11                 | 1.038          | 0.006           | 0.006          | —               |                  |                    |            |                |                 |                |                 | 16                | 0.048  | —      | —      | —      |        |
|                  |    | 10                 | 0.011          | 0.011           | —              | —               |                  |                    |            |                |                 |                |                 | $n_1=20$ $n_2=20$ | 20     | 15.024 | 13.024 | 13.004 | 13.004 |
|                  |    | 9                  | 0.020          | 0.020           | —              | —               |                  |                    |            |                |                 |                |                 |                   |        |        |        |        |        |
|                  |    | 8                  | 0.034          | —               | —              | —               |                  | 18                 | 12.032     | 11.015         | 10.007          | 9.003          |                 |                   |        |        |        |        |        |
| 6                | 19 | 4.013              | 4.013          | 3.002           | 3.002          | 17              | 11.041           | 10.020             | 9.009      | 8.004          |                 |                |                 |                   |        |        |        |        |        |
|                  | 18 | 4.047              | 3.010          | 2.002           | 2.002          | 16              | 10.048           | 9.024              | 7.005      | 7.005          |                 |                |                 |                   |        |        |        |        |        |
|                  | 17 | 3.028              | 2.006          | 2.006           | 1.001          | 15              | 8.027            | 7.012              | 6.005      | 5.002          |                 |                |                 |                   |        |        |        |        |        |
|                  | 16 | 2.014              | 2.014          | 1.002           | 1.002          | 14              | 7.028            | 6.013              | 5.005      | 4.002          |                 |                |                 |                   |        |        |        |        |        |
|                  | 15 | 2.028              | 1.005          | 1.005           | 0.001          | 13              | 6.028            | 5.012              | 4.005      | 4.005          |                 |                |                 |                   |        |        |        |        |        |
|                  | 14 | 1.011              | 1.011          | 0.001           | 0.001          | 12              | 5.027            | 4.011              | 3.004      | 3.004          |                 |                |                 |                   |        |        |        |        |        |
|                  | 13 | 1.021              | 1.021          | 0.003           | 0.003          | 11              | 4.024            | 4.024              | 3.009      | 2.003          |                 |                |                 |                   |        |        |        |        |        |
|                  | 12 | 1.037              | 0.005          | 0.005           | —              | 10              | 4.048            | 3.020              | 2.007      | 1.002          |                 |                |                 |                   |        |        |        |        |        |
|                  | 11 | 0.010              | 0.010          | 0.010           | —              | 9               | 3.041            | 2.015              | 1.004      | 1.004          |                 |                |                 |                   |        |        |        |        |        |
|                  | 10 | 0.017              | 0.017          | —               | —              | 8               | 2.032            | 1.010              | 1.010      | 0.002          |                 |                |                 |                   |        |        |        |        |        |
|                  | 9  | 0.030              | —              | —               | —              | 7               | 1.022            | 1.022              | 0.004      | 0.004          |                 |                |                 |                   |        |        |        |        |        |
|                  | 8  | 0.048              | —              | —               | —              | 6               | 1.046            | 0.010              | —          | —              |                 |                |                 |                   |        |        |        |        |        |
| 5                | 6  | 19                 | 4.050          | 3.009           | 3.009          | 2.001           | 5                | 0.024              | 0.024      | —              | —               |                |                 |                   |        |        |        |        |        |
|                  |    | 18                 | 3.031          | 2.005           | 2.005          | 1.001           | 19               | 20                 | 15.047     | 14.020         | 13.008          | 12.003         |                 |                   |        |        |        |        |        |
|                  |    | 17                 | 2.015          | 2.015           | 1.002          | 1.002           |                  |                    |            |                |                 |                | 19              | 13.039            | 12.018 | 11.008 | 10.003 |        |        |
|                  |    | 16                 | 2.032          | 1.006           | 1.006          | 0.000           |                  |                    |            |                |                 |                | 18              | 11.026            | 10.012 | 9.005  | 9.005  |        |        |
|                  |    | 15                 | 1.012          | 1.012           | 0.001          | 0.001           |                  |                    |            |                |                 |                | 17              | 10.032            | 9.015  | 8.006  | 7.002  |        |        |
|                  |    | 14                 | 1.023          | 1.023           | 0.003          | 0.003           |                  |                    |            |                |                 |                | 16              | 9.036             | 8.017  | 7.007  | 6.003  |        |        |
|                  |    | 13                 | 1.039          | 0.005           | 0.005          | —               |                  |                    |            |                |                 |                | 15              | 8.038             | 7.018  | 6.008  | 5.003  |        |        |
|                  |    | 12                 | 0.010          | 0.010           | 0.010          | —               |                  |                    |            |                |                 |                | 14              | 7.039             | 6.018  | 5.007  | 4.003  |        |        |
|                  |    | 11                 | 0.017          | 0.017           | —              | —               |                  |                    |            |                |                 |                | 13              | 6.038             | 5.017  | 4.007  | 3.002  |        |        |
|                  |    | 10                 | 0.028          | —               | —              | —               |                  |                    |            |                |                 |                | 12              | 5.035             | 4.015  | 3.005  | 2.002  |        |        |
|                  |    | 9                  | 0.045          | —               | —              | —               |                  |                    |            |                |                 |                | 11              | 4.031             | 3.012  | 2.004  | 2.004  |        |        |
|                  |    | 19                 | 3.036          | 2.005           | 2.005          | 2.005           |                  |                    |            |                |                 |                | 10              | 3.026             | 2.009  | 2.009  | 1.002  |        |        |
|                  | 18 | 2.016              | 2.016          | 1.002           | 1.002          | 9               |                  |                    |            |                |                 |                | 2.019           | 2.019             | 1.005  | 0.001  |        |        |        |
|                  | 17 | 2.042              | 1.006          | 1.006           | 0.000          | 8               |                  |                    |            |                |                 |                | 2.039           | 1.012             | 0.002  | 0.002  |        |        |        |
|                  | 16 | 1.014              | 1.014          | 0.001           | 0.001          | 7               |                  |                    |            |                |                 |                | 1.026           | 0.005             | 0.005  | —      |        |        |        |
|                  | 15 | 1.028              | 0.003          | 0.003           | 0.003          | 6               | 0.012            | 0.012              | —          | —              |                 |                |                 |                   |        |        |        |        |        |
|                  | 14 | 1.047              | 0.006          | 0.006           | —              | 5               | 0.027            | —                  | —          | —              |                 |                |                 |                   |        |        |        |        |        |
|                  | 13 | 0.011              | 0.011          | —               | —              |                 |                  |                    |            |                |                 |                |                 |                   |        |        |        |        |        |

## TABLES

TABLE A-29 (Continued). TABLES FOR TESTING SIGNIFICANCE IN  $2 \times 2$  TABLES WITH UNEQUAL SAMPLES

|                       |    | Significance Level |                |                 |                |                       |         | Significance Level |            |                |                 |                |
|-----------------------|----|--------------------|----------------|-----------------|----------------|-----------------------|---------|--------------------|------------|----------------|-----------------|----------------|
|                       |    | $\alpha_1$         | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) |                       |         | 0.005<br>(0.01)    | $\alpha_1$ | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) |
| $n_1=20 \quad n_2=18$ | 20 | 14.041             | 13.017         | 12.007          | 11.003         | $n_1=20 \quad n_2=15$ | 13      | 4.028              | 3.010 -    | 3.010 -        | 2.003           |                |
|                       | 19 | 12.032             | 11.014         | 10.006          | 9.002          |                       | 12      | 3.020              | 3.020      | 2.006          | 1.001           |                |
|                       | 18 | 11.043             | 10.020         | 9.008           | 8.003          |                       | 11      | 3.039              | 2.012      | 1.003          | 1.003           |                |
|                       | 17 | 10.050 -           | 9.034          | 7.004           | 7.004          |                       | 10      | 2.026              | 1.007      | 1.007          | 0.001           |                |
|                       | 16 | 8.026              | 7.011          | 6.006 -         | 6.006 -        |                       | 9       | 2.049              | 1.015 -    | 0.002          | 0.002           |                |
|                       | 15 | 7.027              | 6.012          | 5.004           | 5.004          |                       | 8       | 1.029              | 0.006 +    | 0.006 +        | —               |                |
|                       | 14 | 6.026              | 5.011          | 4.004           | 4.004          |                       | 7       | 0.012              | 0.012      | —              | —               |                |
|                       | 13 | 5.024              | 5.024          | 4.009           | 3.003          |                       | 6       | 0.024              | 0.024      | —              | —               |                |
|                       | 12 | 5.047              | 4.020          | 3.007           | 2.002          |                       | 5       | 0.046              | —          | —              | —               |                |
|                       | 11 | 4.041              | 3.016          | 2.006 +         | 1.001          |                       |         |                    |            |                |                 |                |
|                       | 10 | 3.033              | 2.012          | 1.003           | 1.003          |                       | 14      | 20                 | 10.022     | 10.022         | 9.007           | 8.002          |
|                       | 9  | 2.024              | 2.024          | 1.007           | 0.001          |                       | 19      | 9.032              | 8.012      | 7.004          | 7.004           |                |
|                       | 8  | 2.048              | 1.016 -        | 0.003           | 0.003          |                       | 18      | 8.035 +            | 7.014      | 6.005 -        | 6.005 -         |                |
|                       | 7  | 1.031              | 0.006          | 0.006           | —              |                       | 17      | 7.035 -            | 6.013      | 5.005 -        | 5.005 -         |                |
|                       | 6  | 0.014              | 0.014          | —               | —              |                       | 16      | 6.031              | 5.012      | 4.004          | 4.004           |                |
|                       | 5  | 0.031              | —              | —               | —              |                       | 15      | 5.026              | 4.009      | 4.009          | 3.003           |                |
| 17                    | 20 | 13.038             | 12.014         | 11.006 +        | 10.002         | 14                    | 4.020   | 4.020              | 3.007      | 2.002          |                 |                |
|                       | 19 | 11.026             | 10.011         | 9.004           | 9.004          | 13                    | 4.040   | 3.015 -            | 2.004      | 2.004          |                 |                |
|                       | 18 | 10.034             | 9.015 -        | 8.006           | 7.002          | 12                    | 3.029   | 2.009              | 2.009      | 1.002          |                 |                |
|                       | 17 | 9.038              | 8.017          | 7.007           | 6.003          | 11                    | 2.018   | 2.018              | 1.005 -    | 1.005 -        |                 |                |
|                       | 16 | 8.040              | 7.018          | 6.007           | 5.003          | 10                    | 2.035 + | 1.010 -            | 1.010 -    | 0.001          |                 |                |
|                       | 15 | 7.039              | 6.017          | 5.007           | 4.002          | 9                     | 1.019   | 1.019              | 0.003      | 0.003          |                 |                |
|                       | 14 | 6.037              | 5.016          | 4.006           | 3.002          | 8                     | 1.037   | 0.007              | 0.007      | —              |                 |                |
|                       | 13 | 5.033              | 4.013          | 3.005 -         | 3.005 -        | 7                     | 0.014   | 0.014              | —          | —              |                 |                |
|                       | 12 | 4.028              | 3.010 +        | 2.003           | 2.003          | 6                     | 0.029   | —                  | —          | —              |                 |                |
|                       | 11 | 3.022              | 3.022          | 2.007           | 1.002          | 18                    | 20      | 9.017              | 9.017      | 8.006 +        | 7.002           |                |
|                       | 10 | 3.042              | 2.015 +        | 1.004           | 1.004          | 19                    | 8.025 - | 8.025 -            | 7.008      | 6.003          |                 |                |
|                       | 9  | 2.031              | 1.009          | 1.009           | 0.001          | 18                    | 7.026   | 6.009              | 6.009      | 5.003          |                 |                |
|                       | 8  | 1.019              | 1.019          | 0.002           | 0.003          | 17                    | 6.024   | 6.024              | 5.008      | 4.002          |                 |                |
|                       | 7  | 1.037              | 0.008          | 0.008           | —              | 16                    | 5.020   | 5.020              | 4.007      | 3.002          |                 |                |
|                       | 6  | 0.017              | 0.017          | —               | —              | 15                    | 5.041   | 4.015 +            | 3.005 -    | 3.005 -        |                 |                |
|                       | 5  | 0.036              | —              | —               | —              | 14                    | 4.031   | 3.011              | 2.003      | 2.003          |                 |                |
| 16                    | 20 | 12.031             | 11.012         | 10.004          | 10.004         | 13                    | 3.022   | 3.022              | 2.006      | 1.001          |                 |                |
|                       | 19 | 11.049             | 10.021         | 9.008           | 8.003          | 12                    | 3.041   | 2.013              | 1.003      | 1.003          |                 |                |
|                       | 18 | 9.026              | 8.011          | 7.004           | 7.004          | 11                    | 2.026   | 1.007              | 1.007      | 0.001          |                 |                |
|                       | 17 | 8.028              | 7.012          | 6.004           | 6.004          | 10                    | 2.047   | 1.013              | 0.002      | 0.002          |                 |                |
|                       | 16 | 7.028              | 6.012          | 5.004           | 5.004          | 9                     | 1.028   | 0.004              | 0.004      | 0.004          |                 |                |
|                       | 15 | 6.026              | 5.011          | 4.004           | 4.004          | 8                     | 1.047   | 0.009              | 0.009      | —              |                 |                |
|                       | 14 | 5.023              | 5.023          | 4.009           | 3.003          | 7                     | 0.018   | 0.018              | —          | —              |                 |                |
|                       | 13 | 5.045              | 4.019          | 3.007           | 2.002          | 6                     | 0.035 - | —                  | —          | —              |                 |                |
|                       | 12 | 4.038              | 3.014          | 2.004           | 2.004          | 12                    | 20      | 9.044              | 8.014      | 7.004          | 7.004           |                |
|                       | 11 | 3.029              | 2.010 -        | 2.010 -         | 1.002          | 19                    | 7.018   | 7.018              | 6.006      | 5.002          |                 |                |
|                       | 10 | 2.020              | 2.020          | 1.006 +         | 0.001          | 18                    | 6.018   | 6.018              | 5.006      | 4.002          |                 |                |
|                       | 9  | 2.039              | 1.011          | 0.002           | 0.002          | 17                    | 6.043   | 5.016              | 4.005 -    | 4.005 -        |                 |                |
|                       | 8  | 1.023              | 1.023          | 0.004           | 0.004          | 16                    | 5.034   | 4.012              | 3.003      | 3.003          |                 |                |
|                       | 7  | 1.045 +            | 0.009          | 0.009           | —              | 15                    | 4.025 + | 3.006              | 3.008      | 2.002          |                 |                |
|                       | 6  | 0.020              | 0.020          | —               | —              | 14                    | 4.049   | 3.017              | 2.005 -    | 2.005 -        |                 |                |
|                       | 5  | 0.041              | —              | —               | —              | 13                    | 3.033   | 2.010 -            | 2.010 -    | 1.002          |                 |                |
| 15                    | 20 | 11.028             | 10.009         | 10.009          | 9.003          | 12                    | 2.020   | 2.020              | 1.005 -    | 1.005 -        |                 |                |
|                       | 19 | 10.040             | 9.016          | 8.006           | 7.002          | 11                    | 2.036   | 1.009              | 1.009      | 0.001          |                 |                |
|                       | 18 | 9.046              | 8.019          | 7.007           | 6.002          | 10                    | 1.018   | 1.018              | 0.003      | 0.003          |                 |                |
|                       | 17 | 8.047              | 7.020          | 6.008           | 5.003          | 9                     | 1.034   | 0.006              | 0.006      | —              |                 |                |
|                       | 16 | 7.045 -            | 6.019          | 5.007           | 4.002          | 8                     | 0.012   | 0.012              | —          | —              |                 |                |
|                       | 15 | 6.040              | 5.017          | 4.006           | 3.002          | 7                     | 0.023   | 0.023              | —          | —              |                 |                |
|                       | 14 | 5.034              | 4.013          | 3.004           | 3.004          | 6                     | 0.042   | —                  | —          | —              |                 |                |

## TABLES

TABLE A-29 (Continued). TABLES FOR TESTING SIGNIFICANCE IN  $2 \times 2$  TABLES WITH UNEQUAL SAMPLES

|          |          | Significance Level |                |                 |                |                 |          | Significance Level |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|----------|----------|--------------------|----------------|-----------------|----------------|-----------------|----------|--------------------|------------|----------------|-----------------|----------------|-----------------|-------|-------|-------|-------|-------|-------|-------|----|-------|-------|---------|---------|-------|--|----|-------|-------|-------|-------|--|----|-------|-------|-------|-------|-------|----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----|-------|-------|-------|-------|---|-------|-------|-------|-------|-------|-------|---|-------|-------|-------|----|-------|-------|---|-------|----|-------|-------|-------|-------|---|---|----|-------|-------|-------|-------|-------|-------|----|-------|-------|-------|-------|
|          |          | $\alpha_1$         | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |          |                    | $\alpha_1$ | 0.05<br>(0.10) | 0.025<br>(0.05) | 0.01<br>(0.02) | 0.005<br>(0.01) |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
| $n_1=20$ | $n_2=11$ | 20                 | 8.027          | 7.010 +         | 6.003          | 6.003           | $n_1=20$ | $n_2=7$            | 20         | 4.012          | 4.012           | 3.002          | 3.002           |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 19                 | 7.042          | 6.012           | 5.004          | 5.004           |          |                    | 19         | 4.042          | 3.009           | 3.009          | 2.001           |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 18                 | 6.027          | 5.012           | 4.003          | 4.003           |          |                    | 18         | 3.024          | 3.024           | 2.006          | 2.006           |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 17                 | 5.029          | 4.009           | 4.009          | 3.002           |          |                    | 17         | 3.080          | 2.011           | 1.002          | 1.002           |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 16                 | 4.021          | 4.021           | 3.008          | 2.001           |          |                    | 16         | 2.022          | 2.022           | 1.004          | 1.004           |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 15                 | 4.042          | 3.014           | 2.003          | 2.003           |          |                    | 15         | 2.042          | 1.009           | 1.009          | 0.001           |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 14                 | 3.028          | 2.008           | 2.008          | 1.001           |          |                    | 14         | 1.018          | 1.018           | 0.002          | 0.002           |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 13                 | 2.016          | 2.016           | 1.003          | 1.003           |          |                    | 13         | 1.029          | 0.004           | 0.004          | 0.004           |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 12                 | 2.029          | 1.007           | 1.007          | 0.001           |          |                    | 12         | 1.048          | 0.007           | 0.007          | —               |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 11                 | 1.014          | 1.014           | 0.002          | 0.002           |          |                    | 11         | 0.012          | 0.012           | —              | —               |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 10                 | 1.026          | 0.004           | 0.004          | 0.004           |          |                    | 10         | 0.022          | 0.022           | —              | —               |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 9                  | 1.046          | 0.008           | 0.008          | —               |          |                    | 9          | 0.036          | —               | —              | —               |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 8                  | 0.016          | 0.016           | —              | —               |          |                    | 6          | 20             | 4.048           | 3.008          | 3.008           | 2.001 |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 7                  | 0.029          | —               | —              | —               |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          | 10       | 20                 | 7.030          | 6.008           | 6.008          | 5.002           |          |                    |            |                |                 |                |                 |       |       | 19    | 3.028 | 2.008 | 2.008 | 2.008 |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 19                 | 6.031          | 5.009           | 5.009          | 4.002           |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    | 18    | 2.012 | 2.012   | 1.002   | 1.002 |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 18                 | 5.026          | 4.007           | 4.007          | 3.002           |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  | 17 | 2.028 | 1.004 | 1.004 | 1.004 |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 17                 | 4.018          | 4.018           | 3.008          | 3.008           |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  | 16 | 1.010 | 1.010 | 1.010 | 0.001 |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 16                 | 4.029          | 3.012           | 2.002          | 2.002           |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       | 15 | 1.018 | 1.018 | 0.002 | 0.002 |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 15                 | 3.024          | 3.024           | 2.006          | 1.001           |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       | 14    | 1.032 | 0.004 | 0.004 | 0.004 |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 14                 | 3.046 +        | 2.013           | 1.002          | 1.002           |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       | 13    | 0.007 | 0.007 | 0.007 | —  |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 13                 | 2.028 +        | 1.006           | 1.006          | 0.001           |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       | 12    | 0.012 | 0.012 | — | —     |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 12                 | 2.046 -        | 1.011           | 0.001          | 0.001           |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       | 11    | 0.022 | 0.022 | —     | — |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 11                 | 1.021          | 1.021           | 0.002          | 0.002           |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       | 10    | 0.036 | —  | —     | —     |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 10                 | 1.027          | 0.006           | 0.006          | —               |          |                    | 5          | 20             | 3.022           | 2.004          | 2.004           | 2.004 |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 9                  | 0.012          | 0.012           | —              | —               |          |                    |            |                |                 |                |                 |       |       | 19    | 2.016 | 2.016 | 1.002 | 1.002 |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 8                  | 0.022          | 0.022           | —              | —               |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    | 18    | 2.028 | 1.008 + | 1.008 + | 0.000 |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 7                  | 0.028          | —               | —              | —               |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  | 17 | 1.012 | 1.012 | 0.001 | 0.001 |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          | 9        | 20                 | 6.022          | 6.022           | 5.006 +        | 4.001           |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    | 16    | 1.022 | 1.022 | 0.002 | 0.002 |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 19                 | 5.022          | 5.022           | 4.006 +        | 3.001           |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       | 15    | 1.040 | 0.008 | 0.008 | 0.008 |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 18                 | 4.016          | 4.016           | 3.004          | 3.004           |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       | 14    | 0.009 | 0.009 | 0.009 | —     |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 17                 | 4.027          | 3.010 +         | 2.002          | 2.002           |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       | 13 | 0.018 | 0.018 | —     | —     |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 16                 | 3.022          | 3.022           | 2.006 +        | 1.001           |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       | 12    | 0.024 | 0.024 | —     | —     |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 15                 | 3.042          | 2.012           | 1.002          | 1.002           |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       | 11    | 0.036 | —  | —     | —     |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 14                 | 2.022          | 2.022           | 1.008          | 1.008           |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       | 20 | 2.022 | 2.022 | 1.002 | 1.002 |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          | 13                 | 2.041          | 1.009           | 1.009          | 0.001           |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   | 19 | 1.008 | 1.008 | 1.008 | 0.000 |       |       |    |       |       |       |       |
|          |          | 12                 | 1.016          | 1.016           | 0.002          | 0.002           |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       | 18 | 1.018 | 1.018 | 0.001 | 0.001 |
|          |          | 11                 | 1.022          | 0.005 -         | 0.005 -        | 0.005 -         |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
| 10       | 0.009    | 0.009              | 0.009          | —               |                |                 | 16       | 0.007              | 0.007      | 0.007          | —               |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
| 9        | 0.017    | 0.017              | —              | —               |                |                 |          |                    |            |                |                 |                |                 | 15    | 0.012 | 0.012 | —     | —     |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
| 8        | 0.029    | —                  | —              | —               |                |                 |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       | 14 | 0.020 | 0.020 | —       | —       |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
| 7        | 0.060 -  | —                  | —              | —               |                |                 |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  | 13 | 0.021 | —     | —     | —     |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       | 8  |       |       | 20    | 5.017 | 5.017 | 4.002 |       | 4.002 |       |       | 12    | 0.047 | —     |       | —     | —  |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       | 19    | 4.018 | 4.018 | 3.002 | 3.002 |       |       |       |       |       |       |       |       |    |       | 20    | 1.012 | 1.012 |   | 0.001 | 0.001 |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       | 18    | 4.028 | 3.009 | 3.009 | 2.002 |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       | 19    | 1.024 | 0.002 |   | 0.002 | 0.002 |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       | 17    | 3.022 | 3.022 | 2.008 | 2.008 |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       | 18 | 0.008 | 0.008 |   | 0.008 | —  |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          |                    |                |                 |                |                 |          |                    |            |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       | 16    | 3.044 | 2.011 | 1.002 | 1.002 |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       | 17    | 0.011 | 0.011 |   | — | —  |       |       |       |       |       |       |    |       |       |       |       |
|          |          |                    |                |                 |                | 15              | 2.022    | 2.022              | 1.004      | 1.004          |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       | 16    | 0.020 | 0.020 | —     |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       | — |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          |                    |                |                 |                | 14              | 2.040    | 1.009              | 1.009      | 0.001          |                 |                |                 |       | 15    | 0.032 | —     | —     |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       | — |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          |                    |                |                 |                | 13              | 1.016    | 1.016              | 0.002      | 0.002          |                 |                |                 |       |       |       |       |       |       |       |    | 14    | 0.047 | —       | —       |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    | —     |       |       |       |       |       |    |       |       |       |       |
|          |          |                    |                |                 |                | 12              | 1.029    | 0.004              | 0.004      | 0.004          |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    | 20    | 0.004 | 0.004 | 0.004 |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       | 0.004 |       |       |       |       |    |       |       |       |       |
|          |          |                    |                |                 | 11             | 1.048           | 0.008    | 0.008              | —          |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       | 19    | 0.012 | 0.012 | —  | —     |       |       |       |
|          |          |                    |                |                 | 10             | 0.014           | 0.014    | —                  | —          |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       | 18    | 0.026 | —     | —     |       | —     |    |       |       |       |       |   |       |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          |                    |                |                 | 9              | 0.024           | 0.024    | —                  | —          |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    | 17    | 0.043 | —     | —     |   | —     |       |       |       |       |       |   |       |       |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |
|          |          |                    |                |                 | 8              | 0.041           | —        | —                  | —          |                |                 |                |                 |       |       |       |       |       |       |       |    |       |       |         |         |       |  |    |       |       |       |       |  |    |       |       |       |       |       |    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |    |       |       |       |       |   |       |       | 1     | 20    | 0.048 | —     |   | —     | —     |       |    |       |       |   |       |    |       |       |       |       |   |   |    |       |       |       |       |       |       |    |       |       |       |       |

## TABLES

TABLE A-30. TABLES FOR DISTRIBUTION-FREE TOLERANCE LIMITS (TWO-SIDED)

Values  $(r, s)$  such that we may assert with confidence at least  $\gamma$  that 100 $\gamma$  percent of a population lies between the  $r^{\text{th}}$  smallest and the  $s^{\text{th}}$  largest of a random sample of  $n$  from that population (no assumption of normality required)

| $n \backslash P$ | $\gamma = 0.75$ |       |       |     | $\gamma = 0.90$ |       |       |     |
|------------------|-----------------|-------|-------|-----|-----------------|-------|-------|-----|
|                  | .75             | .90   | .95   | .99 | .75             | .90   | .95   | .99 |
| 50               | 5,5             | 2,1   | —     | —   | 5,4             | 1,1   | —     | —   |
| 55               | 6,6             | 2,2   | 1,1   | —   | 5,5             | 2,1   | —     | —   |
| 60               | 7,6             | 2,2   | 1,1   | —   | 6,5             | 2,1   | —     | —   |
| 65               | 7,7             | 3,2   | 1,1   | —   | 6,6             | 2,2   | —     | —   |
| 70               | 8,7             | 3,2   | 1,1   | —   | 7,6             | 2,2   | —     | —   |
| 75               | 8,8             | 3,3   | 1,1   | —   | 7,7             | 2,2   | —     | —   |
| 80               | 9,8             | 3,3   | 2,1   | —   | 8,7             | 3,2   | 1,1   | —   |
| 85               | 10,9            | 4,3   | 2,1   | —   | 8,8             | 3,2   | 1,1   | —   |
| 90               | 10,10           | 4,3   | 2,1   | —   | 9,8             | 3,2   | 1,1   | —   |
| 95               | 11,10           | 4,3   | 2,1   | —   | 9,9             | 3,3   | 1,1   | —   |
| 100              | 11,11           | 4,4   | 2,1   | —   | 10,10           | 3,3   | 1,1   | —   |
| 110              | 12,12           | 5,4   | 2,2   | —   | 11,11           | 4,3   | 2,1   | —   |
| 120              | 14,13           | 5,5   | 2,2   | —   | 12,12           | 4,4   | 2,1   | —   |
| 130              | 15,14           | 6,5   | 3,2   | —   | 13,13           | 5,4   | 2,1   | —   |
| 140              | 16,15           | 6,6   | 3,2   | —   | 14,14           | 5,5   | 2,2   | —   |
| 150              | 17,17           | 6,6   | 3,3   | —   | 16,15           | 5,5   | 2,2   | —   |
| 170              | 20,19           | 7,7   | 4,3   | —   | 18,17           | 6,6   | 3,2   | —   |
| 200              | 23,23           | 9,8   | 4,4   | —   | 21,21           | 8,7   | 3,3   | —   |
| 300              | 35,35           | 13,13 | 6,6   | 1,1 | 33,32           | 12,11 | 5,5   | —   |
| 400              | 47,47           | 18,18 | 9,8   | 2,1 | 45,44           | 16,16 | 8,7   | 1,1 |
| 500              | 59,59           | 23,22 | 11,11 | 2,1 | 57,56           | 21,20 | 10,9  | 1,1 |
| 600              | 72,71           | 28,27 | 13,13 | 2,2 | 68,68           | 26,25 | 12,11 | 2,1 |
| 700              | 84,83           | 33,32 | 16,15 | 3,2 | 80,80           | 30,30 | 14,14 | 2,2 |
| 800              | 96,96           | 37,37 | 18,18 | 3,3 | 92,92           | 35,34 | 16,16 | 3,2 |
| 900              | 108,108         | 42,42 | 21,20 | 4,3 | 104,104         | 40,39 | 19,18 | 3,2 |
| 1000             | 121,120         | 47,47 | 23,22 | 4,4 | 117,116         | 44,44 | 21,20 | 3,3 |

| $n \backslash P$ | $\gamma = 0.95$ |       |       |     | $\gamma = 0.99$ |       |       |     |
|------------------|-----------------|-------|-------|-----|-----------------|-------|-------|-----|
|                  | .75             | .90   | .95   | .99 | .75             | .90   | .95   | .99 |
| 50               | 4,4             | 1,1   | —     | —   | 3,3             | —     | —     | —   |
| 55               | 5,4             | 1,1   | —     | —   | 4,3             | —     | —     | —   |
| 60               | 5,5             | 1,1   | —     | —   | 4,4             | —     | —     | —   |
| 65               | 6,5             | 2,1   | —     | —   | 5,4             | 1,1   | —     | —   |
| 70               | 6,6             | 2,1   | —     | —   | 5,5             | 1,1   | —     | —   |
| 75               | 7,6             | 2,1   | —     | —   | 5,5             | 1,1   | —     | —   |
| 80               | 7,7             | 2,2   | —     | —   | 6,5             | 1,1   | —     | —   |
| 85               | 8,7             | 2,2   | —     | —   | 6,6             | 2,1   | —     | —   |
| 90               | 8,8             | 3,2   | —     | —   | 7,6             | 2,1   | —     | —   |
| 95               | 9,8             | 3,2   | 1,1   | —   | 7,7             | 2,1   | —     | —   |
| 100              | 9,9             | 3,2   | 1,1   | —   | 8,7             | 2,2   | —     | —   |
| 110              | 10,10           | 3,3   | 1,1   | —   | 9,8             | 2,2   | —     | —   |
| 120              | 11,11           | 4,3   | 1,1   | —   | 10,9            | 3,2   | —     | —   |
| 130              | 13,12           | 4,4   | 2,1   | —   | 11,10           | 3,3   | 1,1   | —   |
| 140              | 14,13           | 4,4   | 2,1   | —   | 12,11           | 3,3   | 1,1   | —   |
| 150              | 15,14           | 5,4   | 2,1   | —   | 13,13           | 4,3   | 1,1   | —   |
| 170              | 17,16           | 6,5   | 2,2   | —   | 15,15           | 5,4   | 2,1   | —   |
| 200              | 20,20           | 7,6   | 3,2   | —   | 18,18           | 6,5   | 2,2   | —   |
| 300              | 32,31           | 11,11 | 5,4   | —   | 29,29           | 10,9  | 4,3   | —   |
| 400              | 43,43           | 15,15 | 7,6   | —   | 40,40           | 14,13 | 6,5   | —   |
| 500              | 55,54           | 20,19 | 9,8   | 1,1 | 52,51           | 18,17 | 7,7   | —   |
| 600              | 67,66           | 24,24 | 11,10 | 1,1 | 63,63           | 22,22 | 9,9   | —   |
| 700              | 78,78           | 29,28 | 13,13 | 2,1 | 75,74           | 26,26 | 11,11 | 1,1 |
| 800              | 90,90           | 33,33 | 15,15 | 2,2 | 86,86           | 31,30 | 13,13 | 1,1 |
| 900              | 102,102         | 38,37 | 18,17 | 2,2 | 98,97           | 35,35 | 15,15 | 2,1 |
| 1000             | 114,114         | 43,42 | 20,19 | 3,2 | 110,109         | 40,39 | 18,17 | 2,1 |

When the values of  $r$  and  $s$  given in the table are not equal, they are interchangeable; i.e., for  $n = 120$  with confidence at least 0.75 we may assert that 75% of the population lies between the 14th smallest and the 13th largest values, or between the 13th smallest and the 14th largest values.

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## TABLES

TABLE A-31. TABLES FOR DISTRIBUTION-FREE TOLERANCE LIMITS (ONE-SIDED)

Largest values of  $m$  such that we may assert with confidence at least  $\gamma$  that 100P percent of a population lies below the  $m^{\text{th}}$  largest (or above the  $m^{\text{th}}$  smallest) of a random sample of  $n$  from that population (no assumption of normality required)

| n \ P | $\gamma = 0.75$ |     |     |     | $\gamma = 0.90$ |     |     |     | $\gamma = 0.95$ |     |     |     | $\gamma = 0.99$ |     |     |     |
|-------|-----------------|-----|-----|-----|-----------------|-----|-----|-----|-----------------|-----|-----|-----|-----------------|-----|-----|-----|
|       | .75             | .90 | .95 | .99 | .75             | .90 | .95 | .99 | .75             | .90 | .95 | .99 | .75             | .90 | .95 | .99 |
| 50    | 10              | 3   | 1   | —   | 9               | 2   | 1   | —   | 8               | 2   | —   | —   | 6               | 1   | —   | —   |
| 55    | 12              | 4   | 2   | —   | 10              | 3   | 1   | —   | 9               | 2   | —   | —   | 7               | 1   | —   | —   |
| 60    | 13              | 4   | 2   | —   | 11              | 3   | 1   | —   | 10              | 2   | 1   | —   | 8               | 1   | —   | —   |
| 65    | 14              | 5   | 2   | —   | 12              | 4   | 1   | —   | 11              | 3   | 1   | —   | 9               | 2   | —   | —   |
| 70    | 15              | 5   | 2   | —   | 13              | 4   | 1   | —   | 12              | 3   | 1   | —   | 10              | 2   | —   | —   |
| 75    | 16              | 6   | 2   | —   | 14              | 4   | 1   | —   | 13              | 3   | 1   | —   | 10              | 2   | —   | —   |
| 80    | 17              | 6   | 3   | —   | 15              | 5   | 2   | —   | 14              | 4   | 1   | —   | 11              | 2   | —   | —   |
| 85    | 19              | 7   | 3   | —   | 16              | 5   | 2   | —   | 15              | 4   | 1   | —   | 12              | 3   | —   | —   |
| 90    | 20              | 7   | 3   | —   | 17              | 5   | 2   | —   | 16              | 5   | 1   | —   | 13              | 3   | 1   | —   |
| 95    | 21              | 7   | 3   | —   | 18              | 6   | 2   | —   | 17              | 5   | 2   | —   | 14              | 3   | 1   | —   |
| 100   | 22              | 8   | 3   | —   | 20              | 6   | 2   | —   | 18              | 5   | 2   | —   | 15              | 4   | 1   | —   |
| 110   | 24              | 9   | 4   | —   | 22              | 7   | 3   | —   | 20              | 6   | 2   | —   | 17              | 4   | 1   | —   |
| 120   | 27              | 10  | 4   | —   | 24              | 8   | 3   | —   | 22              | 7   | 2   | —   | 19              | 5   | 1   | —   |
| 130   | 29              | 11  | 5   | —   | 26              | 9   | 3   | —   | 25              | 8   | 3   | —   | 21              | 6   | 2   | —   |
| 140   | 31              | 12  | 5   | 1   | 28              | 10  | 4   | —   | 27              | 8   | 3   | —   | 23              | 6   | 2   | —   |
| 150   | 34              | 12  | 6   | 1   | 31              | 10  | 4   | —   | 29              | 9   | 3   | —   | 26              | 7   | 2   | —   |
| 170   | 39              | 14  | 7   | 1   | 35              | 12  | 5   | —   | 33              | 11  | 4   | —   | 30              | 9   | 3   | —   |
| 200   | 46              | 17  | 8   | 1   | 42              | 15  | 6   | —   | 40              | 13  | 5   | —   | 36              | 11  | 4   | —   |
| 300   | 70              | 26  | 12  | 2   | 65              | 23  | 10  | 1   | 63              | 22  | 9   | 1   | 58              | 19  | 7   | —   |
| 400   | 94              | 36  | 17  | 3   | 89              | 32  | 15  | 2   | 86              | 30  | 13  | 1   | 80              | 27  | 11  | —   |
| 500   | 118             | 45  | 22  | 3   | 118             | 41  | 19  | 2   | 109             | 39  | 17  | 2   | 103             | 35  | 14  | 1   |
| 600   | 143             | 55  | 28  | 4   | 136             | 51  | 23  | 3   | 133             | 48  | 21  | 2   | 126             | 44  | 18  | 1   |
| 700   | 167             | 65  | 31  | 5   | 160             | 60  | 28  | 4   | 156             | 57  | 26  | 3   | 149             | 52  | 22  | 2   |
| 800   | 192             | 74  | 36  | 6   | 184             | 69  | 32  | 5   | 180             | 66  | 30  | 4   | 172             | 61  | 26  | 2   |
| 900   | 216             | 84  | 41  | 7   | 208             | 79  | 37  | 5   | 204             | 75  | 35  | 4   | 195             | 70  | 30  | 3   |
| 1000  | 241             | 94  | 45  | 8   | 233             | 88  | 41  | 6   | 228             | 85  | 39  | 5   | 219             | 79  | 35  | 3   |

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## TABLES

**TABLE A-32. CONFIDENCE ASSOCIATED WITH A TOLERANCE LIMIT STATEMENT**  
 Confidence  $\gamma$  with which we may assert that 100P percent of the population lies between  
 the largest and smallest of a random sample of  $n$  from that population  
 (continuous distribution assumed)

| $n$ | $P = .75$ | $P = .90$ | $P = .95$ | $P = .99$ |
|-----|-----------|-----------|-----------|-----------|
| 3   | .16       | .03       | .01       | .00       |
| 4   | .26       | .05       | .01       | .00       |
| 5   | .37       | .08       | .02       | .00       |
| 6   | .47       | .11       | .03       | .00       |
| 7   | .56       | .15       | .04       | .00       |
| 8   | .63       | .19       | .06       | .00       |
| 9   | .70       | .23       | .07       | .00       |
| 10  | .76       | .26       | .09       | .00       |
| 11  | .80       | .30       | .10       | .01       |
| 12  | .84       | .34       | .12       | .01       |
| 13  | .87       | .38       | .14       | .01       |
| 14  | .90       | .42       | .15       | .01       |
| 15  | .92       | .45       | .17       | .01       |
| 16  | .94       | .49       | .19       | .01       |
| 17  | .95       | .52       | .21       | .01       |
| 18  | .96       | .55       | .23       | .01       |
| 19  | .97       | .58       | .25       | .02       |
| 20  | .98       | .61       | .26       | .02       |
| 25  | .99       | .73       | .36       | .03       |
| 30  | 1.00 —    | .82       | .45       | .04       |
| 40  | —         | .92       | .60       | .06       |
| 50  | —         | .97       | .72       | .09       |
| 60  | —         | .99       | .81       | .12       |
| 70  | —         | .99       | .87       | .16       |
| 80  | —         | 1.00 —    | .91       | .19       |
| 90  | —         | —         | .94       | .23       |
| 100 | —         | —         | .96       | .26       |

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## TABLES

TABLE A-33. CRITICAL VALUES OF  $r$  FOR THE SIGN TEST

| n  | $\alpha$ for Two-Sided Test |      |     |      | n  | $\alpha$ for Two-Sided Test |      |     |      |
|----|-----------------------------|------|-----|------|----|-----------------------------|------|-----|------|
|    | .01                         | .05  | .10 | .25  |    | .01                         | .05  | .10 | .25  |
|    | $\alpha$ for One-Sided Test |      |     |      |    | $\alpha$ for One-Sided Test |      |     |      |
|    | .005                        | .025 | .05 | .125 |    | .005                        | .025 | .05 | .125 |
| 1  | —                           | —    | —   | —    | 46 | 13                          | 15   | 16  | 18   |
| 2  | —                           | —    | —   | —    | 47 | 14                          | 16   | 17  | 19   |
| 3  | —                           | —    | —   | 0    | 48 | 14                          | 16   | 17  | 19   |
| 4  | —                           | —    | —   | 0    | 49 | 15                          | 17   | 18  | 19   |
| 5  | —                           | —    | 0   | 0    | 50 | 15                          | 17   | 18  | 20   |
| 6  | —                           | 0    | 0   | 1    | 51 | 15                          | 18   | 19  | 20   |
| 7  | —                           | 0    | 0   | 1    | 52 | 16                          | 18   | 19  | 21   |
| 8  | 0                           | 0    | 1   | 1    | 53 | 16                          | 18   | 20  | 21   |
| 9  | 0                           | 1    | 1   | 2    | 54 | 17                          | 19   | 20  | 22   |
| 10 | 0                           | 1    | 1   | 2    | 55 | 17                          | 19   | 20  | 22   |
| 11 | 0                           | 1    | 2   | 3    | 56 | 17                          | 20   | 21  | 23   |
| 12 | 1                           | 2    | 2   | 3    | 57 | 18                          | 20   | 21  | 23   |
| 13 | 1                           | 2    | 3   | 3    | 58 | 18                          | 21   | 22  | 24   |
| 14 | 1                           | 2    | 3   | 4    | 59 | 19                          | 21   | 22  | 24   |
| 15 | 2                           | 3    | 3   | 4    | 60 | 19                          | 21   | 23  | 25   |
| 16 | 2                           | 3    | 4   | 5    | 61 | 20                          | 22   | 23  | 25   |
| 17 | 2                           | 4    | 4   | 5    | 62 | 20                          | 22   | 24  | 25   |
| 18 | 3                           | 4    | 5   | 6    | 63 | 20                          | 23   | 24  | 26   |
| 19 | 3                           | 4    | 5   | 6    | 64 | 21                          | 23   | 24  | 26   |
| 20 | 3                           | 5    | 5   | 6    | 65 | 21                          | 24   | 25  | 27   |
| 21 | 4                           | 5    | 6   | 7    | 66 | 22                          | 24   | 25  | 27   |
| 22 | 4                           | 5    | 6   | 7    | 67 | 22                          | 25   | 26  | 28   |
| 23 | 4                           | 6    | 7   | 8    | 68 | 22                          | 25   | 26  | 28   |
| 24 | 5                           | 6    | 7   | 8    | 69 | 23                          | 25   | 27  | 29   |
| 25 | 5                           | 7    | 7   | 9    | 70 | 23                          | 26   | 27  | 29   |
| 26 | 6                           | 7    | 8   | 9    | 71 | 24                          | 26   | 28  | 30   |
| 27 | 6                           | 7    | 8   | 10   | 72 | 24                          | 27   | 28  | 30   |
| 28 | 6                           | 8    | 9   | 10   | 73 | 25                          | 27   | 28  | 31   |
| 29 | 7                           | 8    | 9   | 10   | 74 | 25                          | 28   | 29  | 31   |
| 30 | 7                           | 9    | 10  | 11   | 75 | 25                          | 28   | 29  | 32   |
| 31 | 7                           | 9    | 10  | 11   | 76 | 26                          | 28   | 30  | 32   |
| 32 | 8                           | 9    | 10  | 12   | 77 | 26                          | 29   | 30  | 32   |
| 33 | 8                           | 10   | 11  | 12   | 78 | 27                          | 29   | 31  | 33   |
| 34 | 9                           | 10   | 11  | 13   | 79 | 27                          | 30   | 31  | 33   |
| 35 | 9                           | 11   | 12  | 13   | 80 | 28                          | 30   | 32  | 34   |
| 36 | 9                           | 11   | 12  | 14   | 81 | 28                          | 31   | 32  | 34   |
| 37 | 10                          | 12   | 13  | 14   | 82 | 28                          | 31   | 33  | 35   |
| 38 | 10                          | 12   | 13  | 14   | 83 | 29                          | 32   | 33  | 35   |
| 39 | 11                          | 12   | 13  | 15   | 84 | 29                          | 32   | 33  | 36   |
| 40 | 11                          | 13   | 14  | 15   | 85 | 30                          | 32   | 34  | 36   |
| 41 | 11                          | 13   | 14  | 16   | 86 | 30                          | 33   | 34  | 37   |
| 42 | 12                          | 14   | 15  | 16   | 87 | 31                          | 33   | 35  | 37   |
| 43 | 12                          | 14   | 15  | 17   | 88 | 31                          | 34   | 35  | 38   |
| 44 | 13                          | 15   | 16  | 17   | 89 | 31                          | 34   | 36  | 38   |
| 45 | 13                          | 15   | 16  | 18   | 90 | 32                          | 35   | 36  | 39   |

For values of  $n$  larger than 90, approximate values of  $r$  may be found by taking the nearest integer less than  $(n-1)/2 - k\sqrt{n+1}$ , where  $k$  is 1.2879, 0.9800, 0.8224, 0.5752 for the 1, 5, 10, 25% values, respectively.

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## TABLES

TABLE A-34. CRITICAL VALUES OF  $T_{\alpha}(n)$  FOR THE WILCOXON SIGNED-RANKS TEST

$T_{\alpha}$  is the integer such that the probability that  $T \leq T_{\alpha}$  is closest to  $\alpha$ . For example, for  $n = 8$ ,  $\Pr\{T \leq 3\} = .020$  and  $\Pr\{T \leq 4\} = .027$ ; hence we list  $T_{.025}(8) = 4$ .

| n  | $\alpha$ for One-Sided Test |     |      |
|----|-----------------------------|-----|------|
|    | .025                        | .01 | .005 |
|    | $\alpha$ for Two-Sided Test |     |      |
|    | .05                         | .02 | .01  |
| 6  | 0                           | —   | —    |
| 7  | 2                           | 0   | —    |
| 8  | 4                           | 2   | 0    |
| 9  | 6                           | 3   | 2    |
| 10 | 8                           | 5   | 3    |
| 11 | 11                          | 7   | 5    |
| 12 | 14                          | 10  | 7    |
| 13 | 17                          | 13  | 10   |
| 14 | 21                          | 16  | 13   |
| 15 | 25                          | 20  | 16   |
| 16 | 30                          | 24  | 20   |
| 17 | 35                          | 28  | 23   |
| 18 | 40                          | 33  | 28   |
| 19 | 46                          | 38  | 32   |
| 20 | 52                          | 43  | 38   |
| 21 | 59                          | 49  | 43   |
| 22 | 66                          | 56  | 49   |
| 23 | 78                          | 62  | 55   |
| 24 | 81                          | 69  | 61   |
| 25 | 89                          | 77  | 68   |

For large  $n$ ,

$$T_P(n) = \frac{n(n+1)}{4} - z_{1-P} \sqrt{\frac{n(n+1)(2n+1)}{24}} \text{ approximately}$$

where  $z$  is given in Table A-2.

Adapted with permission from *Some Rapid Approximate Statistical Procedures* by F. Wilcoxon, 1949, American Cyanamid Company.



TABLE A-35. CRITICAL VALUES OF SMALLER RANK SUM FOR THE WILCOXON-MANN-WHITNEY TEST

| $n_2$ | $\alpha$ for 2-Sided Test | $\alpha$ for 1-Sided Test | $n_1$ (Smaller Sample) |   |    |    |    |    |    |    |    |    |     |     |    |    |    |    |
|-------|---------------------------|---------------------------|------------------------|---|----|----|----|----|----|----|----|----|-----|-----|----|----|----|----|
|       |                           |                           | 1                      | 2 | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11  | 12  | 13 | 14 | 15 | 16 |
| 3     | .20                       | .10                       |                        | 3 | 7  |    |    |    |    |    |    |    |     |     |    |    |    |    |
|       | .10                       | .05                       |                        |   | 6  |    |    |    |    |    |    |    |     |     |    |    |    |    |
|       | .05                       | .025                      |                        |   |    |    |    |    |    |    |    |    |     |     |    |    |    |    |
|       | .01                       | .005                      |                        |   |    |    |    |    |    |    |    |    |     |     |    |    |    |    |
| 4     | .20                       | .10                       |                        | 3 | 7  | 13 |    |    |    |    |    |    |     |     |    |    |    |    |
|       | .10                       | .05                       |                        |   | 6  | 11 |    |    |    |    |    |    |     |     |    |    |    |    |
|       | .05                       | .025                      |                        |   |    | 10 |    |    |    |    |    |    |     |     |    |    |    |    |
|       | .01                       | .005                      |                        |   |    |    |    |    |    |    |    |    |     |     |    |    |    |    |
| 5     | .20                       | .10                       |                        | 4 | 8  | 14 | 20 |    |    |    |    |    |     |     |    |    |    |    |
|       | .10                       | .05                       |                        | 3 | 7  | 12 | 19 |    |    |    |    |    |     |     |    |    |    |    |
|       | .05                       | .025                      |                        |   | 6  | 11 | 17 |    |    |    |    |    |     |     |    |    |    |    |
|       | .01                       | .005                      |                        |   |    |    | 15 |    |    |    |    |    |     |     |    |    |    |    |
| 6     | .20                       | .10                       |                        | 4 | 9  | 15 | 22 | 30 |    |    |    |    |     |     |    |    |    |    |
|       | .10                       | .05                       |                        | 3 | 8  | 13 | 20 | 28 |    |    |    |    |     |     |    |    |    |    |
|       | .05                       | .025                      |                        |   | 7  | 12 | 18 | 26 |    |    |    |    |     |     |    |    |    |    |
|       | .01                       | .005                      |                        |   |    | 10 | 16 | 23 |    |    |    |    |     |     |    |    |    |    |
| 7     | .20                       | .10                       |                        | 4 | 10 | 16 | 23 | 32 | 41 |    |    |    |     |     |    |    |    |    |
|       | .10                       | .05                       |                        | 3 | 8  | 14 | 21 | 29 | 39 |    |    |    |     |     |    |    |    |    |
|       | .05                       | .025                      |                        |   | 7  | 13 | 20 | 27 | 36 |    |    |    |     |     |    |    |    |    |
|       | .01                       | .005                      |                        |   |    | 10 | 16 | 24 | 32 |    |    |    |     |     |    |    |    |    |
| 8     | .20                       | .10                       |                        | 5 | 11 | 17 | 25 | 34 | 44 | 55 |    |    |     |     |    |    |    |    |
|       | .10                       | .05                       |                        | 4 | 9  | 15 | 23 | 31 | 41 | 51 |    |    |     |     |    |    |    |    |
|       | .05                       | .025                      |                        | 3 | 8  | 14 | 21 | 29 | 38 | 49 |    |    |     |     |    |    |    |    |
|       | .01                       | .005                      |                        |   | 7  | 11 | 17 | 25 | 34 | 43 |    |    |     |     |    |    |    |    |
| 9     | .20                       | .10                       |                        | 5 | 11 | 19 | 27 | 36 | 46 | 58 | 70 |    |     |     |    |    |    |    |
|       | .10                       | .05                       | 1                      | 4 | 9  | 16 | 24 | 33 | 43 | 54 | 66 |    |     |     |    |    |    |    |
|       | .05                       | .025                      |                        | 3 | 8  | 14 | 22 | 31 | 40 | 51 | 62 |    |     |     |    |    |    |    |
|       | .01                       | .005                      |                        |   | 7  | 11 | 18 | 26 | 35 | 45 | 56 |    |     |     |    |    |    |    |
| 10    | .20                       | .10                       |                        | 6 | 12 | 20 | 28 | 38 | 49 | 60 | 73 | 87 |     |     |    |    |    |    |
|       | .10                       | .05                       | 1                      | 4 | 10 | 17 | 26 | 35 | 45 | 56 | 69 | 82 |     |     |    |    |    |    |
|       | .05                       | .025                      |                        | 3 | 9  | 15 | 23 | 32 | 42 | 53 | 65 | 78 |     |     |    |    |    |    |
|       | .01                       | .005                      |                        |   | 8  | 12 | 19 | 27 | 37 | 47 | 58 | 71 |     |     |    |    |    |    |
| 11    | .20                       | .10                       |                        | 6 | 13 | 21 | 30 | 40 | 51 | 63 | 76 | 91 | 106 |     |    |    |    |    |
|       | .10                       | .05                       | 1                      | 4 | 11 | 18 | 27 | 37 | 47 | 59 | 72 | 86 | 100 |     |    |    |    |    |
|       | .05                       | .025                      |                        | 3 | 9  | 16 | 24 | 34 | 44 | 55 | 68 | 81 | 96  |     |    |    |    |    |
|       | .01                       | .005                      |                        |   | 8  | 12 | 20 | 28 | 38 | 49 | 61 | 73 | 87  |     |    |    |    |    |
| 12    | .20                       | .10                       |                        | 7 | 14 | 22 | 32 | 42 | 54 | 66 | 80 | 94 | 110 | 127 |    |    |    |    |
|       | .10                       | .05                       | 1                      | 5 | 11 | 19 | 28 | 38 | 49 | 62 | 75 | 89 | 104 | 120 |    |    |    |    |
|       | .05                       | .025                      |                        | 4 | 10 | 17 | 26 | 35 | 46 | 58 | 71 | 84 | 99  | 115 |    |    |    |    |
|       | .01                       | .005                      |                        |   | 9  | 13 | 21 | 30 | 40 | 51 | 63 | 76 | 90  | 105 |    |    |    |    |

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## TABLES

[illegible]

For larger values of  $n$ , and  $n$ , critical values are given to a good approximation by the formula:

$$\frac{n_1}{2}(n_1 + n_2 + 1) - z \left\{ \frac{n_1 n_2 (n_1 + n_2 + 1)}{12} \right\}^{\frac{1}{2}}$$

where  $z = 1.28$  for  $\alpha = .20$  (two-sided test)

$$z = 1.64 \text{ for } \alpha = .10$$
$$z = 1.96 \text{ for } \alpha = .05$$
 $z = 2.58$  for  $\alpha = .01$

## TABLES

TABLE A-36. SHORT TABLE OF RANDOM NUMBERS

|    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 46 | 96 | 85 | 77 | 27 | 92 | 86 | 26 | 45 | 21 | 89 | 91 | 71 | 42 | 64 | 64 | 58 | 22 | 75 | 81 | 74 | 91 | 48 | 46 | 18 |
| 44 | 19 | 15 | 32 | 63 | 55 | 87 | 77 | 33 | 29 | 45 | 00 | 31 | 34 | 84 | 05 | 72 | 90 | 44 | 27 | 78 | 22 | 07 | 62 | 17 |
| 34 | 39 | 80 | 62 | 24 | 33 | 81 | 67 | 28 | 11 | 34 | 79 | 26 | 35 | 34 | 23 | 09 | 94 | 00 | 80 | 55 | 31 | 63 | 27 | 91 |
| 74 | 97 | 80 | 30 | 65 | 07 | 71 | 30 | 01 | 84 | 47 | 45 | 89 | 70 | 74 | 13 | 04 | 90 | 51 | 27 | 61 | 34 | 63 | 87 | 44 |
| 22 | 14 | 61 | 60 | 86 | 38 | 33 | 71 | 18 | 33 | 72 | 08 | 16 | 13 | 50 | 56 | 48 | 51 | 29 | 48 | 30 | 93 | 45 | 66 | 29 |
| 40 | 03 | 96 | 40 | 03 | 47 | 24 | 60 | 09 | 21 | 21 | 18 | 00 | 05 | 86 | 52 | 85 | 40 | 73 | 73 | 57 | 68 | 36 | 33 | 91 |
| 52 | 33 | 76 | 44 | 56 | 15 | 47 | 75 | 78 | 73 | 78 | 19 | 87 | 06 | 98 | 47 | 48 | 02 | 62 | 03 | 42 | 05 | 32 | 55 | 02 |
| 87 | 59 | 20 | 40 | 93 | 17 | 82 | 24 | 19 | 90 | 80 | 87 | 32 | 74 | 59 | 84 | 24 | 49 | 79 | 17 | 23 | 75 | 83 | 42 | 00 |
| 11 | 02 | 55 | 67 | 48 | 84 | 74 | 36 | 22 | 67 | 19 | 20 | 15 | 92 | 58 | 37 | 13 | 75 | 54 | 89 | 56 | 73 | 23 | 39 | 07 |
| 10 | 33 | 79 | 26 | 34 | 54 | 71 | 33 | 89 | 74 | 68 | 48 | 23 | 17 | 49 | 18 | 81 | 05 | 52 | 85 | 70 | 05 | 73 | 11 | 17 |
| 67 | 59 | 28 | 25 | 47 | 89 | 11 | 65 | 65 | 20 | 42 | 23 | 96 | 41 | 64 | 20 | 30 | 89 | 87 | 64 | 37 | 93 | 36 | 96 | 35 |
| 98 | 50 | 75 | 20 | 09 | 18 | 54 | 34 | 68 | 02 | 54 | 87 | 23 | 05 | 43 | 36 | 98 | 29 | 97 | 93 | 87 | 08 | 30 | 92 | 98 |
| 24 | 43 | 23 | 72 | 80 | 64 | 34 | 27 | 23 | 46 | 15 | 36 | 10 | 63 | 21 | 59 | 69 | 76 | 02 | 62 | 31 | 62 | 47 | 60 | 34 |
| 39 | 91 | 63 | 18 | 38 | 27 | 10 | 78 | 88 | 84 | 42 | 32 | 00 | 97 | 92 | 00 | 04 | 94 | 50 | 05 | 75 | 82 | 70 | 80 | 35 |
| 74 | 62 | 19 | 67 | 54 | 18 | 28 | 92 | 33 | 69 | 98 | 96 | 74 | 35 | 72 | 11 | 68 | 25 | 08 | 95 | 31 | 79 | 11 | 79 | 54 |
| 91 | 03 | 35 | 60 | 81 | 16 | 61 | 97 | 25 | 14 | 78 | 21 | 22 | 05 | 25 | 47 | 26 | 37 | 80 | 39 | 19 | 06 | 41 | 02 | 00 |
| 42 | 57 | 66 | 76 | 72 | 91 | 03 | 63 | 48 | 46 | 44 | 01 | 33 | 53 | 62 | 28 | 80 | 59 | 55 | 05 | 02 | 16 | 13 | 17 | 54 |
| 06 | 36 | 63 | 06 | 15 | 03 | 72 | 38 | 01 | 58 | 25 | 37 | 66 | 48 | 56 | 19 | 56 | 41 | 29 | 28 | 76 | 49 | 74 | 39 | 50 |
| 92 | 70 | 96 | 70 | 89 | 80 | 87 | 14 | 25 | 49 | 25 | 94 | 62 | 78 | 26 | 15 | 41 | 39 | 48 | 75 | 64 | 69 | 61 | 06 | 38 |
| 91 | 08 | 88 | 53 | 52 | 13 | 04 | 82 | 23 | 00 | 26 | 36 | 47 | 44 | 04 | 08 | 84 | 80 | 07 | 44 | 76 | 51 | 52 | 41 | 59 |
| 68 | 85 | 97 | 74 | 47 | 53 | 90 | 05 | 90 | 84 | 87 | 48 | 25 | 01 | 11 | 05 | 45 | 11 | 43 | 15 | 60 | 40 | 31 | 84 | 59 |
| 59 | 54 | 13 | 09 | 13 | 80 | 42 | 29 | 63 | 03 | 24 | 64 | 12 | 43 | 28 | 10 | 01 | 65 | 62 | 07 | 79 | 83 | 05 | 59 | 61 |
| 39 | 18 | 32 | 69 | 33 | 46 | 58 | 19 | 34 | 03 | 59 | 28 | 97 | 31 | 02 | 65 | 47 | 47 | 70 | 39 | 74 | 17 | 30 | 22 | 65 |
| 67 | 43 | 31 | 09 | 12 | 60 | 19 | 57 | 63 | 78 | 11 | 80 | 10 | 97 | 15 | 70 | 04 | 89 | 81 | 78 | 54 | 84 | 87 | 83 | 42 |
| 61 | 75 | 37 | 19 | 56 | 90 | 75 | 39 | 03 | 56 | 49 | 92 | 72 | 95 | 27 | 52 | 87 | 47 | 12 | 52 | 54 | 62 | 43 | 23 | 13 |
| 78 | 10 | 91 | 11 | 00 | 63 | 19 | 63 | 74 | 58 | 69 | 03 | 51 | 38 | 60 | 36 | 53 | 56 | 77 | 06 | 69 | 03 | 89 | 91 | 24 |
| 93 | 23 | 71 | 58 | 09 | 78 | 08 | 03 | 07 | 71 | 79 | 32 | 25 | 19 | 61 | 04 | 40 | 33 | 12 | 06 | 78 | 91 | 97 | 88 | 95 |
| 37 | 55 | 48 | 82 | 63 | 89 | 92 | 59 | 14 | 72 | 19 | 17 | 22 | 51 | 90 | 20 | 03 | 64 | 96 | 60 | 48 | 01 | 95 | 44 | 84 |
| 62 | 13 | 11 | 71 | 17 | 23 | 29 | 25 | 13 | 85 | 33 | 35 | 07 | 69 | 25 | 68 | 57 | 92 | 57 | 11 | 84 | 44 | 01 | 33 | 66 |
| 29 | 89 | 97 | 47 | 08 | 13 | 20 | 86 | 22 | 45 | 59 | 98 | 64 | 53 | 89 | 64 | 94 | 81 | 55 | 87 | 73 | 81 | 58 | 46 | 42 |
| 16 | 94 | 85 | 82 | 89 | 07 | 17 | 30 | 29 | 89 | 89 | 80 | 98 | 36 | 25 | 36 | 53 | 02 | 49 | 14 | 34 | 03 | 52 | 09 | 20 |
| 04 | 93 | 10 | 59 | 75 | 12 | 98 | 84 | 60 | 93 | 68 | 16 | 87 | 60 | 11 | 50 | 46 | 56 | 58 | 45 | 88 | 72 | 50 | 46 | 11 |
| 95 | 71 | 43 | 68 | 97 | 18 | 85 | 17 | 18 | 08 | 00 | 50 | 77 | 50 | 46 | 92 | 45 | 26 | 97 | 21 | 48 | 22 | 23 | 08 | 32 |
| 86 | 05 | 39 | 14 | 35 | 48 | 68 | 18 | 36 | 57 | 09 | 62 | 40 | 28 | 87 | 08 | 74 | 79 | 91 | 08 | 27 | 12 | 43 | 32 | 03 |
| 59 | 30 | 60 | 10 | 41 | 31 | 00 | 69 | 63 | 77 | 01 | 89 | 94 | 60 | 19 | 02 | 70 | 88 | 72 | 33 | 38 | 88 | 20 | 60 | 86 |
| 05 | 45 | 35 | 40 | 54 | 03 | 98 | 96 | 76 | 27 | 77 | 84 | 80 | 08 | 64 | 60 | 44 | 34 | 54 | 24 | 85 | 20 | 85 | 77 | 32 |
| 71 | 85 | 17 | 74 | 66 | 27 | 85 | 19 | 55 | 56 | 51 | 36 | 48 | 92 | 32 | 44 | 40 | 47 | 10 | 38 | 22 | 52 | 42 | 29 | 96 |
| 80 | 20 | 32 | 80 | 98 | 00 | 40 | 92 | 57 | 51 | 52 | 83 | 14 | 55 | 31 | 99 | 73 | 23 | 40 | 07 | 64 | 54 | 44 | 99 | 21 |
| 13 | 50 | 78 | 02 | 73 | 39 | 66 | 82 | 01 | 28 | 67 | 51 | 75 | 66 | 33 | 97 | 47 | 58 | 42 | 44 | 88 | 09 | 28 | 58 | 06 |
| 67 | 92 | 65 | 41 | 45 | 36 | 77 | 96 | 46 | 21 | 14 | 39 | 56 | 36 | 70 | 15 | 74 | 43 | 62 | 69 | 82 | 30 | 77 | 28 | 77 |
| 72 | 56 | 73 | 44 | 26 | 04 | 62 | 81 | 15 | 35 | 79 | 26 | 99 | 57 | 28 | 22 | 25 | 94 | 80 | 62 | 95 | 48 | 98 | 23 | 86 |
| 28 | 86 | 85 | 64 | 94 | 11 | 58 | 78 | 45 | 36 | 34 | 45 | 91 | 38 | 51 | 10 | 68 | 36 | 87 | 81 | 16 | 77 | 30 | 19 | 36 |
| 69 | 57 | 40 | 80 | 44 | 94 | 60 | 82 | 94 | 93 | 98 | 01 | 48 | 50 | 57 | 69 | 60 | 77 | 69 | 60 | 74 | 22 | 05 | 77 | 17 |
| 71 | 20 | 03 | 30 | 79 | 25 | 74 | 17 | 78 | 34 | 54 | 45 | 04 | 77 | 42 | 59 | 75 | 78 | 64 | 99 | 37 | 03 | 18 | 03 | 36 |
| 89 | 98 | 55 | 98 | 22 | 45 | 12 | 49 | 82 | 71 | 57 | 33 | 28 | 69 | 50 | 59 | 15 | 09 | 25 | 79 | 39 | 42 | 84 | 18 | 70 |
| 58 | 74 | 82 | 81 | 14 | 02 | 01 | 05 | 77 | 94 | 65 | 57 | 70 | 39 | 42 | 48 | 56 | 84 | 31 | 59 | 18 | 70 | 41 | 74 | 60 |
| 50 | 54 | 73 | 81 | 91 | 07 | 81 | 26 | 25 | 45 | 49 | 61 | 22 | 88 | 41 | 20 | 00 | 15 | 59 | 93 | 51 | 60 | 65 | 65 | 63 |
| 49 | 33 | 72 | 90 | 10 | 20 | 65 | 28 | 44 | 63 | 95 | 86 | 75 | 78 | 69 | 24 | 41 | 65 | 86 | 10 | 34 | 10 | 32 | 00 | 93 |
| 11 | 85 | 01 | 43 | 65 | 02 | 85 | 69 | 56 | 88 | 34 | 29 | 64 | 35 | 48 | 15 | 70 | 11 | 77 | 83 | 01 | 34 | 82 | 91 | 04 |
| 34 | 22 | 46 | 41 | 84 | 74 | 27 | 02 | 57 | 77 | 47 | 93 | 72 | 02 | 95 | 63 | 75 | 74 | 69 | 69 | 61 | 34 | 31 | 92 | 13 |

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## TABLES

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| 95 | 82 | 20 | 95 | 52 | 65 | 95 | 03 | 48 | 75 | 64 | 25 | 04 | 13 | 85 | 80 | 13 | 37 | 08 | 18 | 09 | 28 | 63 | 07 | 69 |
| 44 | 06 | 82 | 49 | 28 | 27 | 34 | 53 | 42 | 35 | 44 | 12 | 40 | 64 | 35 | 06 | 28 | 14 | 37 | 23 | 97 | 88 | 07 | 60 | 80 |
| 99 | 22 | 26 | 64 | 15 | 71 | 06 | 96 | 22 | 98 | 77 | 46 | 78 | 57 | 51 | 22 | 64 | 82 | 37 | 99 | 96 | 27 | 25 | 87 | 77 |
| 08 | 44 | 26 | 12 | 87 | 72 | 42 | 13 | 57 | 77 | 61 | 07 | 94 | 24 | 62 | 17 | 76 | 19 | 45 | 18 | 98 | 11 | 47 | 40 | 31 |
| 14 | 96 | 76 | 08 | 87 | 82 | 09 | 72 | 81 | 22 | 87 | 70 | 81 | 98 | 78 | 98 | 37 | 22 | 32 | 25 | 38 | 45 | 38 | 08 | 31 |
| 27 | 86 | 41 | 53 | 58 | 16 | 49 | 99 | 19 | 08 | 62 | 98 | 79 | 81 | 98 | 15 | 03 | 62 | 82 | 93 | 68 | 24 | 14 | 44 | 50 |
| 99 | 67 | 81 | 61 | 25 | 52 | 97 | 87 | 98 | 15 | 85 | 99 | 01 | 86 | 59 | 00 | 11 | 39 | 32 | 53 | 49 | 18 | 62 | 51 | 65 |
| 89 | 14 | 37 | 94 | 03 | 22 | 32 | 45 | 42 | 61 | 97 | 83 | 04 | 26 | 30 | 48 | 49 | 40 | 99 | 99 | 69 | 96 | 13 | 94 | 21 |
| 34 | 18 | 53 | 15 | 82 | 42 | 02 | 58 | 32 | 14 | 83 | 78 | 02 | 82 | 49 | 25 | 62 | 91 | 14 | 94 | 70 | 72 | 64 | 50 | 51 |
| 72 | 11 | 79 | 75 | 79 | 36 | 07 | 12 | 92 | 61 | 89 | 93 | 77 | 82 | 08 | 23 | 74 | 75 | 67 | 56 | 87 | 45 | 35 | 13 | 44 |
| 19 | 72 | 57 | 61 | 99 | 08 | 62 | 02 | 26 | 82 | 52 | 90 | 72 | 51 | 94 | 84 | 59 | 79 | 34 | 19 | 95 | 76 | 21 | 49 | 91 |
| 96 | 99 | 76 | 63 | 90 | 27 | 60 | 94 | 15 | 70 | 17 | 74 | 92 | 31 | 85 | 24 | 47 | 55 | 64 | 51 | 91 | 47 | 13 | 39 | 69 |
| 44 | 15 | 86 | 76 | 18 | 15 | 57 | 29 | 51 | 62 | 95 | 84 | 20 | 83 | 01 | 11 | 90 | 66 | 80 | 81 | 40 | 48 | 65 | 87 | 35 |
| 33 | 83 | 94 | 07 | 50 | 18 | 89 | 86 | 16 | 50 | 09 | 97 | 04 | 76 | 51 | 41 | 20 | 56 | 50 | 20 | 33 | 58 | 70 | 10 | 22 |
| 53 | 07 | 06 | 16 | 30 | 84 | 43 | 40 | 57 | 82 | 18 | 09 | 47 | 16 | 69 | 41 | 08 | 38 | 24 | 02 | 16 | 41 | 58 | 89 | 58 |

## TABLES

TABLE A-37. SHORT TABLE OF RANDOM NORMAL DEVIATES

 $m = 0, \sigma = 1$ 

|        |        |        |        |        |        |        |        |        |        |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 0.048  | 1.040  | -0.111 | -0.120 | 1.396  | -0.393 | -0.220 | 0.422  | 0.233  | 0.197  |
| -0.521 | -0.563 | -0.116 | -0.512 | -0.518 | -2.194 | 2.261  | 0.461  | -1.533 | -1.836 |
| -1.407 | -0.213 | 0.948  | -0.073 | -1.474 | -0.236 | -0.649 | 1.555  | 1.285  | -0.747 |
| 1.822  | 0.898  | -0.691 | 0.972  | -0.011 | 0.517  | 0.808  | 2.651  | -0.650 | 0.592  |
| 1.346  | -0.137 | 0.952  | 1.467  | -0.352 | 0.309  | 0.578  | -1.881 | -0.488 | -0.329 |
| 0.420  | -1.085 | -1.578 | -0.125 | 1.337  | 0.169  | 0.551  | -0.745 | -0.588 | 1.810  |
| -1.760 | -1.868 | 0.677  | 0.545  | 1.465  | 0.572  | -0.770 | 0.655  | -0.574 | 1.262  |
| -0.959 | 0.061  | -1.260 | -0.573 | -0.646 | -0.697 | -0.026 | -1.115 | 3.591  | -0.519 |
| 0.561  | -0.534 | -1.730 | -1.172 | -0.261 | -0.049 | 0.173  | 0.027  | 1.138  | 0.524  |
| -0.717 | 0.254  | 0.421  | -1.891 | 2.592  | -1.443 | -0.061 | -2.520 | -0.497 | 0.909  |
| -2.097 | -0.180 | -1.298 | -0.647 | 0.159  | 0.769  | -0.735 | -0.343 | 0.966  | 0.595  |
| 0.443  | -0.191 | 0.705  | 0.420  | -0.486 | -1.038 | -0.396 | 1.406  | 0.327  | 1.198  |
| 0.481  | 0.161  | -0.044 | -0.864 | -0.587 | -0.037 | -1.304 | -1.544 | 0.946  | -0.344 |
| -2.219 | -0.123 | -0.260 | 0.680  | 0.224  | -1.217 | 0.052  | 0.174  | 0.692  | -1.068 |
| 1.723  | -0.215 | -0.158 | 0.369  | 1.073  | -2.442 | -0.472 | 2.060  | -3.246 | -1.020 |
| -0.937 | 1.253  | 0.321  | -0.541 | -0.648 | 0.265  | 1.487  | -0.554 | 1.890  | 0.499  |
| -0.568 | -0.146 | 0.285  | 1.337  | -0.840 | 0.361  | -0.468 | 0.746  | 0.470  | 0.171  |
| -1.717 | -1.293 | -0.556 | -0.545 | 1.344  | 0.320  | -0.087 | 0.418  | 1.076  | 1.669  |
| -0.151 | -0.266 | 0.920  | -2.370 | 0.484  | -1.915 | -0.268 | 0.718  | 2.075  | -0.975 |
| 2.278  | -1.819 | 0.245  | -0.163 | 0.980  | -1.629 | -0.094 | -0.573 | 1.548  | -0.896 |
| -0.650 | 0.669  | -0.761 | 0.154  | 0.872  | 0.914  | -0.563 | -1.434 | -0.006 | -0.975 |
| -1.086 | 0.810  | 0.461  | -0.528 | 2.130  | -0.218 | 0.111  | -0.412 | -0.580 | -1.487 |
| -0.143 | -1.196 | -1.254 | -0.133 | 0.937  | -0.475 | -2.348 | 0.618  | -0.057 | -0.710 |
| -2.072 | 0.711  | 1.241  | 0.066  | -0.341 | 0.356  | 1.220  | 0.431  | 0.263  | -1.623 |
| -0.394 | -0.368 | -2.108 | 0.605  | 0.485  | 2.068  | 0.687  | -1.474 | 0.071  | -1.196 |
| 0.174  | -1.131 | 0.870  | 2.114  | 0.201  | -0.373 | -0.284 | -0.234 | -2.087 | -1.304 |
| 0.020  | 0.102  | -1.911 | -1.132 | 1.267  | 0.420  | 0.791  | 1.548  | -0.147 | -0.453 |
| 0.297  | 0.449  | -0.604 | -0.858 | -1.739 | 1.143  | 0.131  | 0.740  | -1.596 | 0.165  |
| 1.160  | 0.253  | 0.716  | -1.032 | -0.595 | -1.662 | 0.632  | -0.315 | -0.374 | 0.700  |
| -0.351 | -0.490 | -0.632 | -0.409 | -0.116 | -1.153 | -0.266 | -0.125 | 0.489  | -0.366 |
| -0.594 | -0.214 | -0.461 | 0.030  | -0.595 | -0.889 | 0.638  | -0.488 | 0.418  | -0.693 |
| -1.882 | 1.890  | -0.236 | 0.006  | 0.966  | -0.723 | 0.229  | -2.136 | -1.017 | -0.008 |
| 0.041  | 2.955  | -1.526 | 2.114  | -0.540 | 1.040  | 0.753  | 0.025  | 0.462  | 1.221  |
| -0.403 | 1.237  | -1.938 | -1.704 | -0.103 | -0.346 | 1.214  | 0.826  | 0.336  | -1.140 |
| -0.068 | 0.599  | 0.192  | 1.503  | -0.579 | -1.485 | -1.645 | 0.302  | -1.348 | 0.553  |
| -0.361 | 0.958  | 0.807  | 0.787  | -0.547 | -0.074 | -1.378 | -0.010 | -1.096 | 0.789  |
| -0.251 | 0.629  | 0.459  | -0.165 | 0.016  | 0.489  | -1.205 | -0.260 | -0.256 | -0.399 |
| -1.011 | 0.893  | -0.741 | -0.514 | -0.576 | -0.929 | 0.478  | -0.374 | 1.950  | -0.695 |
| 0.780  | -2.464 | -0.522 | 0.767  | -1.657 | -0.983 | 0.217  | -0.529 | -0.648 | 1.454  |
| -0.712 | -0.355 | -0.564 | 1.052  | -0.169 | -0.410 | 1.543  | -2.330 | -0.008 | -0.955 |
| -0.612 | -1.068 | -0.644 | -0.007 | -0.835 | 0.623  | 0.093  | 0.105  | -0.318 | -0.228 |
| -0.064 | 0.012  | -0.676 | 0.349  | 0.303  | 1.539  | 0.792  | -0.101 | -0.344 | -0.096 |
| -0.379 | 1.504  | 2.375  | 0.498  | -0.996 | 0.174  | -1.268 | -1.137 | -0.618 | 0.173  |
| 1.145  | -1.403 | 0.770  | 0.799  | 0.844  | -1.361 | -1.059 | 0.128  | 1.398  | 0.277  |
| -0.117 | 0.585  | -1.763 | -0.632 | 0.239  | -0.854 | 1.684  | 1.024  | -0.067 | -0.045 |
| 1.333  | 1.374  | -0.515 | -1.655 | 0.607  | -0.885 | -0.902 | -1.010 | -1.297 | -0.139 |
| -0.249 | -0.747 | 1.044  | -0.930 | 0.346  | 0.575  | 0.335  | -1.159 | -1.651 | -1.642 |
| -1.022 | 0.085  | -1.441 | -0.198 | 0.844  | 0.697  | 0.548  | -0.080 | 0.656  | 0.443  |
| -0.780 | -0.534 | -0.339 | -0.642 | -0.902 | -0.827 | 0.071  | -0.678 | -0.359 | -0.479 |
| -0.687 | -0.418 | 0.991  | 0.331  | -1.003 | 0.061  | -1.416 | 0.876  | 0.125  | -2.246 |

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## TABLES

TABLE A-37 (Continued). SHORT TABLE OF RANDOM NORMAL DEVIATES

 $m = 0, \sigma = 1$ 

|        |        |        |        |        |        |        |        |        |        |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| -0.670 | 0.518  | 0.387  | 0.523  | 0.641  | 1.243  | 0.322  | -2.607 | -1.097 | -0.012 |
| -2.912 | 1.448  | 1.343  | -0.122 | 0.726  | -0.617 | 0.609  | 2.319  | -0.450 | -1.197 |
| -0.028 | -0.790 | 0.057  | 1.425  | 1.940  | 1.161  | -0.878 | -0.716 | -0.244 | -1.151 |
| -1.257 | 0.774  | 0.003  | 0.388  | 1.060  | 1.028  | -0.236 | 1.172  | 0.442  | -0.157 |
| 2.372  | -1.376 | -1.318 | 1.236  | 0.738  | 0.337  | -0.534 | 0.090  | 0.886  | 0.676  |
| -0.970 | 0.438  | -0.672 | -0.180 | 0.667  | 1.370  | -0.481 | 0.329  | 0.842  | 0.449  |
| -1.228 | 0.129  | -0.426 | -0.165 | 0.028  | 2.696  | 1.201  | -1.351 | 0.724  | -1.017 |
| -0.369 | 0.310  | 0.432  | 0.237  | 0.884  | -1.224 | 0.539  | 0.852  | 0.497  | -0.283 |
| 1.161  | 1.219  | 1.615  | 0.336  | 1.100  | -0.528 | 0.161  | 0.278  | 0.675  | -1.143 |
| -0.284 | 2.609  | 0.792  | 1.825  | -0.249 | 1.654  | 0.621  | 0.979  | -1.472 | -1.173 |
| -0.578 | -0.789 | 0.106  | 0.832  | -0.597 | 0.496  | -0.561 | -1.033 | -0.578 | -0.378 |
| 0.074  | 0.261  | -0.766 | -1.046 | 0.361  | -0.043 | -1.927 | 1.527  | 0.605  | 1.475  |
| 0.230  | 0.046  | 0.978  | -1.901 | 1.162  | -0.545 | 0.697  | 1.151  | 2.033  | 0.080  |
| 2.162  | -0.562 | 1.190  | 0.925  | -1.057 | 0.015  | -1.371 | 1.067  | -1.080 | -1.129 |
| -1.020 | -1.130 | -0.315 | 0.628  | -0.140 | 2.050  | -0.030 | -0.629 | 0.128  | -1.221 |
| 1.323  | -0.836 | -0.284 | -0.249 | -0.768 | 1.242  | -0.879 | -0.417 | 0.013  | -0.502 |
| 2.329  | 1.884  | 0.033  | 0.598  | -0.217 | 0.260  | 0.431  | -1.914 | 0.205  | 1.155  |
| 2.761  | 1.800  | -0.562 | 0.714  | -0.407 | 0.009  | -0.724 | -1.168 | 0.247  | 1.166  |
| -0.232 | 0.605  | -0.023 | -0.531 | 0.542  | -0.155 | 0.697  | 1.037  | -0.316 | -0.003 |
| -0.742 | 0.210  | -0.741 | -1.099 | 0.158  | 2.112  | -0.765 | -0.319 | -0.247 | 0.345  |
| -1.410 | 0.413  | 0.705  | 1.444  | 1.057  | -0.843 | 0.043  | -0.571 | -0.001 | 0.203  |
| 2.272  | -0.719 | 0.679  | 2.007  | -0.180 | 0.698  | -1.137 | 0.688  | -0.571 | -0.100 |
| 2.832  | 0.925  | -1.350 | 1.529  | -0.260 | -1.007 | -2.350 | -1.501 | 0.289  | 1.522  |
| -1.086 | -0.558 | -0.973 | -1.285 | -0.021 | 0.077  | 0.915  | -0.241 | -0.249 | -0.529 |
| 0.134  | 1.815  | 0.313  | 1.571  | -0.216 | 2.261  | 0.696  | -0.130 | 0.393  | 0.017  |
| 0.783  | 0.600  | -0.745 | 1.127  | -0.684 | -0.519 | 0.125  | -0.499 | 1.543  | -0.082 |
| 0.174  | -0.897 | 0.575  | -0.751 | 0.694  | -2.959 | 0.529  | 1.587  | 0.339  | -0.813 |
| -1.319 | 0.556  | 2.963  | 1.218  | 1.199  | -1.746 | 1.611  | 0.467  | -0.490 | 0.202  |
| 1.298  | -0.940 | -1.143 | -1.136 | -1.516 | 0.548  | 0.629  | 0.250  | -1.087 | 0.322  |
| -0.676 | -1.107 | -1.483 | 0.278  | 0.493  | -0.442 | 1.078  | -0.336 | -0.177 | -0.057 |
| -1.287 | 0.775  | -1.095 | 1.161  | -1.877 | 1.874  | 1.703  | -1.619 | -0.725 | -1.407 |
| 0.260  | -0.028 | -1.982 | 0.811  | 0.999  | 1.662  | 0.908  | 1.476  | -1.137 | -0.945 |
| 0.481  | 1.060  | 1.441  | 0.163  | 0.720  | 1.490  | -0.026 | -0.502 | 0.427  | -0.351 |
| 0.794  | 0.725  | 1.971  | 0.384  | -0.579 | -1.079 | -1.440 | -0.859 | -0.346 | 0.077  |
| 0.584  | -0.554 | 1.460  | 0.791  | -0.426 | -0.682 | 0.430  | 1.922  | -2.099 | 0.221  |
| -0.114 | 0.379  | -0.698 | 1.570  | -0.511 | -0.725 | 0.680  | -0.591 | -1.091 | 0.357  |
| -1.128 | -1.707 | 0.921  | -0.859 | -1.566 | 1.523  | -0.900 | -0.988 | 0.264  | 0.282  |
| 0.691  | 0.153  | 0.076  | 1.691  | 0.553  | 0.457  | -1.107 | 0.322  | 0.633  | 0.007  |
| 1.115  | 0.777  | -0.738 | 0.868  | 1.484  | -1.792 | 0.950  | -0.842 | -0.192 | 0.620  |
| -0.389 | 0.559  | 0.670  | -0.315 | 1.234  | 0.475  | 1.117  | 1.286  | -0.649 | -1.880 |
| 0.330  | 0.750  | -0.642 | 0.148  | -0.608 | 0.866  | -1.720 | 0.653  | -0.210 | -0.959 |
| -0.333 | -0.084 | 1.239  | -0.049 | -0.095 | -0.197 | -0.213 | -1.420 | -0.491 | 0.102  |
| 1.718  | 1.111  | -0.548 | -0.653 | 1.534  | -0.456 | -0.395 | 1.614  | -0.531 | -0.785 |
| -0.182 | 0.620  | 1.178  | -1.071 | 0.444  | -0.072 | -1.001 | 1.325  | -0.302 | -1.119 |
| 1.260  | -1.192 | 0.182  | -0.397 | -0.705 | -1.085 | -1.492 | 1.642  | 0.673  | -0.707 |
| -1.204 | -1.725 | 1.695  | 1.473  | 0.665  | -0.489 | 0.020  | 0.267  | 1.230  | 0.865  |
| -0.619 | 0.307  | -0.226 | -0.096 | 0.987  | -1.195 | -1.412 | 0.433  | 2.052  | 0.022  |
| -0.272 | -0.096 | 0.137  | -0.361 | 0.653  | -0.156 | 1.309  | -0.480 | -0.397 | 1.302  |
| 0.245  | -0.690 | 0.493  | -1.123 | 1.465  | 0.132  | 0.582  | -0.429 | 0.225  | 0.125  |
| 0.101  | -0.855 | 0.782  | -1.040 | 2.113  | -1.423 | -1.010 | 0.158  | 0.106  | -1.232 |



## TABLES

TABLE A-37 (Continued). SHORT TABLE OF RANDOM NORMAL DEVIATES

 $m = 0, \sigma = 1$ 

|        |        |        |        |        |        |        |        |        |        |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 0.117  | -0.136 | 0.820  | -1.213 | 0.131  | -0.738 | 0.918  | 1.002  | -0.846 | 0.288  |
| 0.519  | -0.787 | -1.128 | 1.100  | 1.609  | 0.797  | 0.382  | -1.157 | -1.320 | -2.056 |
| -0.876 | -0.832 | -0.788 | 1.490  | -0.923 | -0.710 | -2.149 | -1.967 | 0.088  | 1.158  |
| 0.311  | 0.494  | 0.357  | 0.025  | -0.016 | 0.448  | 0.733  | -0.199 | 0.440  | 0.609  |
| -1.041 | 0.627  | -0.957 | 0.777  | 0.304  | -0.581 | 1.495  | -1.564 | -1.471 | -1.097 |
| 0.239  | 0.061  | 1.091  | -0.060 | 0.521  | -0.777 | 0.461  | 0.919  | -0.091 | 1.412  |
| -0.151 | 0.664  | 0.596  | 0.370  | -0.346 | -0.526 | -1.557 | -0.180 | -0.323 | 0.918  |
| 0.962  | -0.502 | -0.967 | 0.859  | 0.916  | -1.525 | 0.064  | 1.023  | 0.001  | -1.577 |
| 1.573  | -1.912 | -1.010 | 1.780  | -0.771 | 2.390  | -0.188 | -0.593 | -0.608 | -0.561 |
| -0.742 | 0.137  | 0.563  | 0.887  | -0.740 | -1.410 | -0.818 | -0.545 | 1.130  | -0.741 |
| -0.143 | -1.299 | -1.869 | 0.191  | -0.789 | -0.296 | -2.232 | 0.268  | -1.582 | 0.389  |
| -1.433 | 1.169  | -0.733 | 1.176  | -0.582 | 1.060  | 0.447  | 0.305  | -2.418 | -1.209 |
| -1.946 | 1.045  | -1.705 | -1.544 | 1.701  | 0.972  | 0.346  | -0.341 | -1.240 | -0.194 |
| -0.885 | 0.247  | -1.230 | -1.461 | 0.175  | 2.072  | 1.174  | -0.223 | -1.106 | 0.028  |
| -0.046 | 0.513  | -0.201 | -0.740 | 0.727  | 0.668  | -0.433 | -0.991 | -0.174 | 1.421  |
| -0.683 | -0.161 | 0.964  | -1.182 | 0.485  | 0.901  | 1.321  | 0.803  | -0.727 | -0.569 |
| -0.749 | -0.029 | -1.150 | 0.122  | -0.016 | -0.690 | 1.261  | 1.884  | 0.758  | -0.035 |
| 0.995  | 0.542  | 0.448  | 0.796  | 0.616  | 0.261  | 1.072  | -1.153 | -1.866 | -1.029 |
| 0.274  | -0.188 | -0.846 | 1.557  | 0.554  | 0.514  | 0.723  | -0.322 | -0.805 | 0.178  |
| 1.120  | -0.396 | 2.110  | -1.469 | -0.589 | 0.779  | 0.338  | -0.093 | 1.629  | 0.134  |
| -0.668 | -0.678 | 0.406  | 0.092  | 0.944  | -0.728 | -0.358 | -1.206 | -0.783 | 0.510  |
| 1.583  | -0.730 | -0.911 | 0.126  | 1.864  | -0.296 | -0.980 | -1.022 | 0.315  | 0.274  |
| 1.050  | 1.162  | 1.236  | -2.039 | -1.299 | -0.722 | -0.630 | 1.359  | 0.511  | 0.448  |
| 0.477  | -0.433 | 0.110  | -0.182 | -0.363 | 0.716  | -1.355 | 1.579  | -0.574 | 0.043  |
| -1.538 | 0.137  | -0.382 | 0.578  | 1.053  | 0.489  | 1.552  | 1.520  | 0.391  | -1.026 |
| -0.314 | -0.889 | -0.913 | 0.417  | 0.537  | -0.426 | -0.100 | 1.467  | 0.483  | -0.627 |
| 0.730  | -0.946 | -0.231 | -0.671 | -0.798 | 1.330  | -1.006 | -0.123 | 0.442  | 1.513  |
| 0.276  | -0.473 | 0.477  | 1.076  | 0.316  | -0.600 | -0.146 | 0.090  | -0.608 | -1.198 |
| -0.638 | -1.270 | -0.447 | -1.101 | -1.107 | -1.433 | 0.349  | 0.546  | -0.283 | 0.887  |
| 0.497  | -0.829 | 0.745  | 0.469  | 1.975  | 0.130  | 0.367  | 0.202  | -0.433 | 0.630  |
| -0.769 | -0.866 | -1.034 | -1.615 | 0.120  | 0.493  | 0.103  | -0.639 | 1.732  | 1.066  |
| -1.384 | 0.453  | 0.586  | -1.549 | -0.421 | 0.815  | -1.319 | -0.805 | -0.009 | -0.100 |
| 0.784  | 1.980  | -1.265 | 0.239  | 1.189  | -0.382 | 0.047  | -0.582 | 0.806  | -1.336 |
| -0.035 | -0.514 | -0.087 | -0.202 | 0.925  | -0.047 | -0.926 | -1.157 | 0.498  | -1.066 |
| 0.678  | 0.917  | 0.376  | 1.282  | -1.176 | 0.622  | 2.123  | 0.646  | -0.730 | 0.026  |
| 0.179  | 0.841  | -0.298 | -2.437 | -0.740 | -0.039 | 0.226  | 0.247  | -1.614 | 0.492  |
| 0.111  | -0.044 | 0.209  | 0.527  | 0.598  | -0.206 | -1.042 | -0.012 | 0.757  | 0.840  |
| 1.006  | -0.919 | 0.956  | 0.808  | 1.793  | -0.079 | 1.953  | -1.494 | 0.559  | 1.290  |
| -0.307 | -1.174 | -0.858 | 0.039  | -1.505 | 0.037  | -0.107 | 0.120  | 0.557  | 1.809  |
| -2.467 | 0.273  | -0.899 | -0.691 | -1.092 | -1.374 | 1.238  | 2.046  | 0.879  | 0.296  |
| 0.275  | -1.313 | -0.331 | 0.305  | 0.404  | -0.399 | 0.591  | 0.280  | -1.802 | 1.207  |
| -0.514 | -0.713 | 0.501  | 1.214  | 0.001  | 0.360  | -0.124 | 1.373  | 1.857  | -1.135 |
| 0.982  | -0.139 | 1.113  | -0.433 | -0.761 | 0.182  | -0.405 | 0.714  | -0.616 | -1.402 |
| -0.071 | -0.115 | -0.344 | 0.429  | 0.316  | -0.667 | 1.676  | -0.155 | 1.085  | -1.780 |
| -1.975 | -1.416 | 1.367  | -0.592 | 0.480  | 0.406  | 0.701  | 1.077  | -1.475 | 1.024  |
| 0.027  | -1.446 | -0.464 | -1.180 | 1.223  | -1.116 | -1.017 | 1.051  | 0.051  | -0.853 |
| 0.016  | -1.118 | -1.228 | 1.382  | -0.502 | 0.494  | -0.612 | 2.755  | -0.809 | -1.216 |
| 0.584  | -1.410 | -0.551 | -0.602 | -0.381 | -0.078 | -1.310 | 1.198  | 1.359  | 0.115  |
| 0.669  | -0.611 | -0.452 | 0.302  | -1.026 | -0.331 | -1.047 | 0.618  | 0.931  | -0.218 |
| 0.070  | -1.598 | -0.506 | -0.812 | 1.203  | -2.110 | 0.049  | 0.059  | 1.890  | 0.421  |

## TABLES

TABLE A-37 (Continued). SHORT TABLE OF RANDOM NORMAL DEVIATES

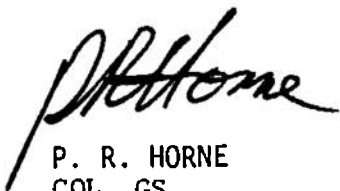
 $m = 0, \sigma = 1$ 

|        |        |        |        |        |        |        |        |        |        |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 1.801  | 0.459  | 1.102  | -1.072 | -0.336 | 0.942  | -0.290 | -0.716 | 1.396  | -0.466 |
| -0.175 | -0.754 | -0.134 | 1.231  | 1.483  | -0.149 | 0.555  | 1.401  | -1.142 | 0.205  |
| -0.861 | -1.460 | 0.526  | 0.239  | -0.206 | 2.021  | 0.313  | -0.253 | -0.891 | 1.135  |
| -0.577 | 0.335  | -0.820 | 0.140  | -0.333 | 0.426  | 0.209  | -0.024 | 0.323  | 1.223  |
| 0.827  | 0.802  | -0.457 | 0.560  | 0.643  | -0.729 | -0.249 | 0.338  | -0.281 | -1.804 |
| -1.344 | 0.949  | -1.459 | -1.210 | 1.016  | -0.148 | -1.737 | 0.069  | -1.185 | 0.040  |
| 1.476  | 1.262  | -1.428 | 0.489  | -0.523 | -0.646 | 1.721  | 0.749  | 0.179  | -0.922 |
| 0.527  | -1.045 | 0.877  | 0.646  | 2.957  | -0.972 | -1.796 | 0.309  | 2.224  | -0.070 |
| -0.645 | 0.117  | 0.059  | -0.080 | -1.637 | -0.746 | 1.256  | 2.520  | -0.673 | 0.994  |
| -0.514 | -1.510 | -0.714 | -1.581 | 0.905  | 1.745  | 1.767  | 0.682  | -0.648 | -1.742 |
| -0.656 | -0.217 | 0.287  | 0.114  | 1.175  | 0.791  | -0.263 | -0.695 | -1.348 | 1.239  |
| -0.778 | 1.177  | 0.180  | 1.156  | 0.458  | 1.089  | 0.339  | 1.304  | 0.402  | -0.831 |
| 0.352  | -1.829 | -0.645 | 0.236  | 0.641  | 0.920  | -1.287 | -0.187 | -2.339 | -0.237 |
| 1.352  | -0.076 | -1.962 | 0.827  | 0.252  | 1.621  | 0.770  | 1.324  | 0.488  | -0.037 |
| 0.017  | 0.030  | 0.211  | 2.276  | 0.693  | -1.733 | 0.773  | 0.652  | -0.947 | 0.148  |
| -0.218 | -1.060 | -0.553 | 1.043  | 2.305  | 0.380  | -0.794 | -1.498 | 1.088  | -0.689 |
| 1.118  | 0.816  | 0.713  | 0.485  | 0.185  | 0.318  | -1.050 | 0.110  | 0.563  | 1.177  |
| -1.622 | 0.436  | 0.481  | 0.021  | 2.070  | -0.845 | -0.257 | -0.680 | -0.565 | 0.024  |
| -1.103 | -0.210 | -1.088 | -0.033 | -1.022 | 0.366  | -0.531 | 2.022  | 0.210  | 1.037  |
| -0.677 | -0.737 | -0.950 | -1.517 | 1.148  | 0.377  | -0.397 | -1.902 | -0.748 | -1.753 |
| 1.110  | 1.120  | 1.163  | 1.577  | -1.172 | -0.133 | -0.213 | 0.154  | -0.435 | 0.218  |
| -0.278 | 0.569  | 0.586  | 1.523  | -0.244 | -0.170 | -1.274 | 0.874  | -1.020 | -0.809 |
| 0.178  | 1.314  | 0.462  | -0.253 | -0.122 | 0.108  | -1.256 | -0.137 | 1.043  | -0.135 |
| 0.312  | -2.287 | -0.655 | -1.459 | 0.075  | -0.457 | -0.206 | -0.326 | 0.489  | -0.149 |
| 0.469  | -2.066 | -0.973 | -1.009 | -1.410 | 0.505  | 0.459  | -0.572 | -1.186 | 0.978  |
| -0.730 | 1.650  | 0.760  | -0.520 | -0.671 | -0.122 | -0.324 | -0.202 | 0.411  | -2.103 |
| 0.834  | 0.280  | 0.744  | 0.598  | 0.122  | -0.460 | -1.310 | -1.271 | -0.917 | 0.650  |
| -1.397 | -1.053 | 0.412  | 1.286  | -0.820 | -0.371 | 0.826  | -0.666 | 0.505  | 0.733  |
| 0.238  | -0.668 | 1.861  | 0.051  | 0.460  | 0.079  | 1.008  | -0.487 | 0.306  | -0.061 |
| 0.102  | -0.907 | -0.833 | 1.103  | -0.921 | 0.145  | -0.904 | -0.401 | 0.553  | -1.422 |
| -0.160 | 0.567  | -0.638 | 0.355  | 0.427  | -0.695 | -0.846 | 0.359  | 1.500  | -0.926 |
| 0.496  | 1.179  | -0.776 | 0.511  | -1.325 | 0.275  | -0.130 | -0.123 | 1.175  | -0.102 |
| 0.307  | -0.328 | -2.474 | -0.121 | 1.371  | 0.266  | 1.235  | 1.827  | -0.296 | -2.715 |
| -0.559 | 0.523  | 1.264  | -0.018 | -2.791 | 0.139  | 1.515  | 1.976  | 0.173  | -1.728 |
| 0.658  | -0.261 | 0.004  | -1.296 | 0.568  | -1.215 | 0.104  | 0.178  | 1.126  | 1.134  |
| -0.856 | -2.278 | -0.140 | -0.164 | 1.416  | -0.043 | 0.243  | -1.399 | -0.448 | 0.120  |
| 2.778  | 0.245  | 0.282  | 0.301  | -1.506 | 1.805  | 1.798  | 1.078  | 1.629  | -0.648 |
| 0.543  | 0.761  | -2.038 | -0.533 | -0.594 | 1.742  | 0.487  | 1.432  | -0.210 | -0.358 |
| -0.008 | -0.445 | -2.551 | 0.935  | 1.961  | -0.270 | -1.557 | -1.318 | -0.744 | -0.860 |
| -1.147 | -1.151 | -0.522 | -2.118 | -0.667 | 0.906  | 0.639  | 1.005  | -0.480 | -1.354 |
| -0.851 | 0.585  | 0.672  | 0.481  | -0.888 | -0.480 | 0.041  | 0.345  | -0.537 | -0.589 |
| 0.023  | 0.609  | 0.623  | 0.356  | 0.279  | -0.051 | 0.158  | -0.353 | 0.776  | 0.102  |
| -0.257 | 0.152  | -1.413 | 0.175  | 0.149  | -1.354 | 0.286  | 1.794  | -0.571 | -0.202 |
| -0.421 | -0.344 | -0.803 | 0.832  | 0.256  | -1.296 | -1.390 | 0.379  | 0.955  | 0.366  |
| -1.681 | 2.444  | -1.025 | 1.178  | -0.827 | -0.200 | 0.727  | 0.778  | 0.169  | -1.363 |
| 0.717  | -1.666 | 1.071  | -2.061 | -1.367 | -0.450 | -0.038 | -1.004 | -1.240 | 0.901  |
| -1.266 | 0.256  | -1.312 | -0.582 | -0.351 | -1.002 | 0.648  | 0.873  | 0.015  | 0.641  |
| 0.350  | 0.552  | -1.549 | -1.680 | 1.417  | -0.769 | -0.514 | -1.900 | 1.017  | -1.222 |
| -0.186 | 0.006  | 0.148  | 0.560  | -1.081 | -0.637 | -1.968 | -0.623 | 0.009  | -0.369 |
| 1.359  | 1.027  | 0.740  | -2.067 | 0.543  | 1.099  | 0.543  | 0.064  | 0.589  | -0.016 |

(AMCRD-TV)

FOR THE COMMANDER:

OFFICIAL:

A handwritten signature in black ink, appearing to read 'P. R. Horne', written in a cursive style.

P. R. HORNE  
COL, GS  
Chief, Administrative Office

LEO B. JONES  
Major General, USA  
Chief of Staff

DISTRIBUTION:  
Special

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